

A GUIDE TO UNDERSTAND

COLLECTIVITY IN SMALL SYSTEMS

KATARINA KRIZKOVA GAJDOSOVA

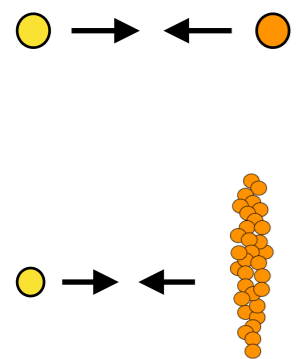
18.01.2019

OUTLINE

- Heavy-ion collisions
- Flow
- Collectivity in heavy-ion collisions

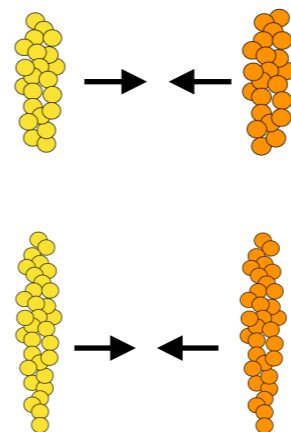
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- Heavy-ion collisions
- Flow
- Collectivity in heavy-ion collisions
- Small collision systems



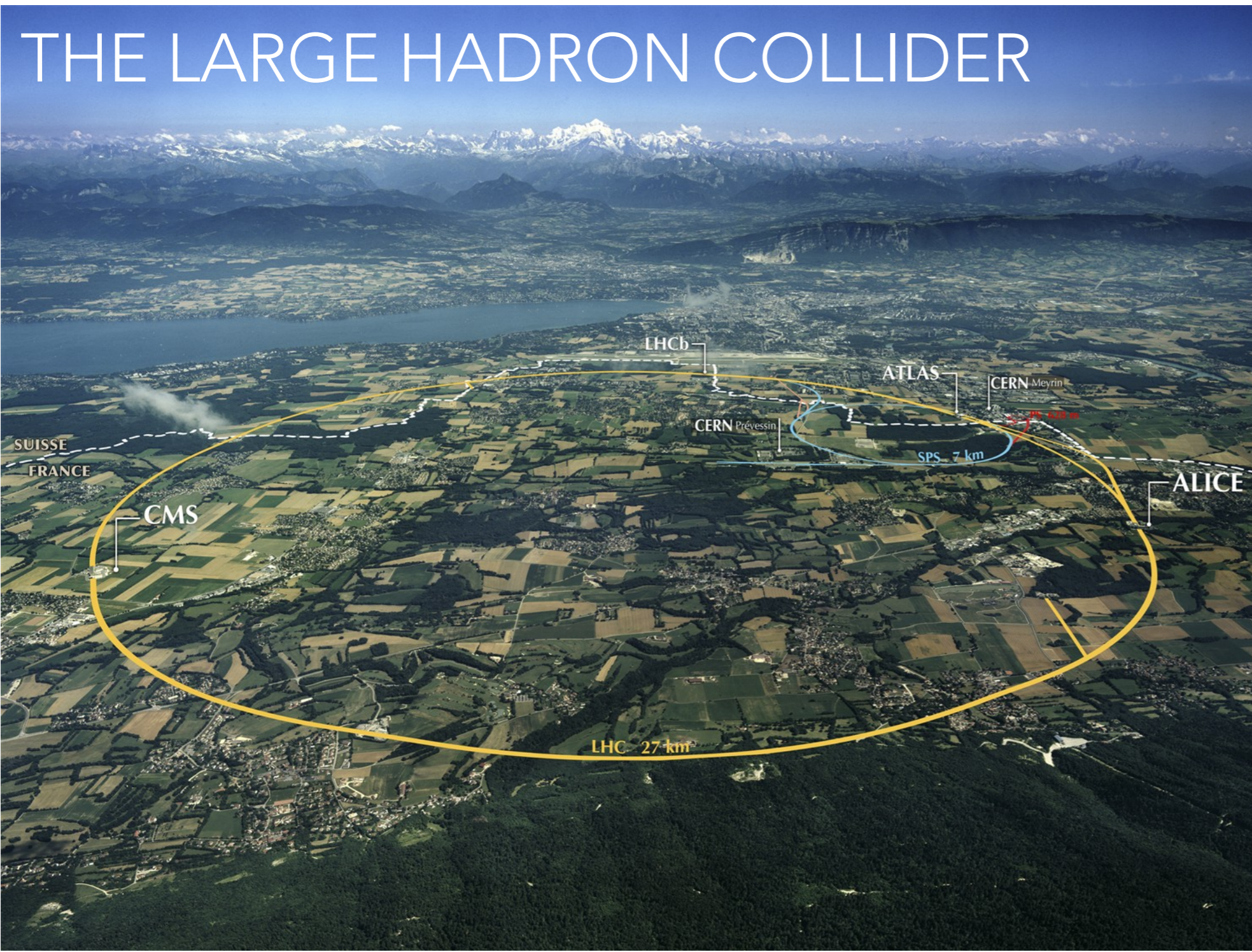
small systems

1+1 nucleon
1+208 nucleons



large systems

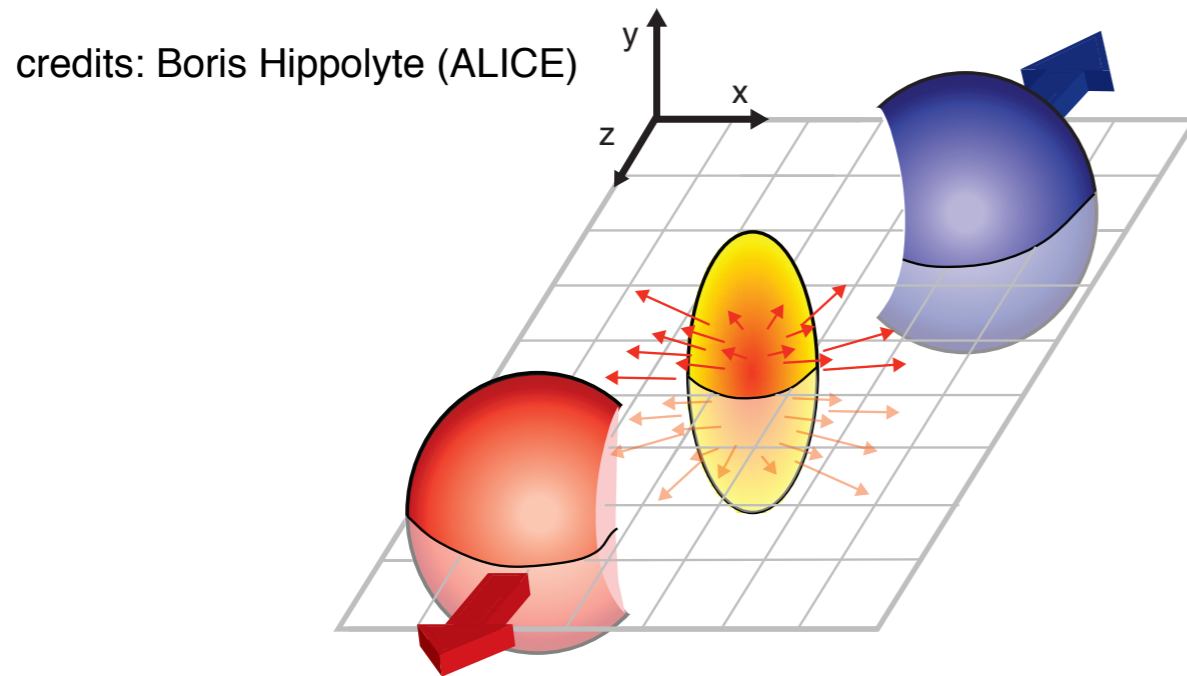
129+129 nucleons
208+208 nucleons



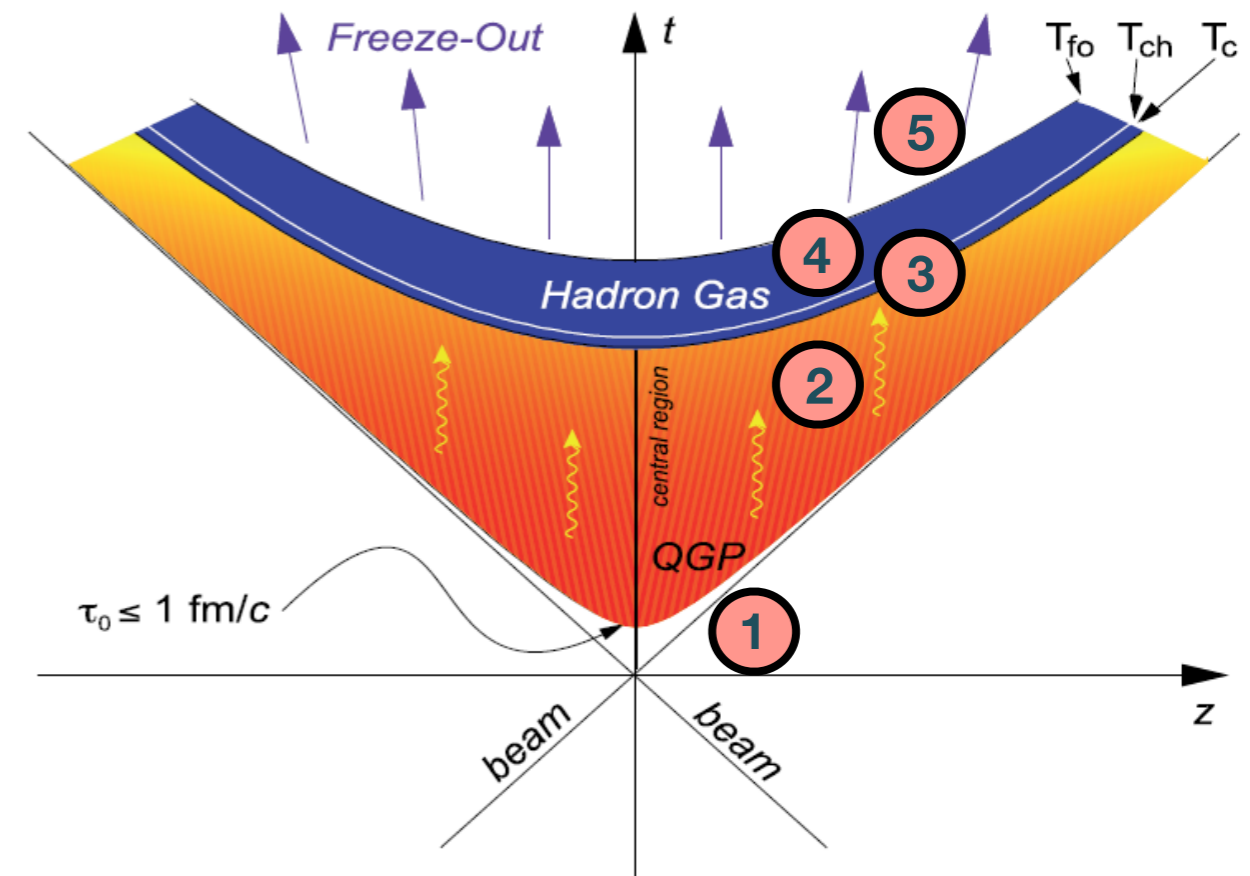
THE LARGE HADRON COLLIDER

- Collisions:
 - pp
 - p-Pb
 - Xe-Xe
 - Pb-Pb

HEAVY-ION COLLISION



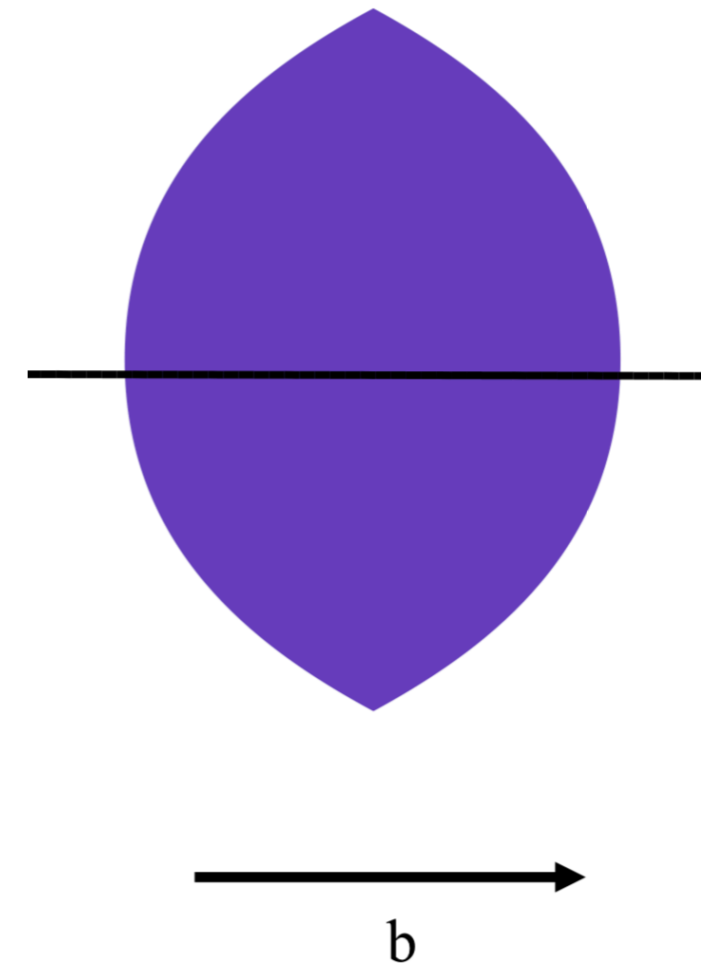
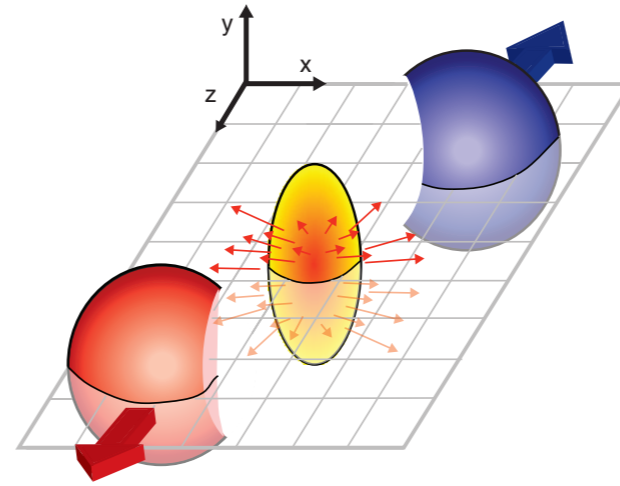
5. Freeze-out
4. Hadron gas
3. Phase transition
2. **Quark-Gluon Plasma**
1. Pre-equilibrium phase



arXiv: 0807.1610 [nucl-ex]

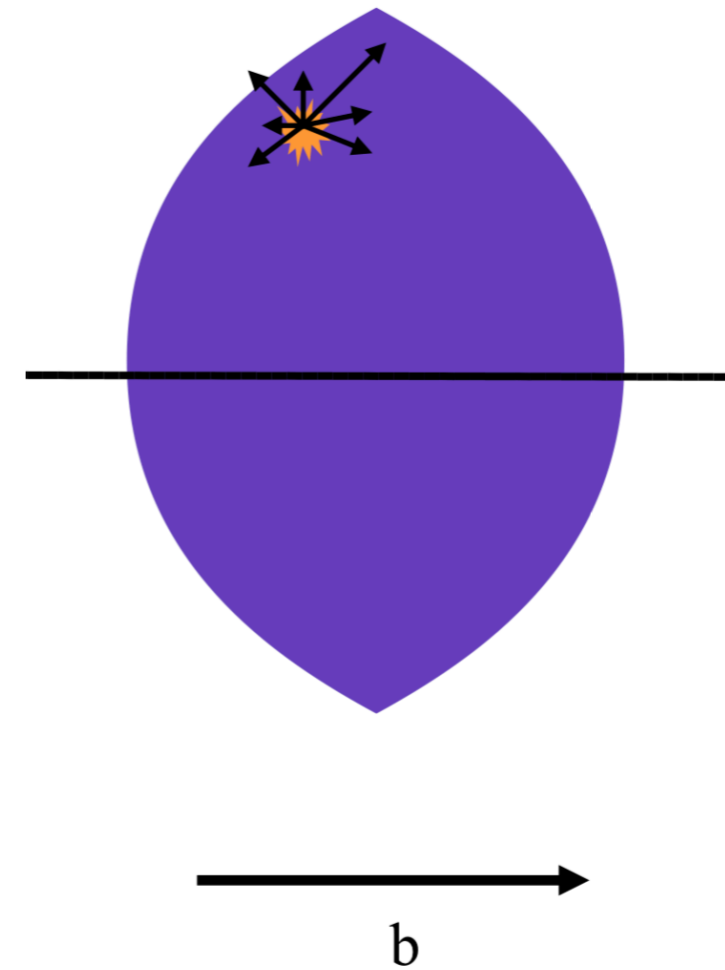
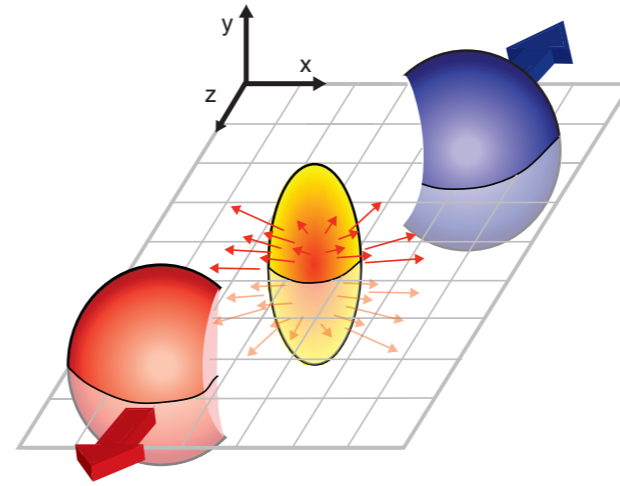
EVOLUTION OF A HEAVY-ION COLLISION

A. Superposition of independent pp collisions



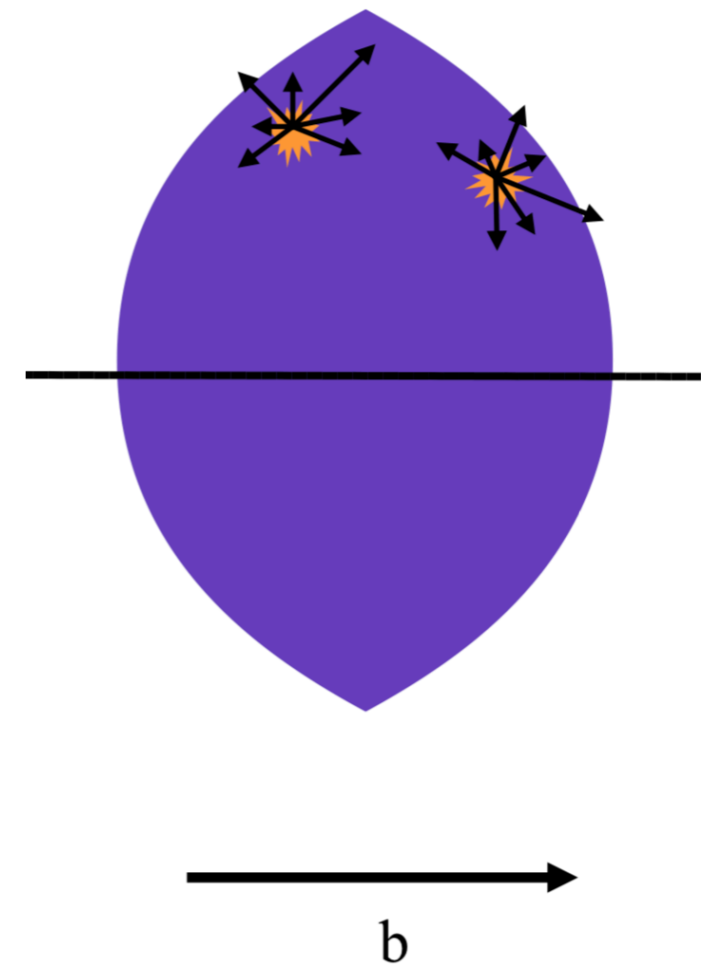
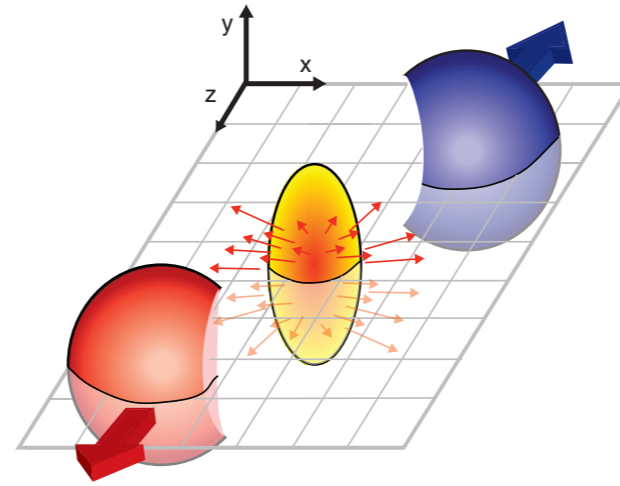
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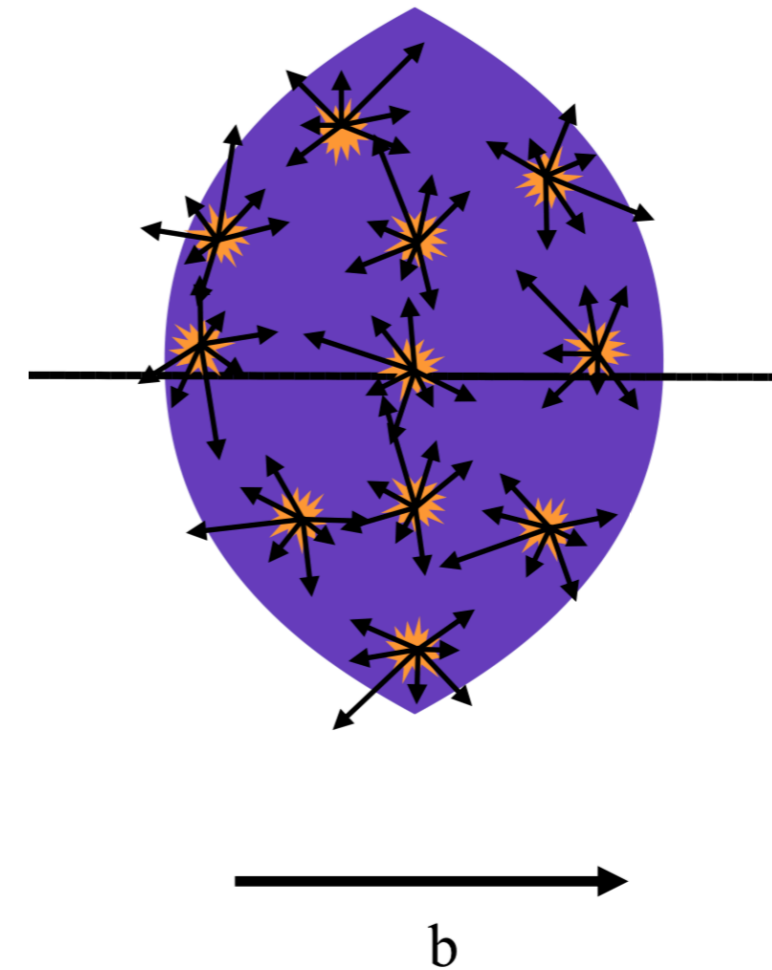
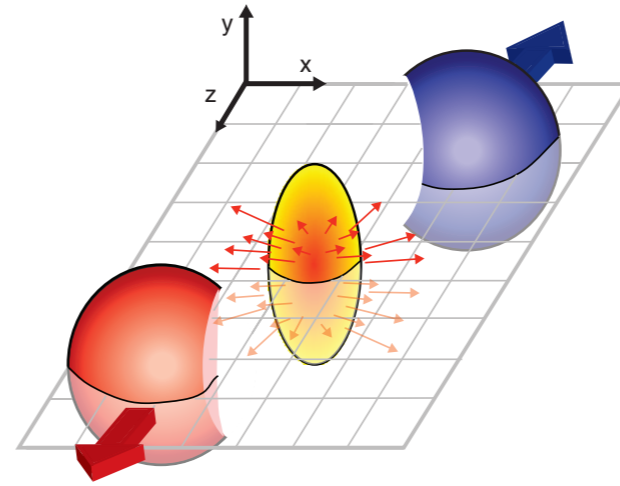
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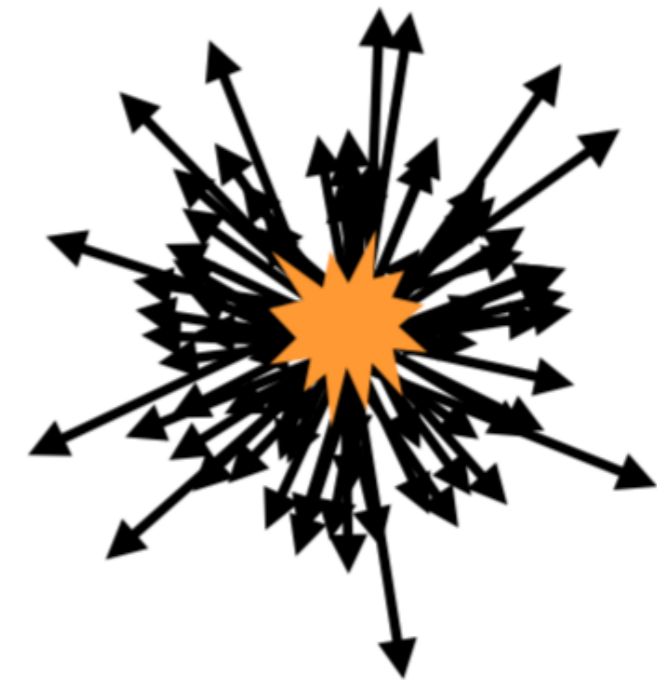
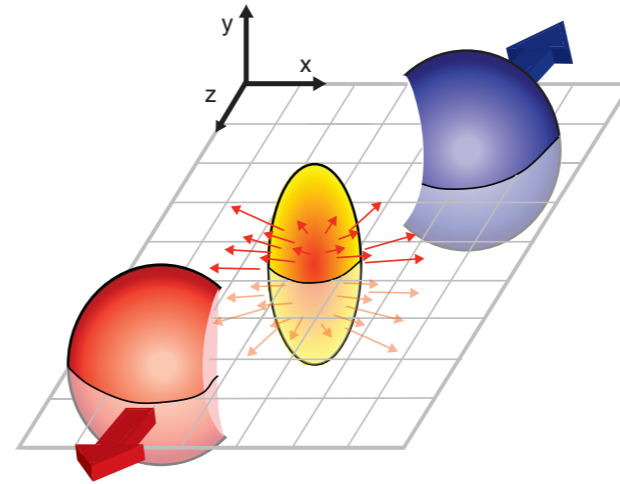
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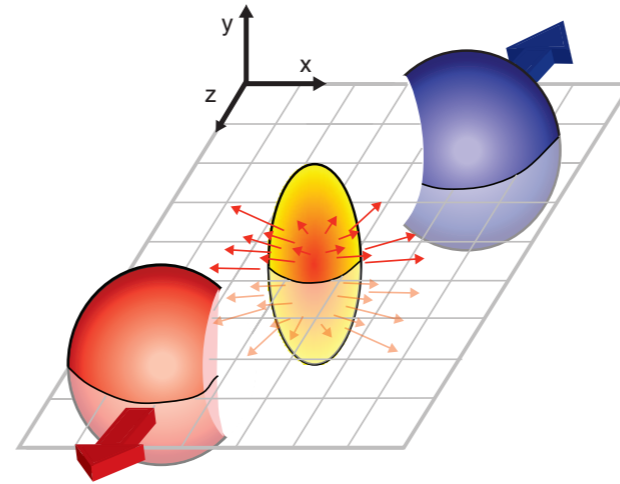
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- A. Superposition of independent pp collisions
- Particles emitted randomly

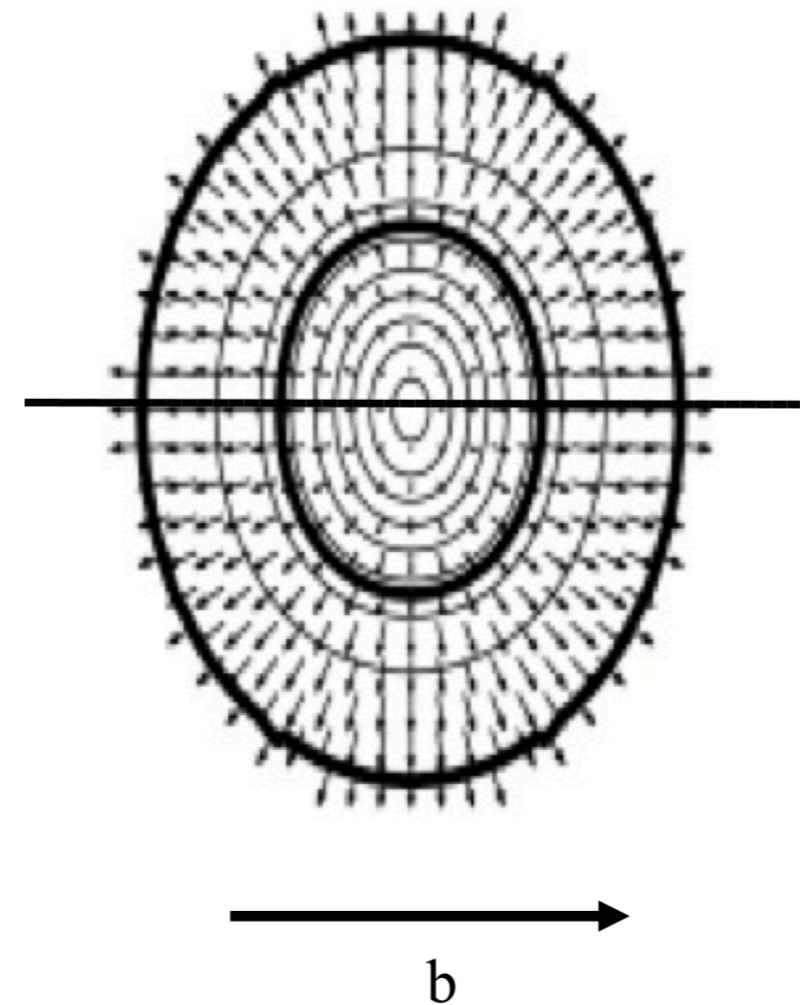


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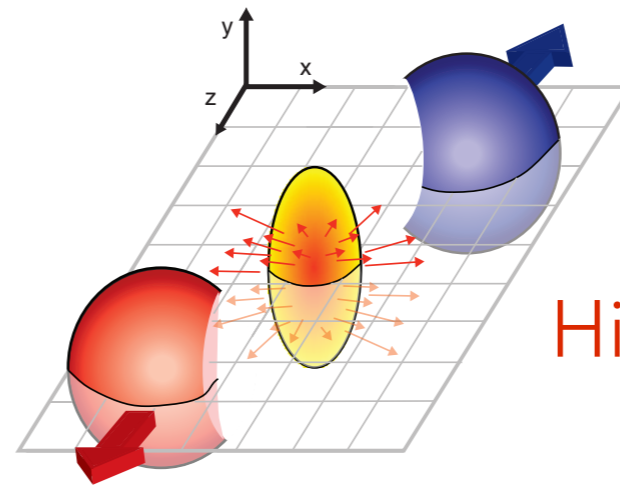


- B. Evolution as a bulk



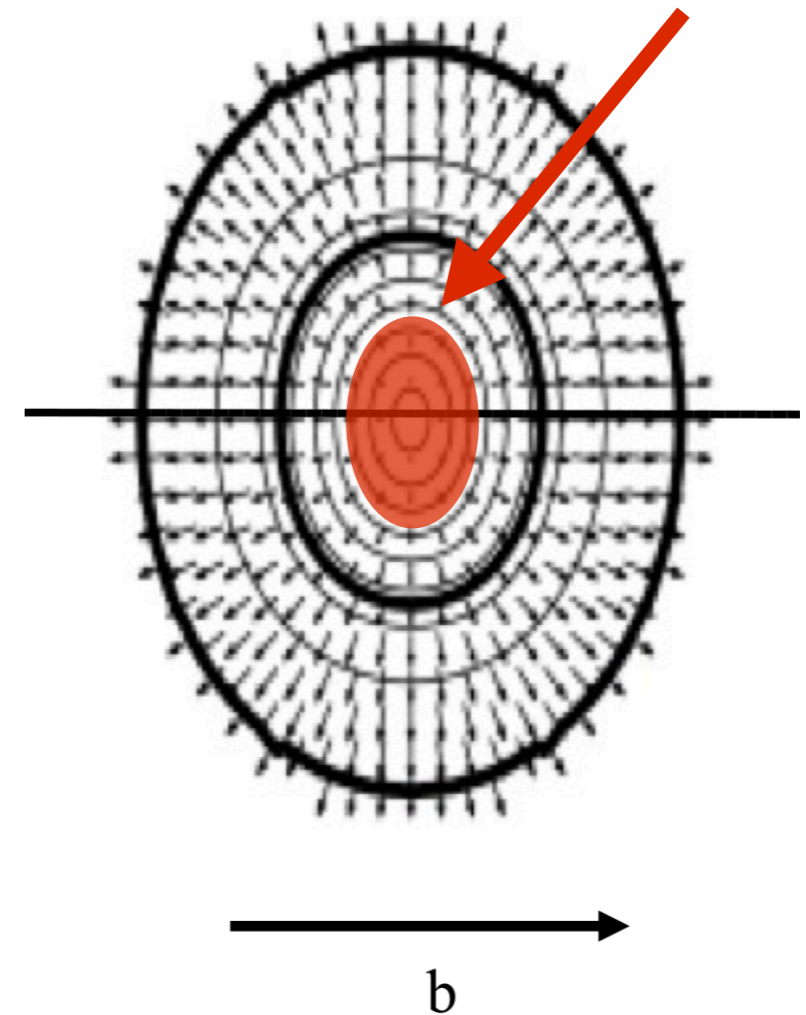
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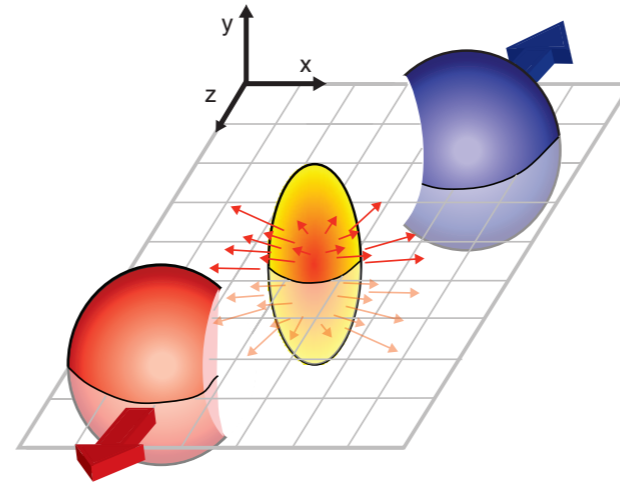
High pressure at the centre

- B. Evolution as a bulk



"Zero" pressure around

EVOLUTION OF A HEAVY-ION COLLISION

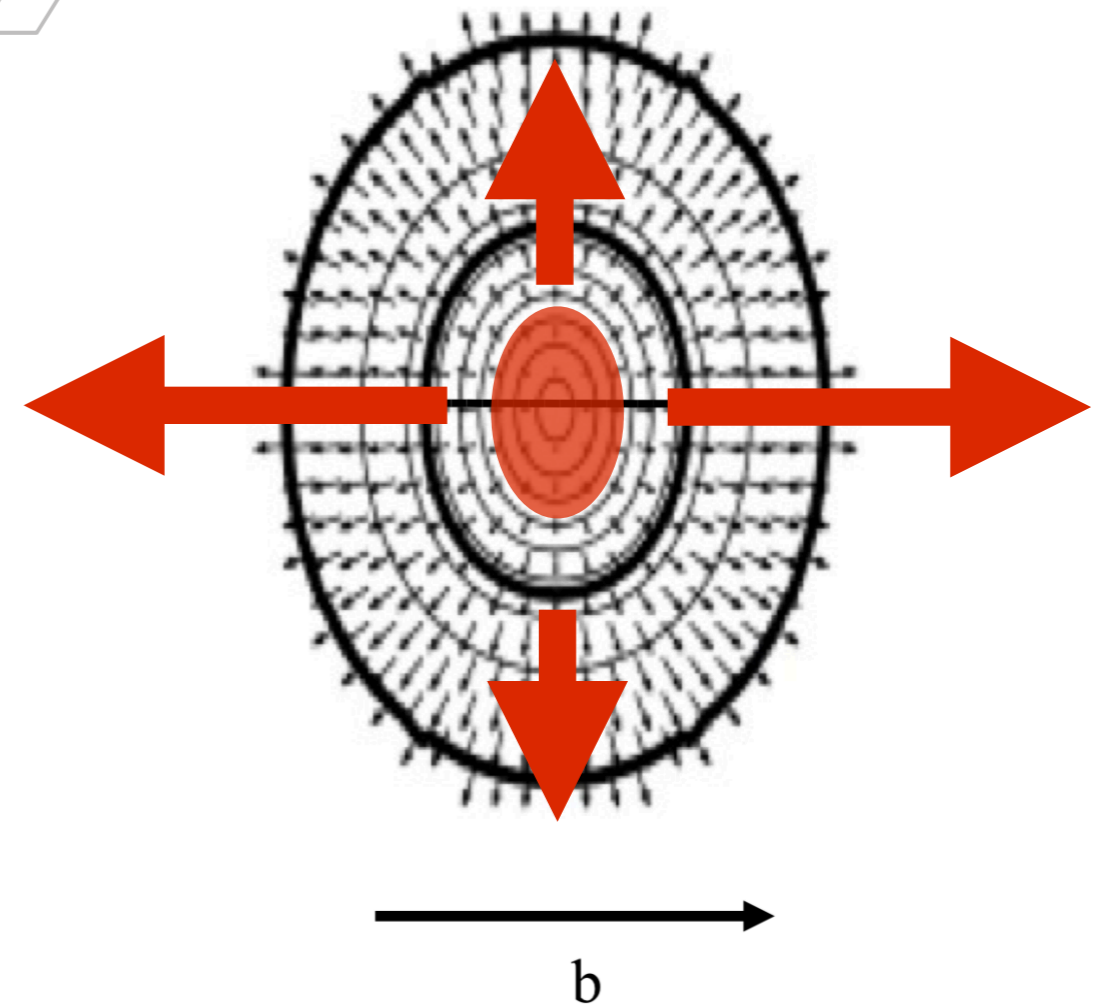


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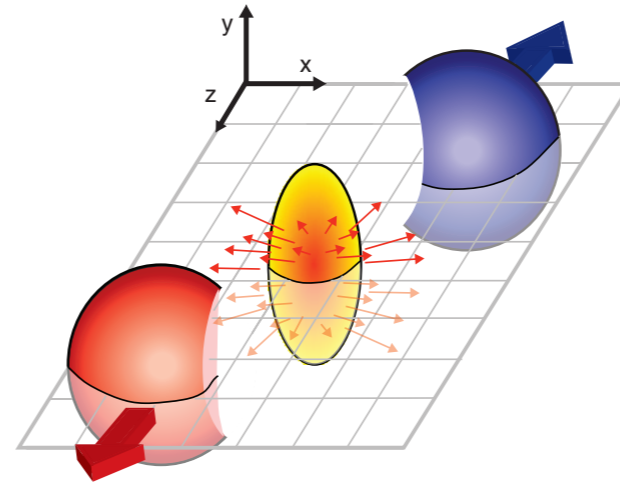
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- Particles are pushed out (with a preferred direction)



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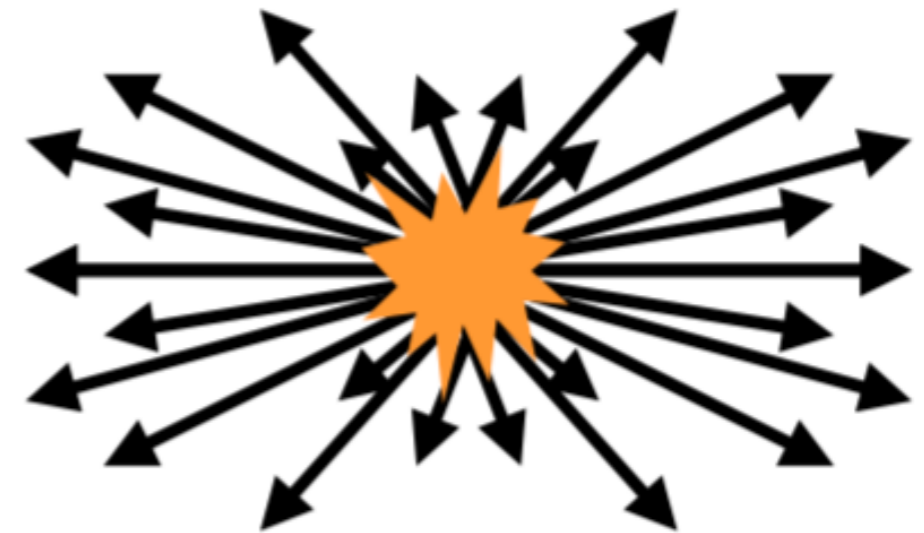


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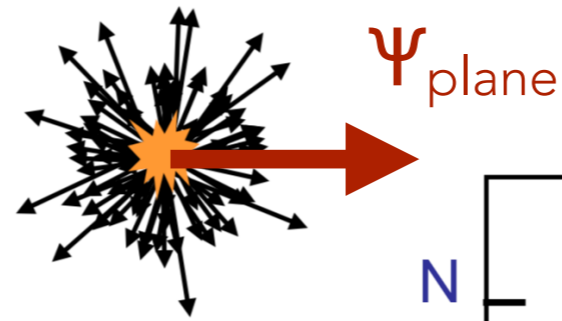
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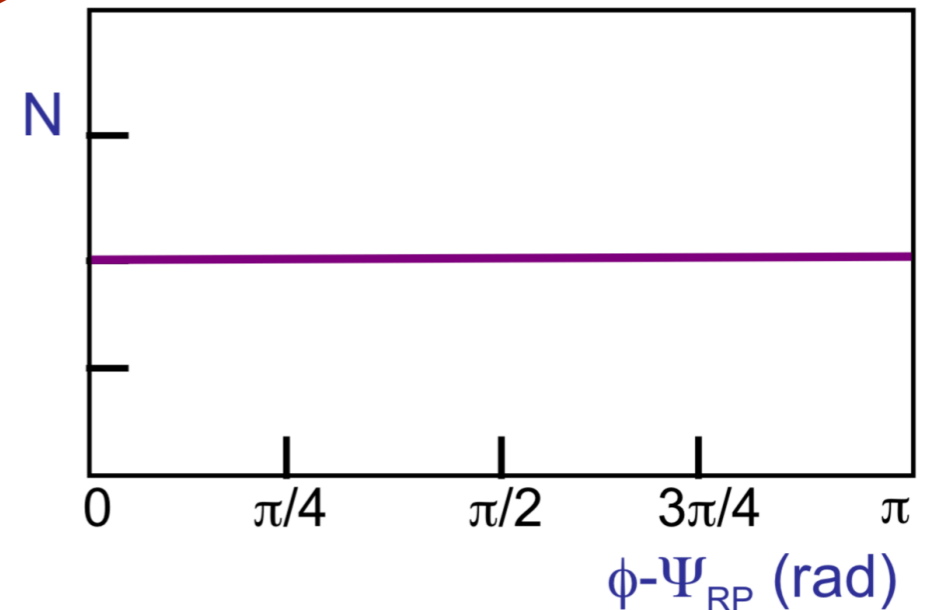


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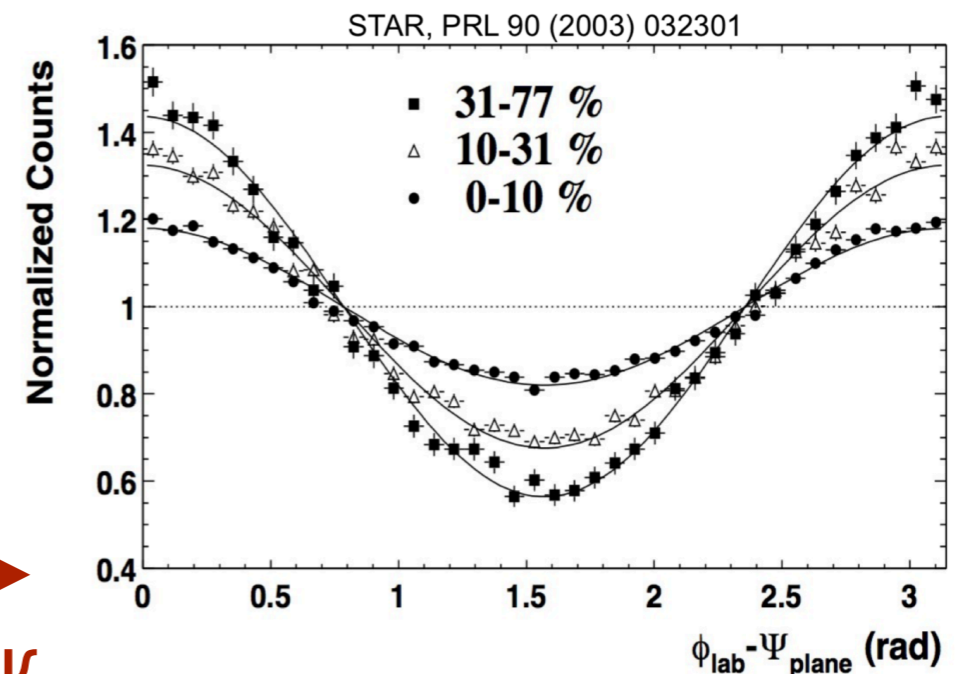
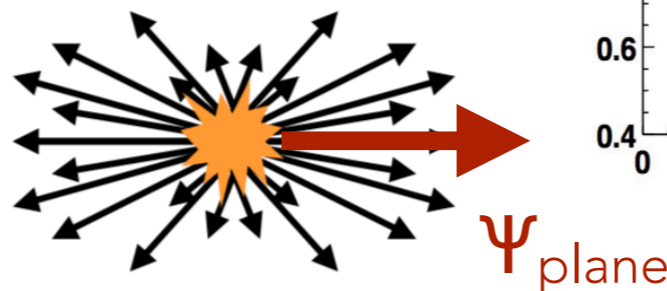
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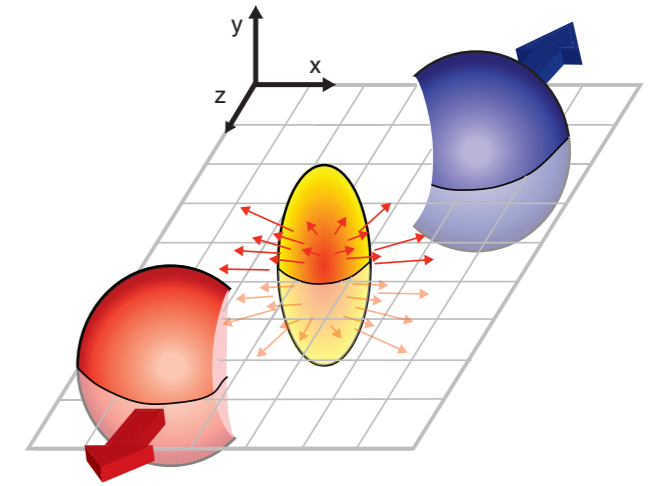
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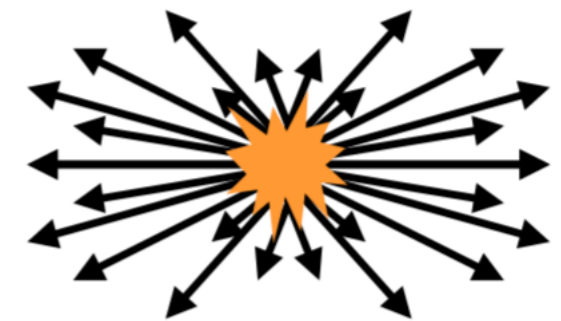


Credits: Mike Lisa

- QGP transforms initial spatial anisotropy to the anisotropy of final emitted particles

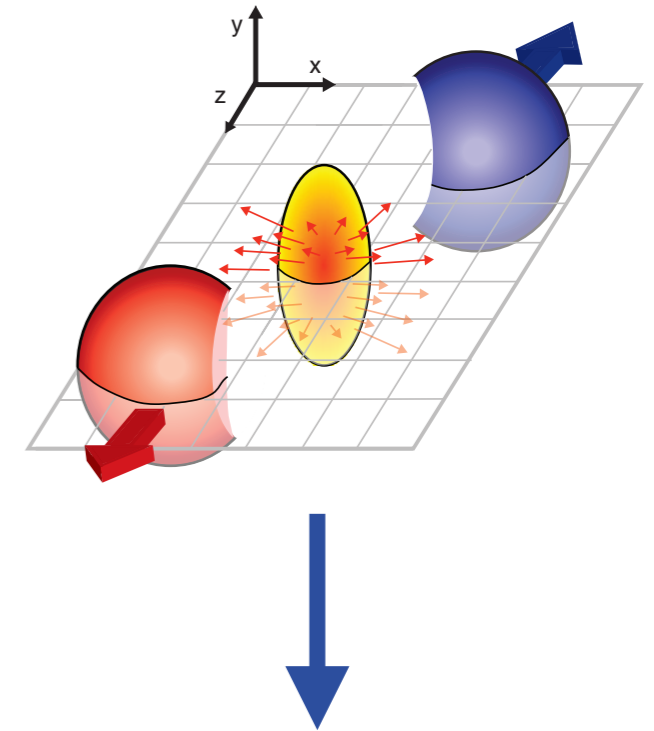


- The system expands collectively
 - Global collectivity

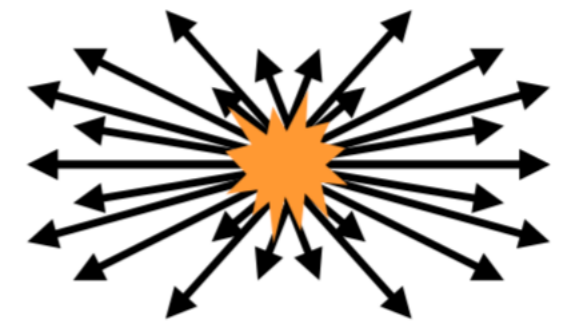


- Investigation of anisotropy of the distribution of emitted particles provides information about the evolution of HI collision

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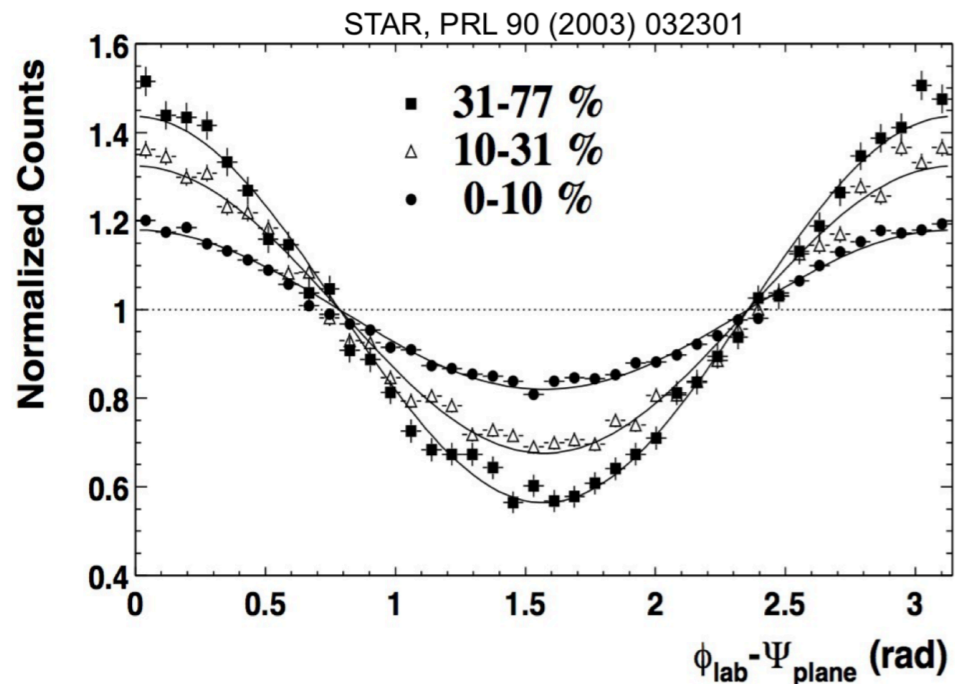


- Investigation of anisotropy of the distribution of emitted particles provides information about the evolution of HI collision -> HOW?

HOW TO QUANTIFY PARTICLE ANISOTROPY

- Distribution of emitted particles in azimuth expanded in Fourier series

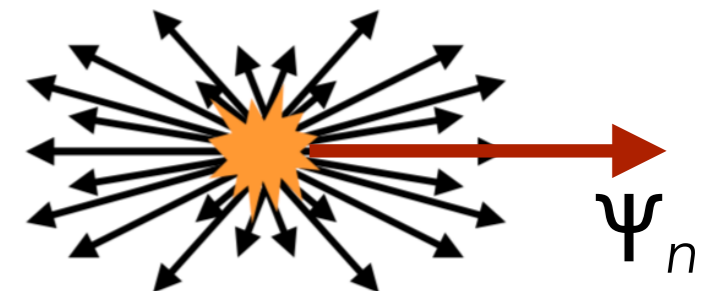
$$\frac{dN}{d\varphi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n \cos n(\varphi - \Psi_n)$$



flow coefficient:

$$v_n = \langle \cos n(\varphi - \Psi_n) \rangle$$

participant plane



HOW TO QUANTIFY PARTICLE ANISOTROPHY

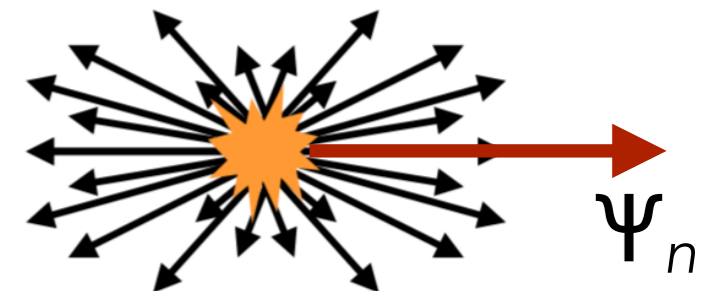
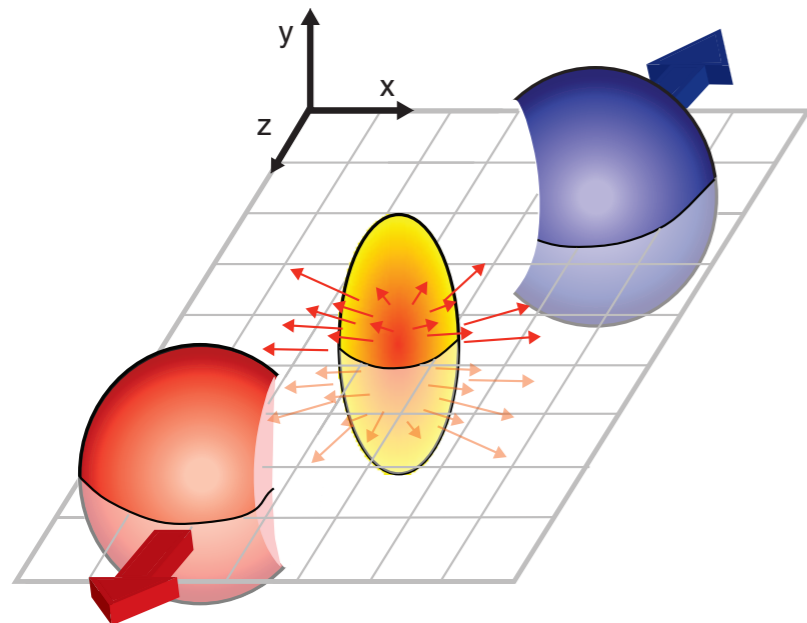
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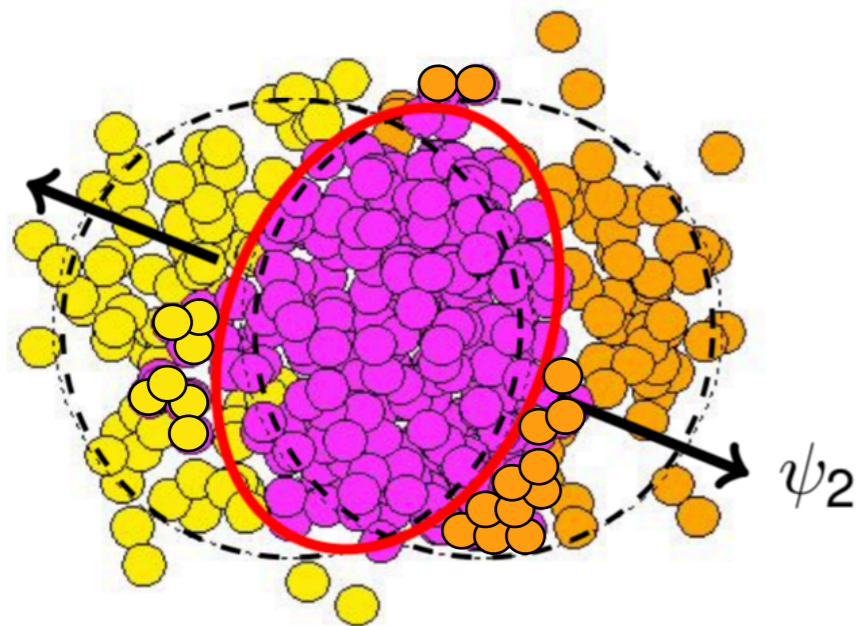
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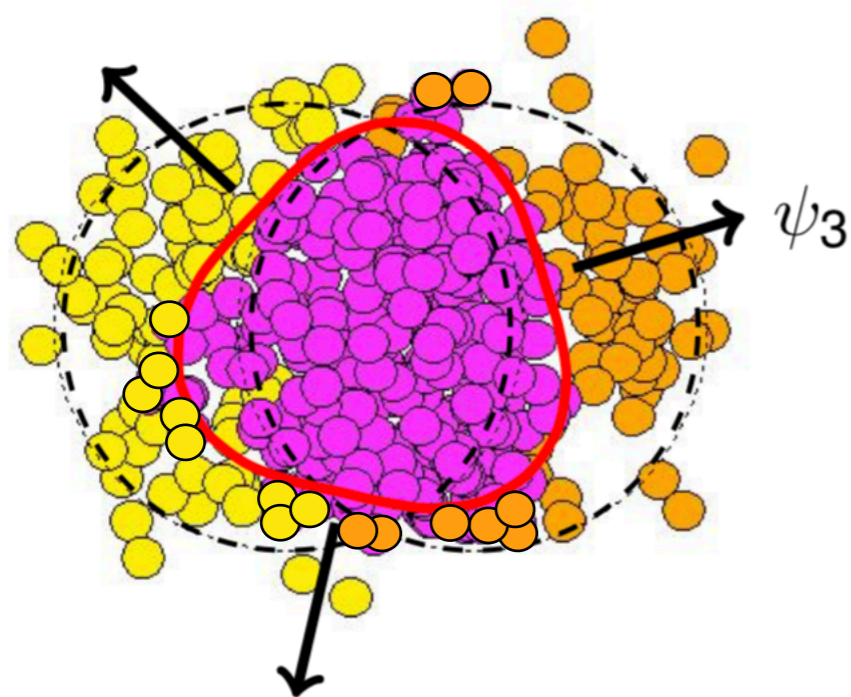
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Elliptic initial overlap geometry $\epsilon_2 \rightarrow$ Large elliptic flow v_2

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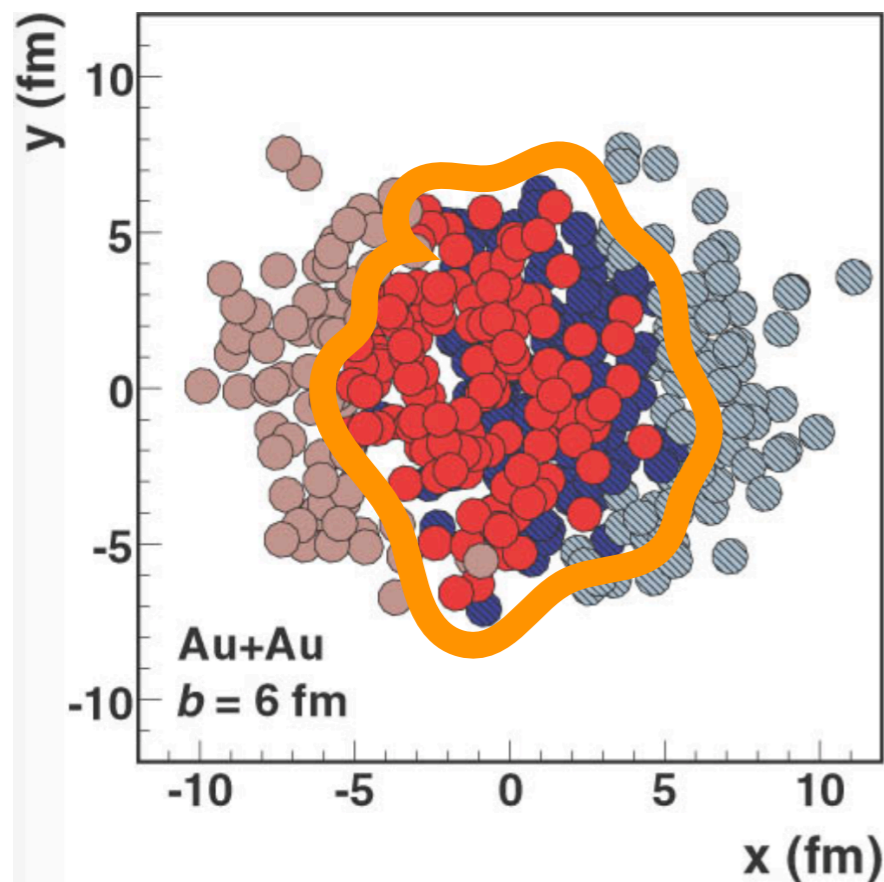
participant plane

Triangular initial overlap geometry $\epsilon_3 \rightarrow$ Large triangular flow v_3

HOW TO QUANTIFY PARTICLE ANISOTROPY

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flow coefficient:

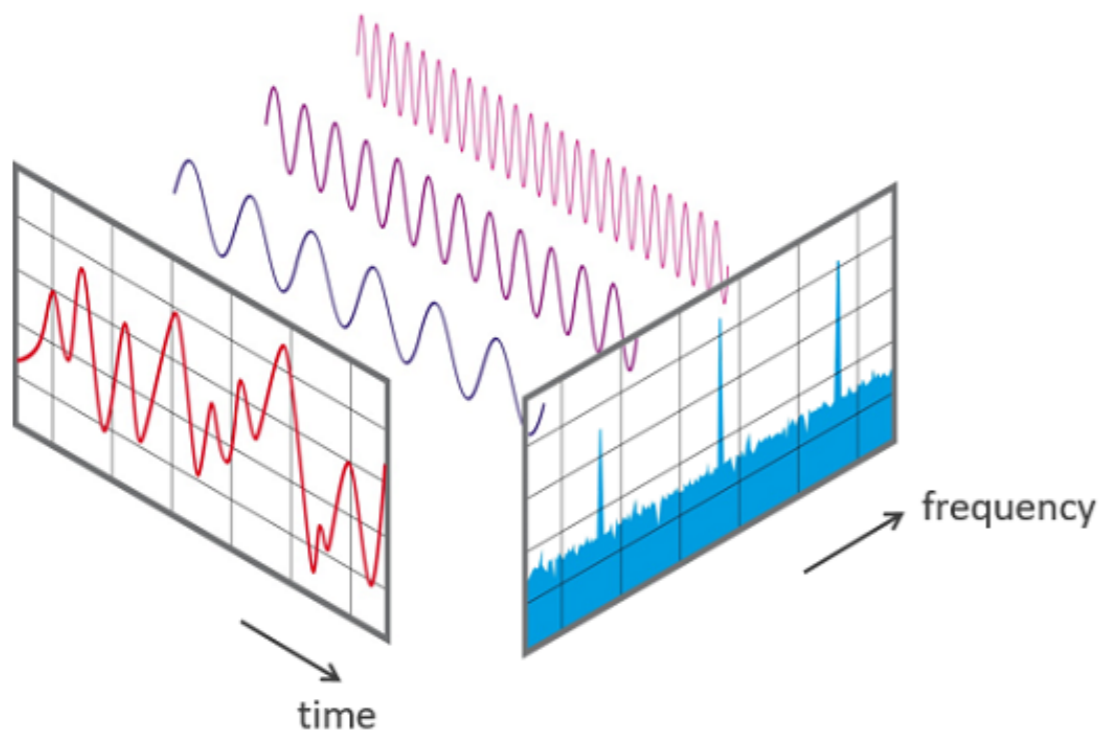
$$v_n = \langle \cos n(\varphi - \Psi_n) \rangle$$

participant plane

Real collision contains several harmonic modes \rightarrow superposition of v_2, v_3, v_4, \dots

ANALOGY TO FLOW COEFFICIENTS

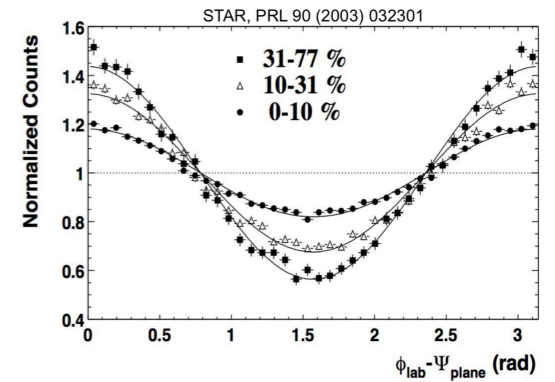
- Electronic signal contains several types of waves
 - Superposition of the basic harmonic modes



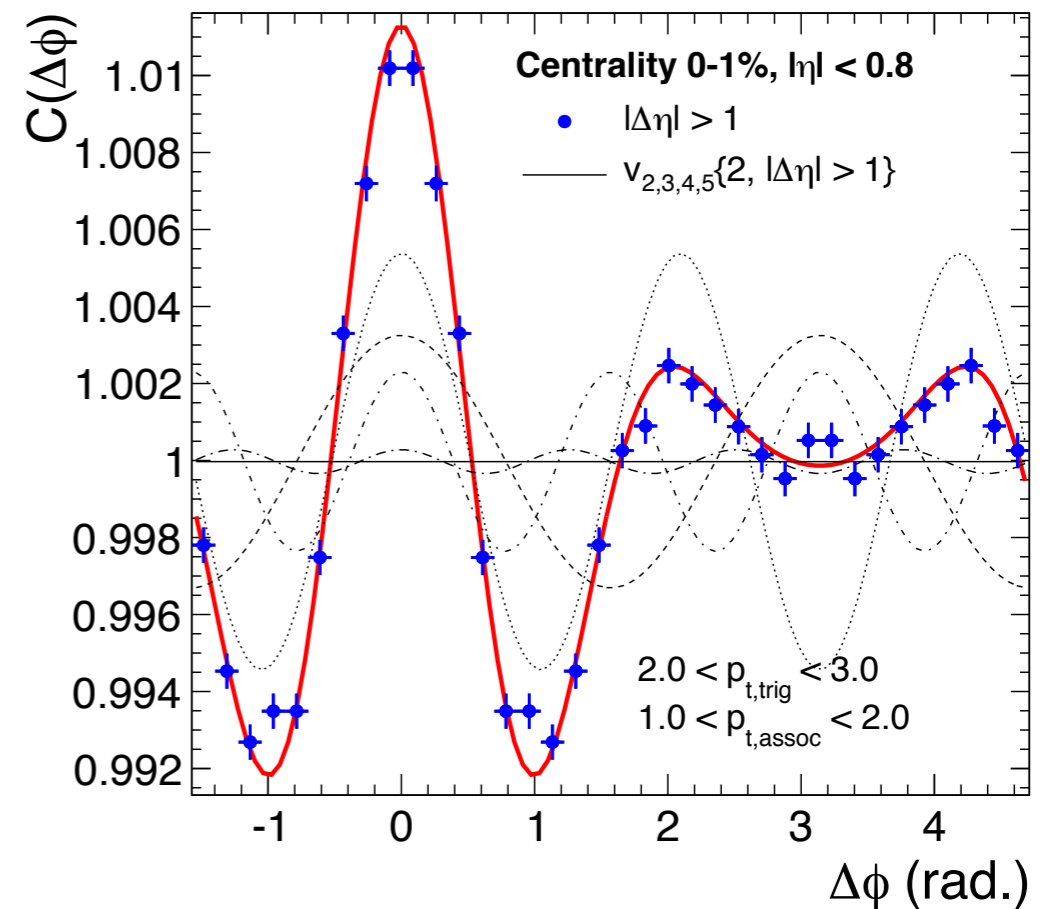
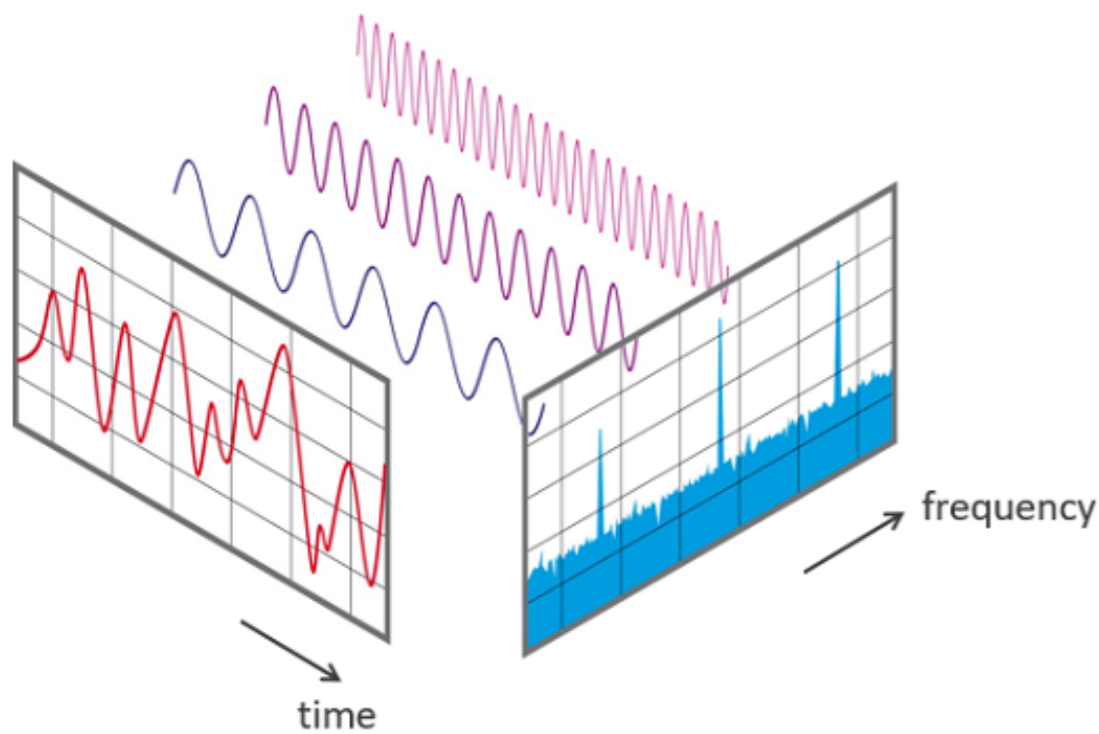
wikipedia, https://en.wikipedia.org/wiki/Fast_Fourier_transform#/media/File:FFT-Time-Frequency-View.png

ANALOGY TO FLOW COEFFICIENTS

- Electronic signal contains several types of waves
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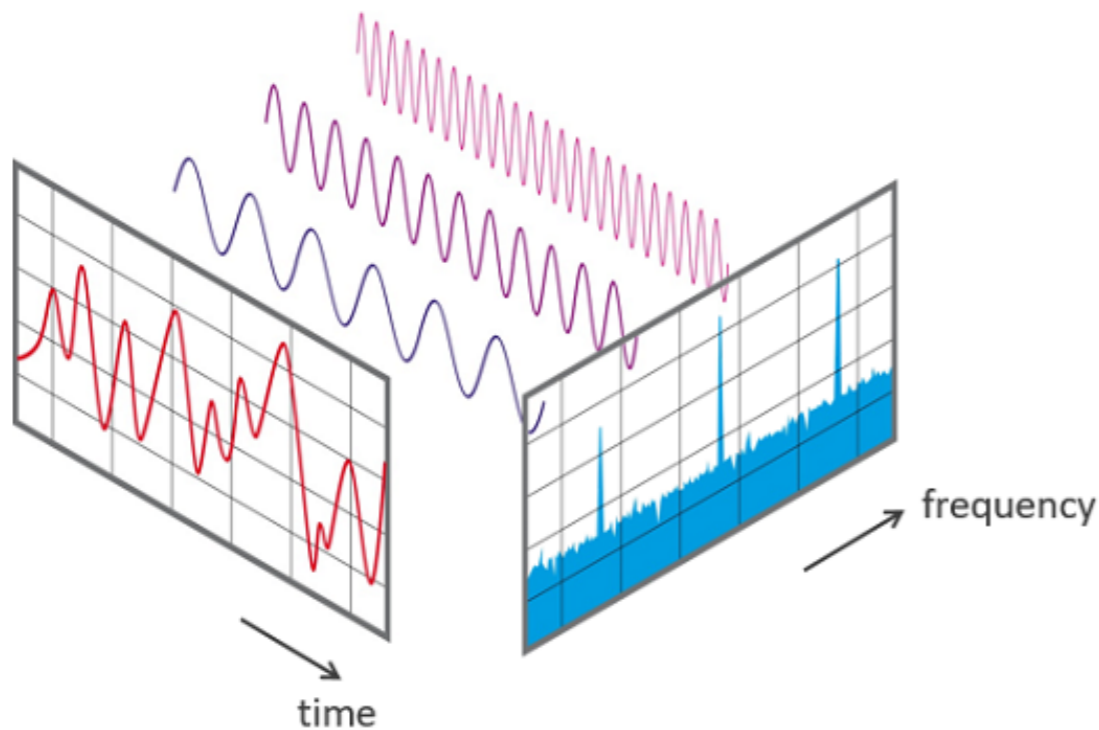
PRL 107, 032301 (2011)



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ANALOGY TO FLOW COEFFICIENTS

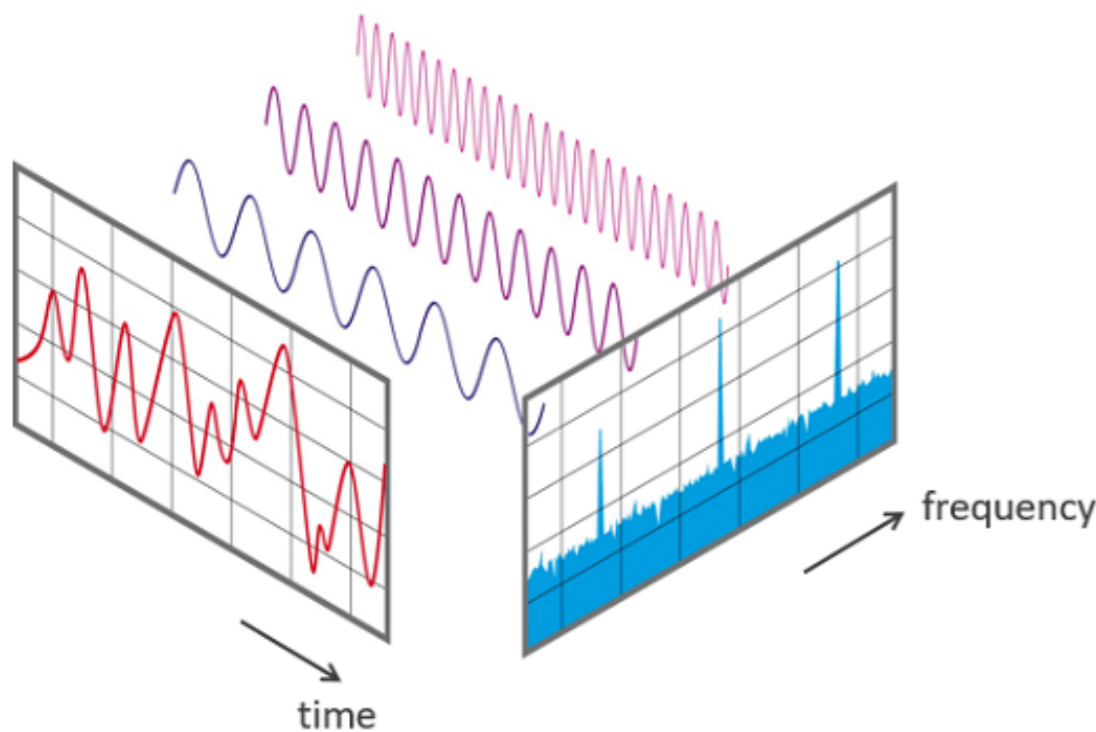
- Electronic signal contains several types of waves
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 - Fourier transform to frequency domain: amplitude shows the abundance of the basic harmonic modes within the signal



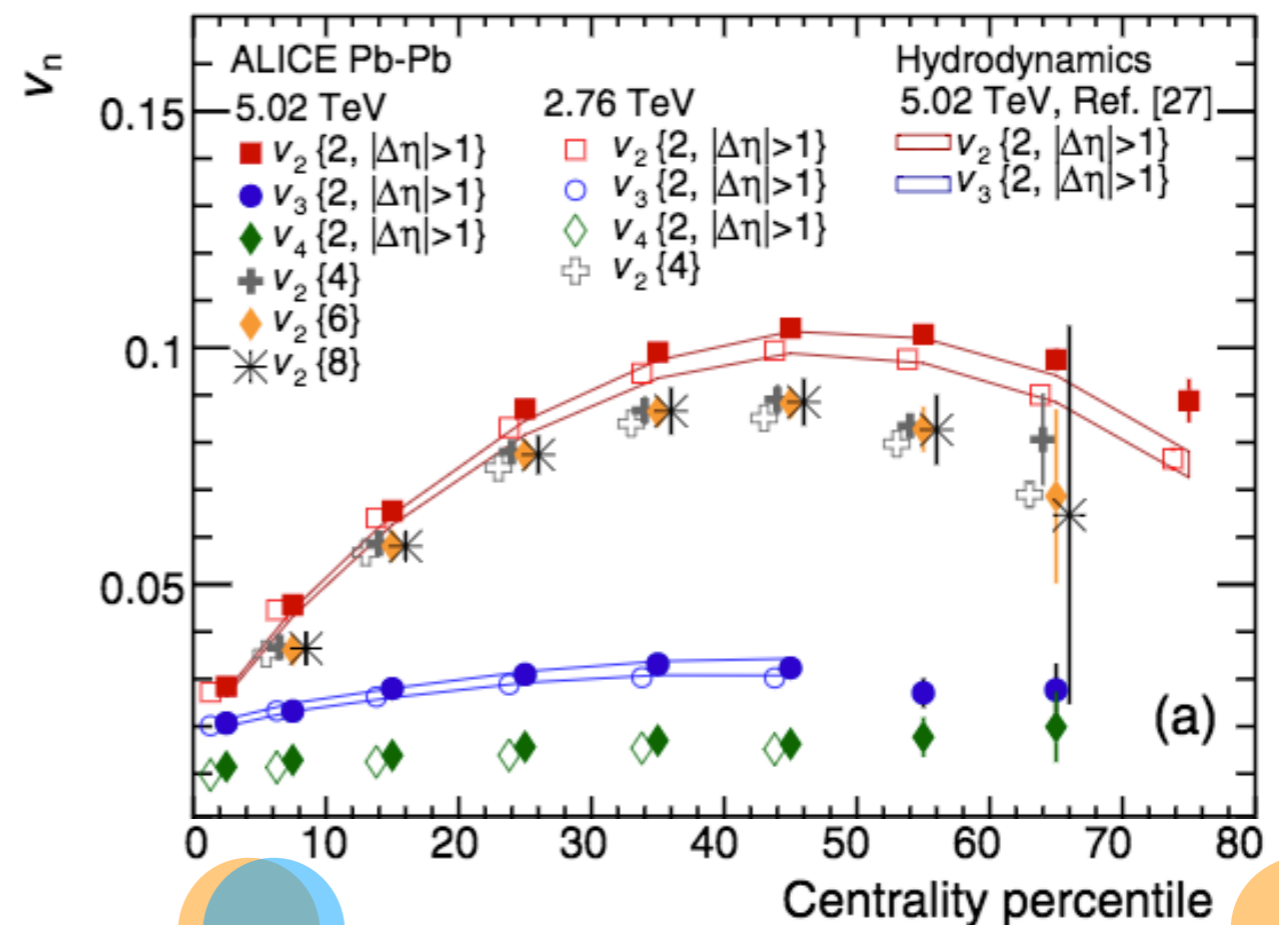
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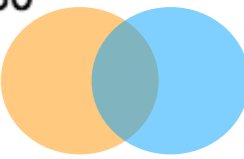
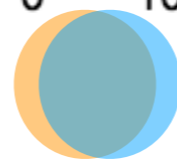
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PRL 116, 132302 (2016)



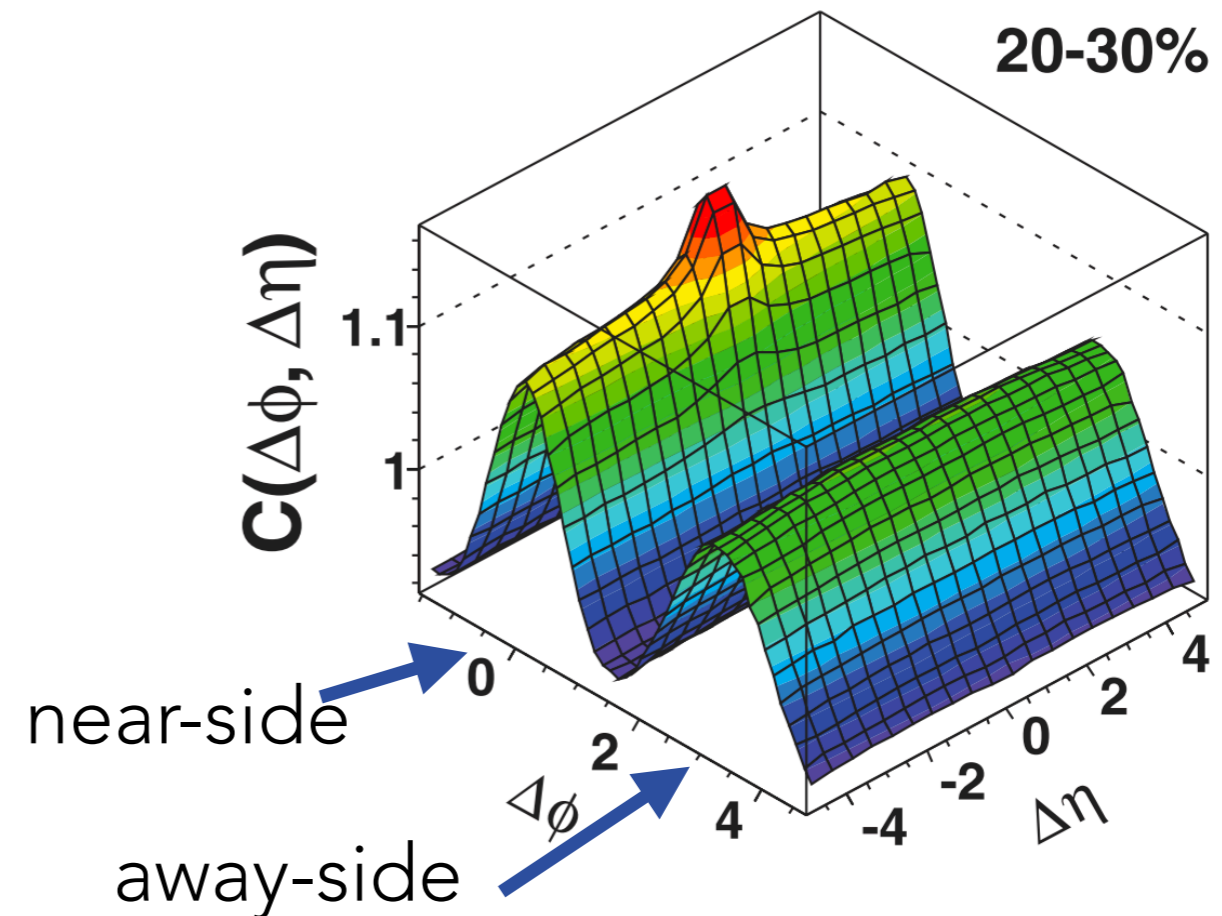
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HOW TO MEASURE FLOW

- Two-particle correlation function between particles with (φ_1, η_1) and (φ_2, η_2)

ATLAS, PRC 86, 014907 (2012)



$$\Delta\varphi = \varphi_1 - \varphi_2 \quad \Delta\eta = \eta_1 - \eta_2$$

short range $\Delta\eta \approx 0$

long range $\Delta\eta \gg 0$

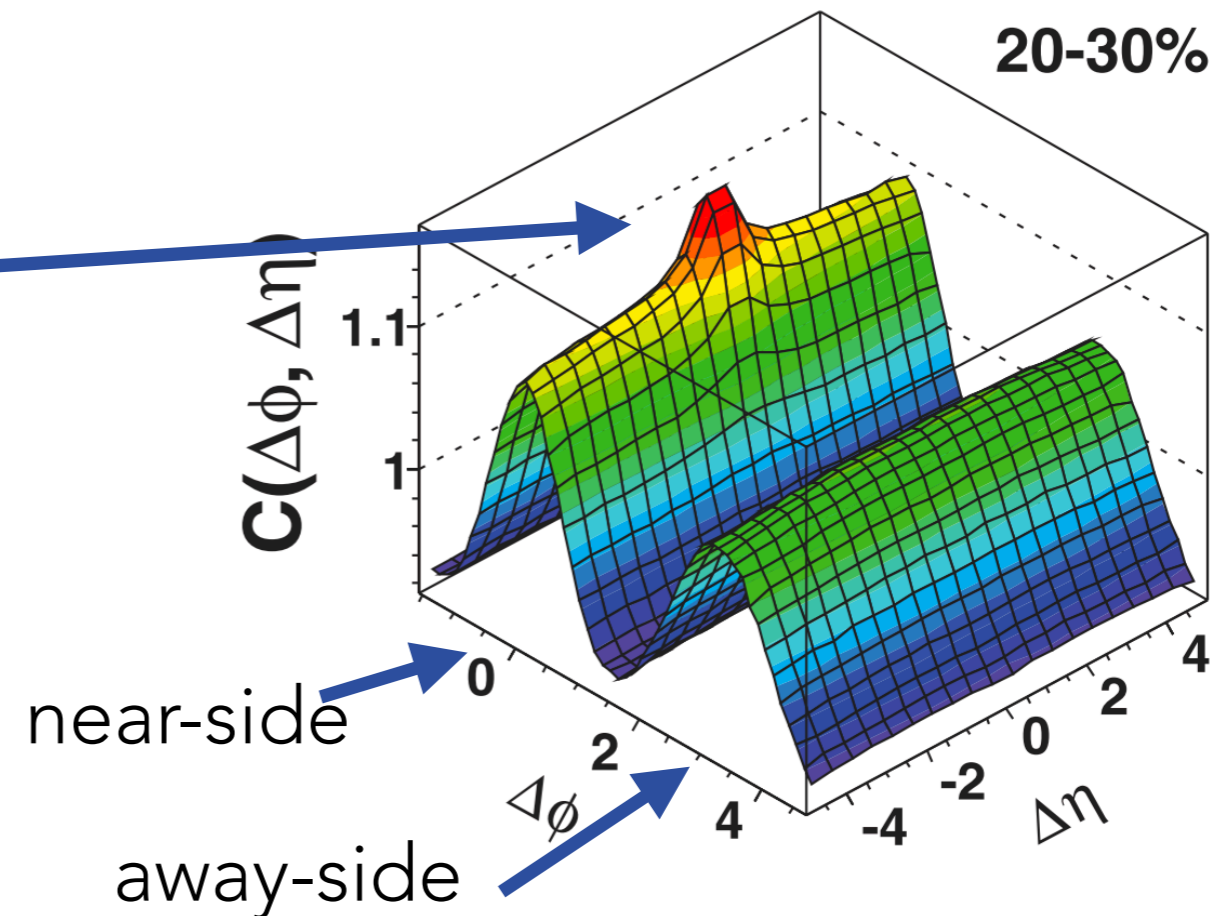
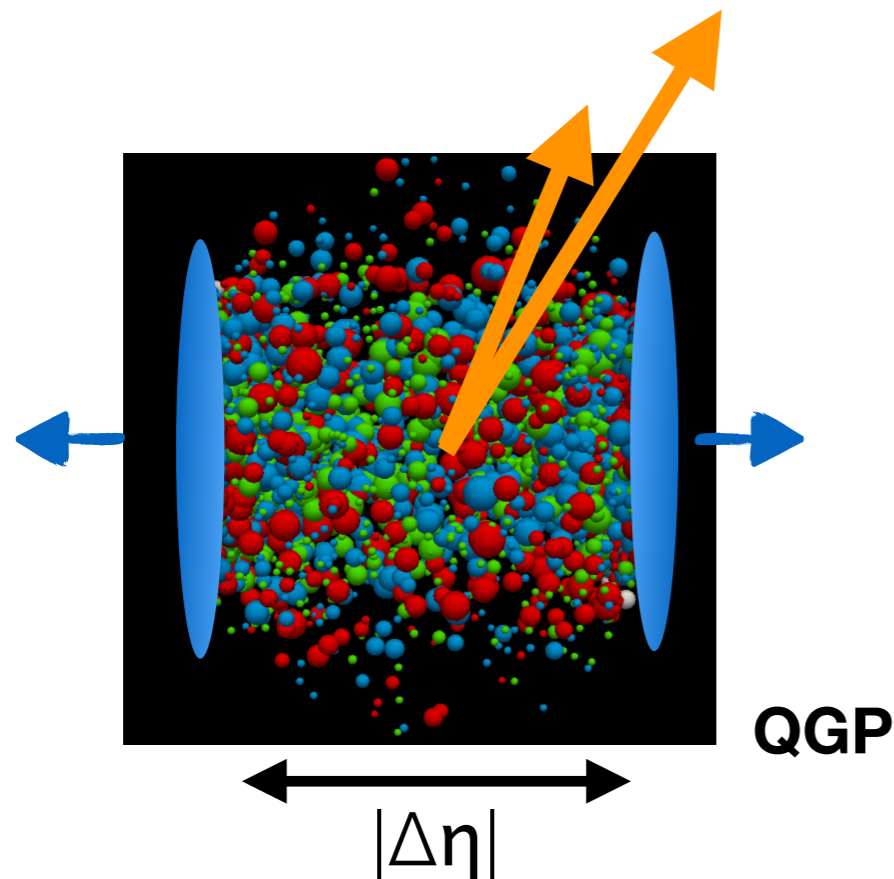
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- Jet peak: high- p_T resonances or jets

20-30%



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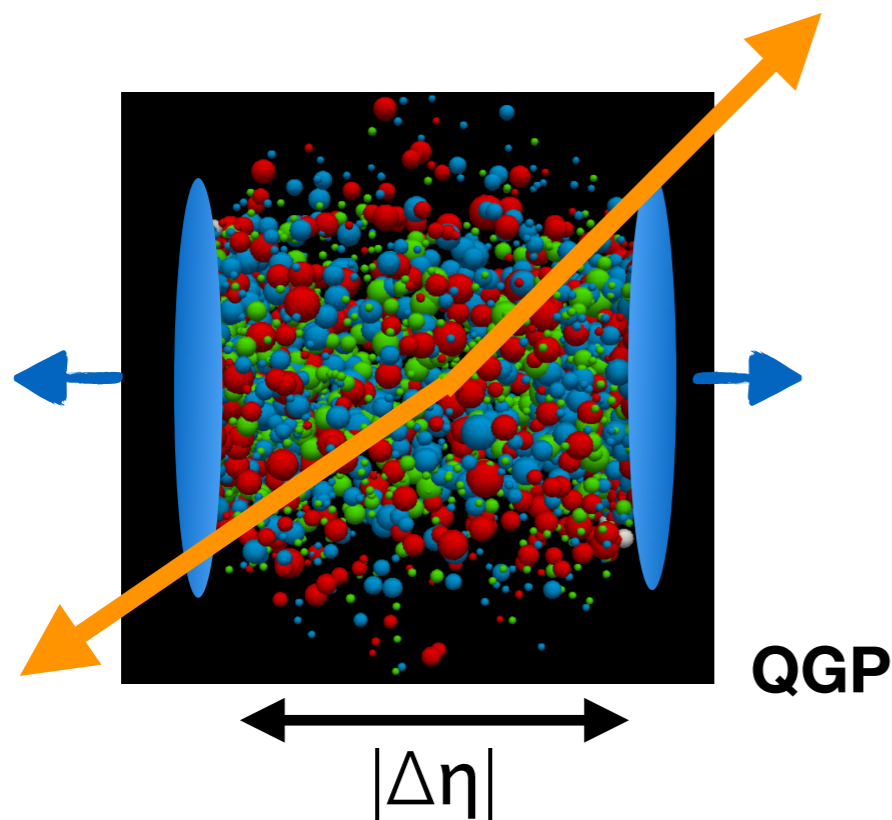
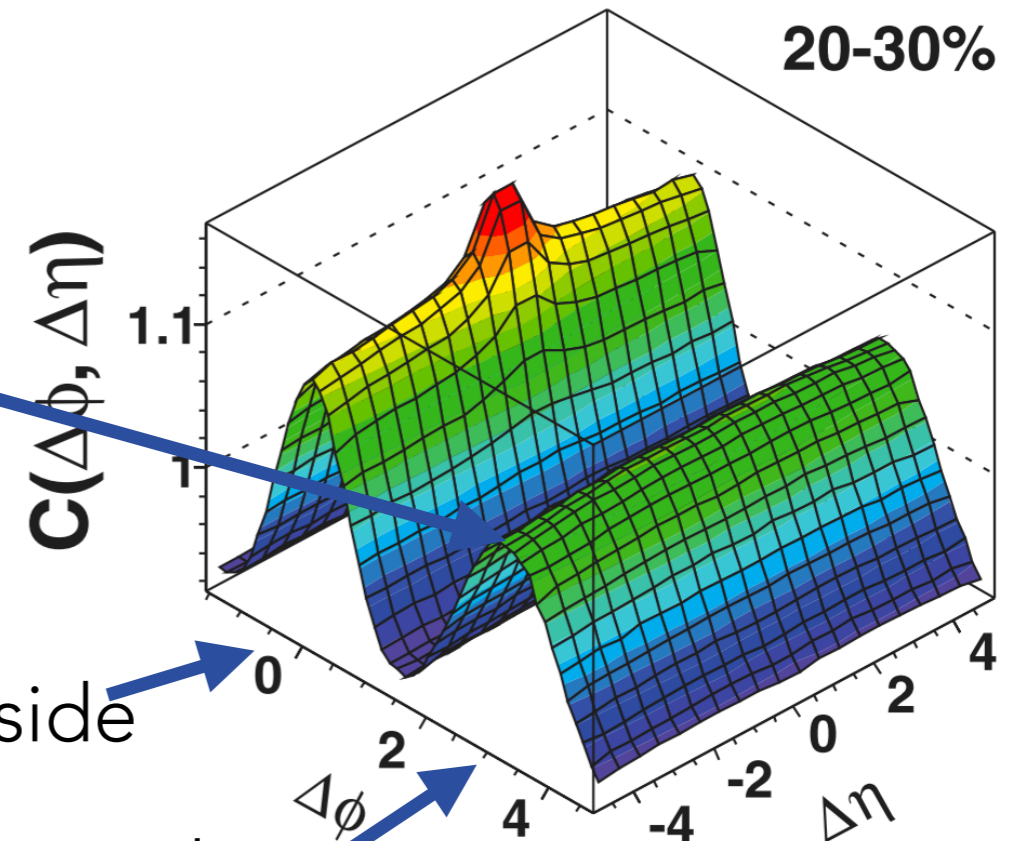
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- **Away-side ridge**: low p_T resonances or correlations between particles from the two cones of a jet

20-30%



near-side

away-side

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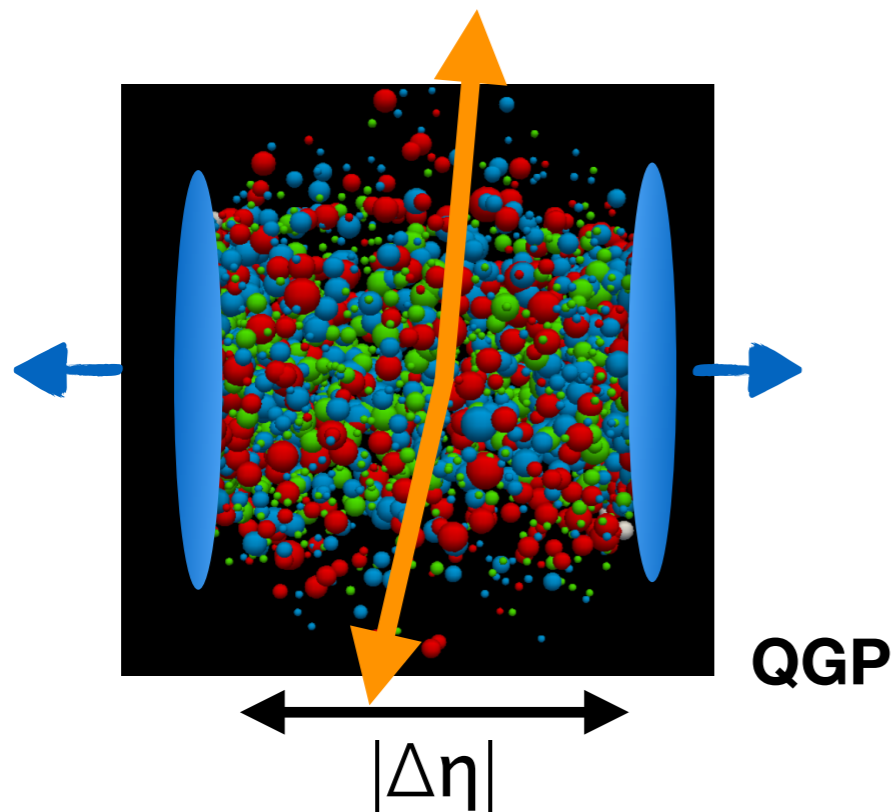
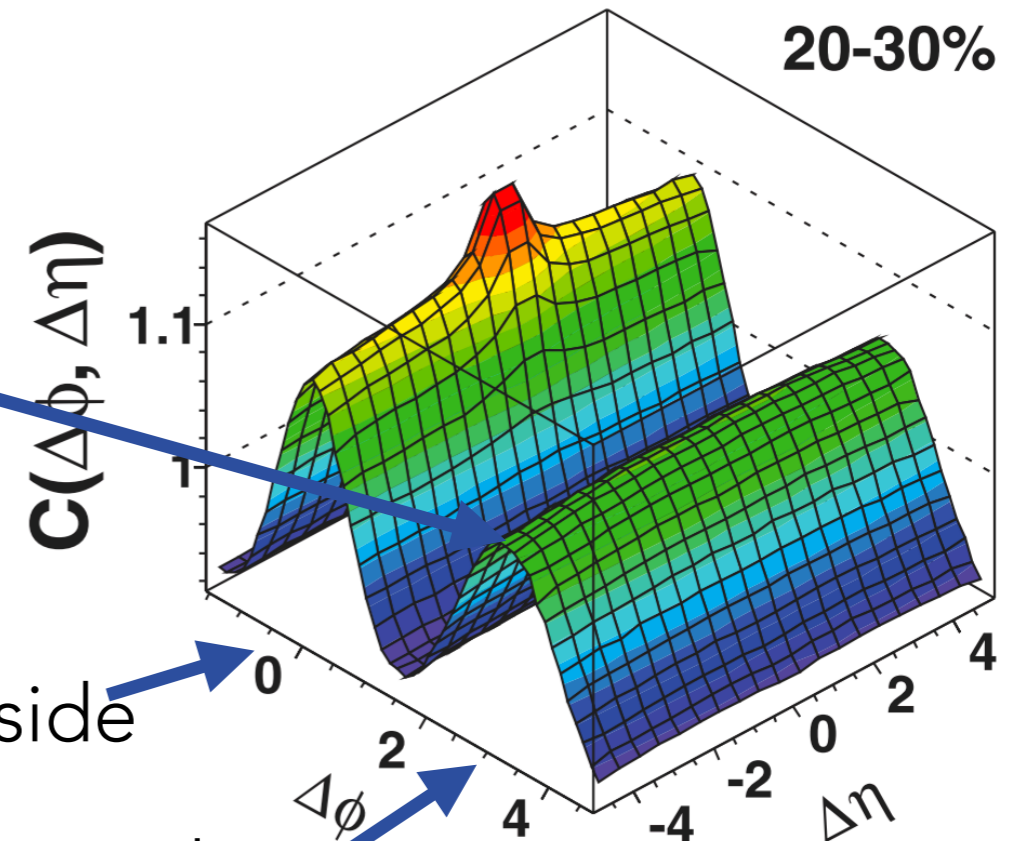
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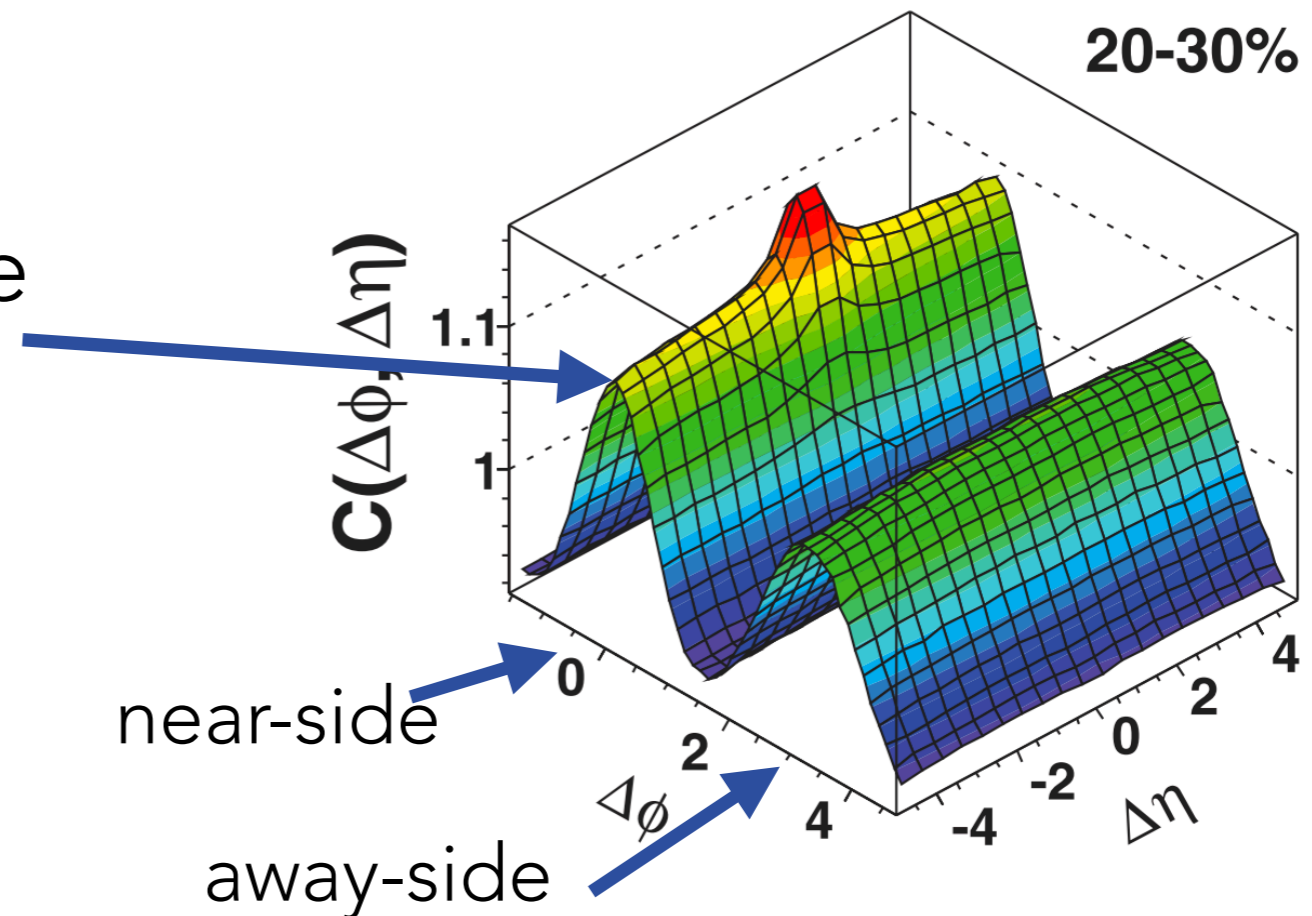
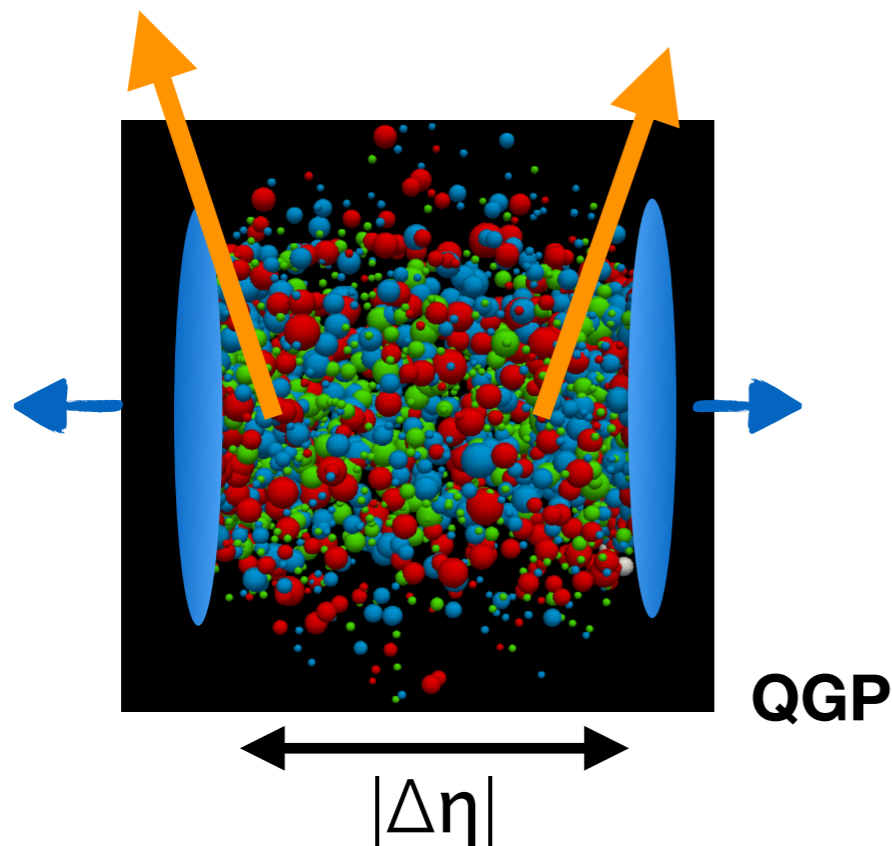
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ATLAS, PRC 86, 014907 (2012)

- Near-side ridge: collective expansion of the system

20-30%



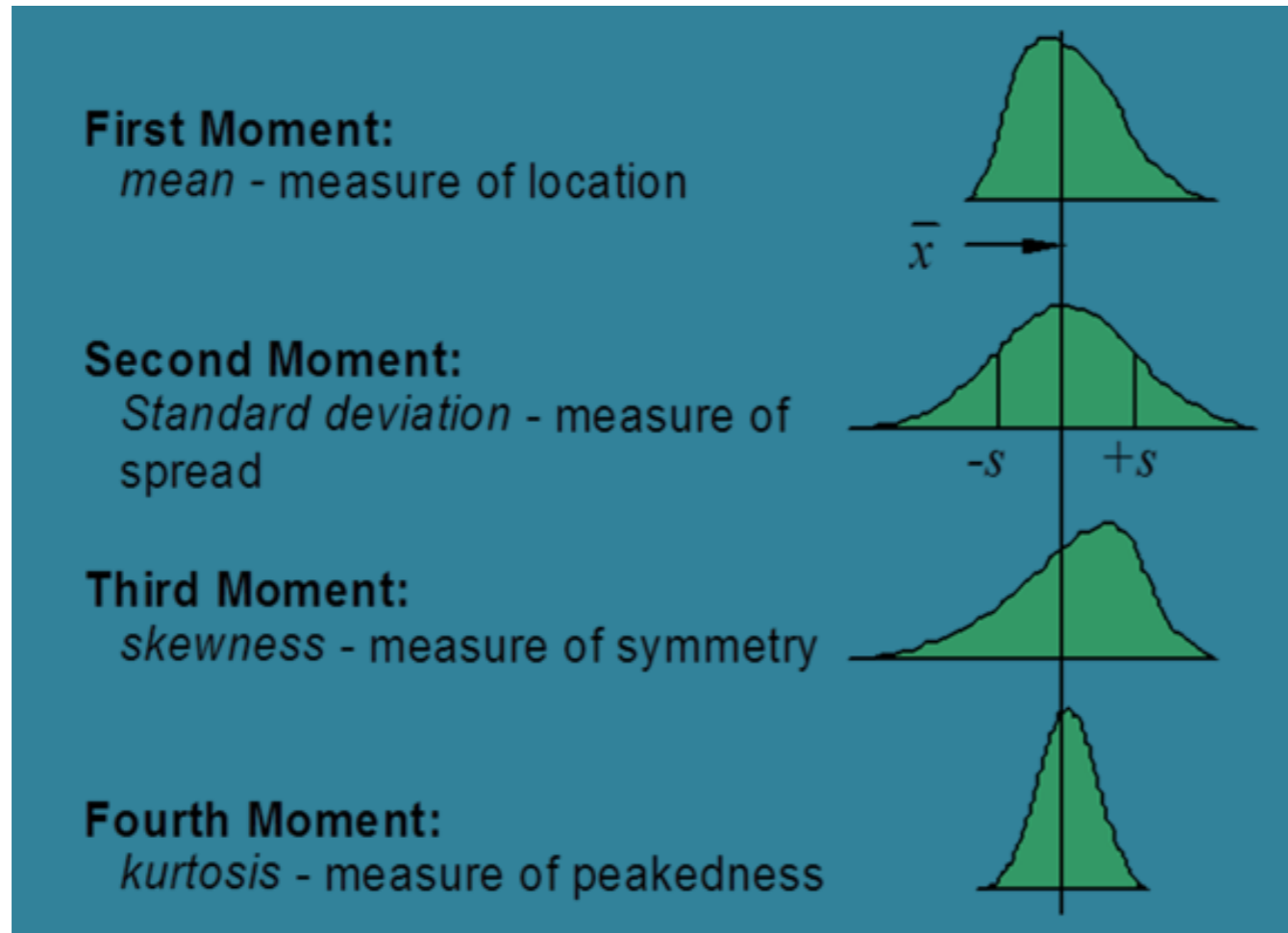
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HOW TO MEASURE FLOW

- *m*-particle cumulants



- Moments of a distribution:
- Cumulants are similar (derived from moments)

- We measure cumulants of the flow distribution

HOW TO MEASURE FLOW

How to get flow coefficients (using cumulants)

1. multi-particle correlations
2. multi-particle cumulants
3. flow coefficients

HOW TO MEASURE FLOW

How to get flow coefficients (using cumulants)

1. multi-particle correlations

$$\langle\langle 2 \rangle\rangle = \langle\langle \cos n(\varphi_1 - \varphi_2) \rangle\rangle = \langle v_n^2 \rangle$$

average over particles in an event

average over all events

HOW TO MEASURE FLOW

How to get flow coefficients (using cumulants)

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average over particles in an event

average over all events

$$\langle\langle 4 \rangle\rangle = \langle\langle \cos n(\varphi_1 + \varphi_2 - \varphi_3 - \varphi_4) \rangle\rangle = \langle v_n^4 \rangle$$

- 4-particle correlation contains contribution from:

$$\langle\langle \cos n(\varphi_1 - \varphi_3) \rangle\rangle \langle\langle \cos n(\varphi_2 - \varphi_4) \rangle\rangle = \langle\langle 2 \rangle\rangle^2$$

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HOW TO MEASURE FLOW

How to get flow coefficients (using cumulants)

1. multi-particle correlations
2. multi-particle cumulants

$$c_n\{2\} = \langle\langle 2 \rangle\rangle$$

$$c_n\{4\} = \langle\langle 4 \rangle\rangle - 2 \cdot \langle\langle 2 \rangle\rangle^2$$

 **genuine** 4-particle correlation

HOW TO MEASURE FLOW

How to get flow coefficients (using cumulants)

1. multi-particle correlations
2. multi-particle cumulants
3. flow coefficients

$$\sqrt{c_n\{2\}} = \sqrt{\langle\langle 2 \rangle\rangle} \approx v_n \rightarrow \boxed{v_n\{2\}}$$

$$\langle\langle 2 \rangle\rangle = \langle\langle \cos n(\varphi_1 - \varphi_2) \rangle\rangle = \langle v_n^2 \rangle$$

Equality is in ideal case of a delta function of v_n

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How to get flow coefficients (using cumulants)

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2. multi-particle cumulants
3. flow coefficients

$$\sqrt{c_n\{2\}} = \sqrt{\langle\langle 2 \rangle\rangle} \approx v_n \rightarrow \boxed{v_n\{2\}}$$

$$\begin{aligned} \sqrt[4]{-c_n\{4\}} &= \sqrt[4]{-\langle\langle 4 \rangle\rangle + 2 \cdot \langle\langle 2 \rangle\rangle^2} \\ &= \sqrt[4]{-v_n^4 + 2 \cdot v_n^2} \approx v_n \rightarrow \boxed{v_n\{4\}} \end{aligned}$$

Equality is in ideal case of a delta function of v_n

HOW TO MEASURE FLOW

How to get flow coefficients (using cumulants)

1. multi-particle correlations
2. multi-particle cumulants
3. flow coefficients

$$v_n\{2\} = \sqrt{c_n\{2\}}$$

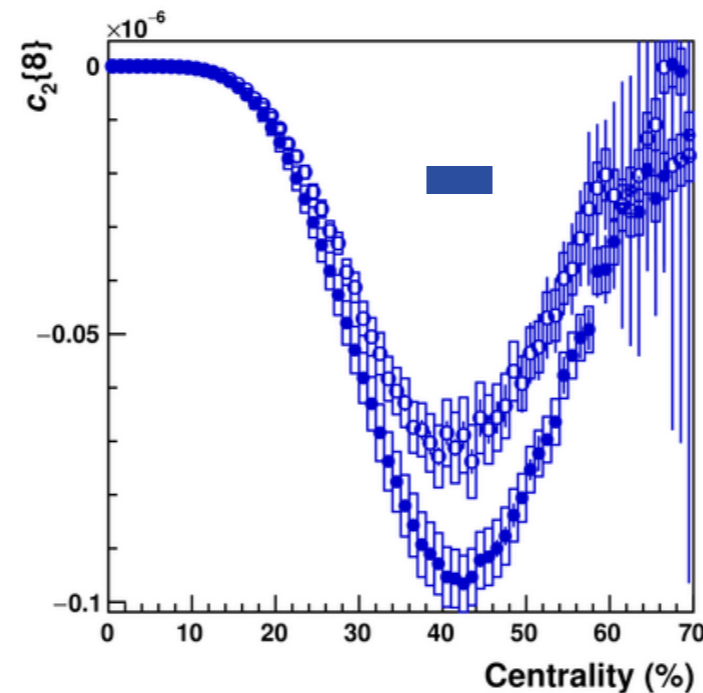
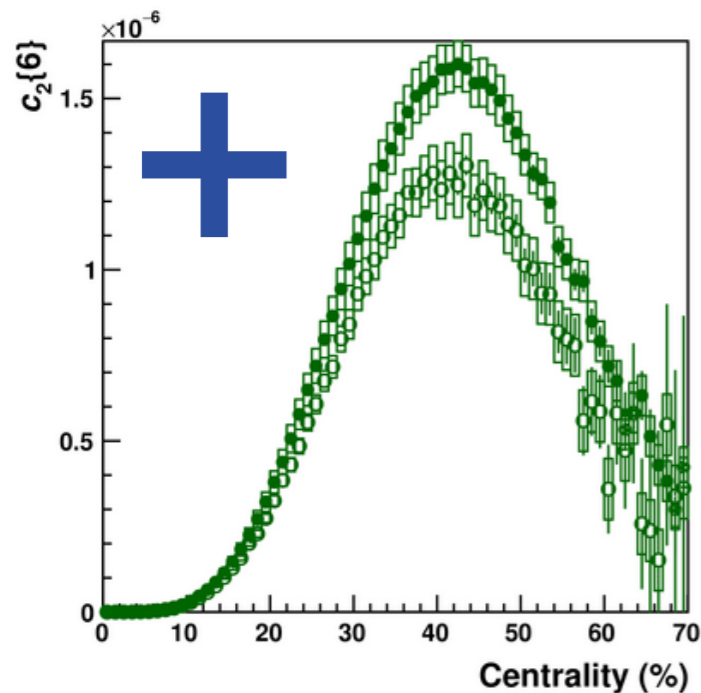
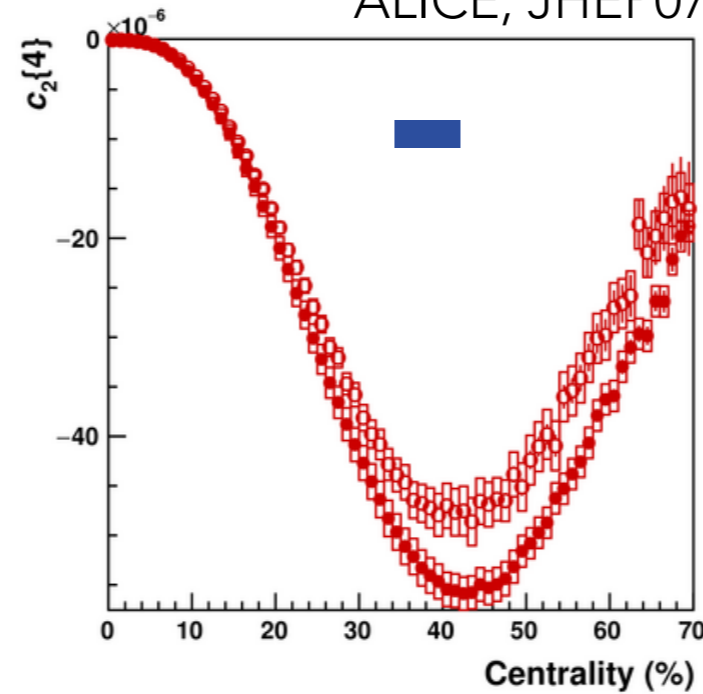
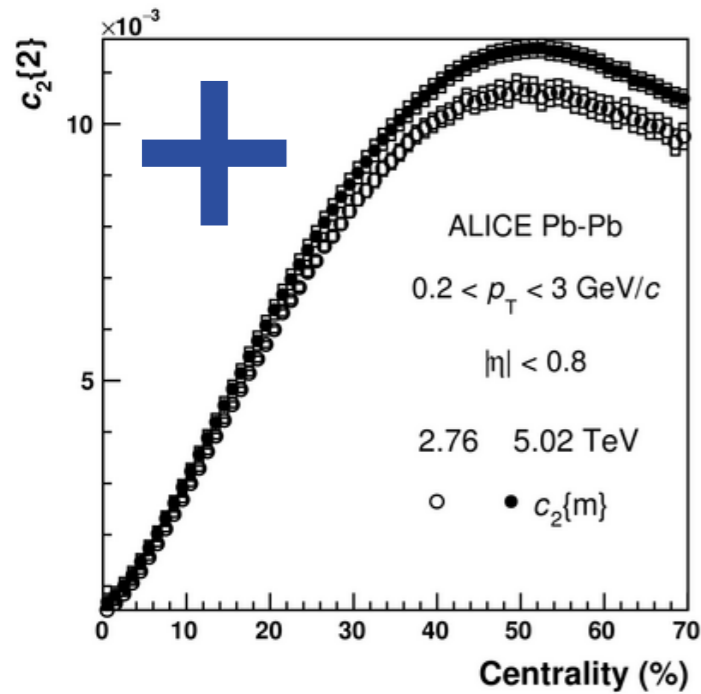
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$$v_n\{6\} = \sqrt[6]{1/4 \cdot c_n\{6\}}$$

$$v_n\{8\} = \sqrt[8]{-1/33 \cdot c_n\{8\}}$$

MEASUREMENTS OF FLOW USING M-PARTICLE CUMULANTS

ALICE, JHEP07 (2018) 103



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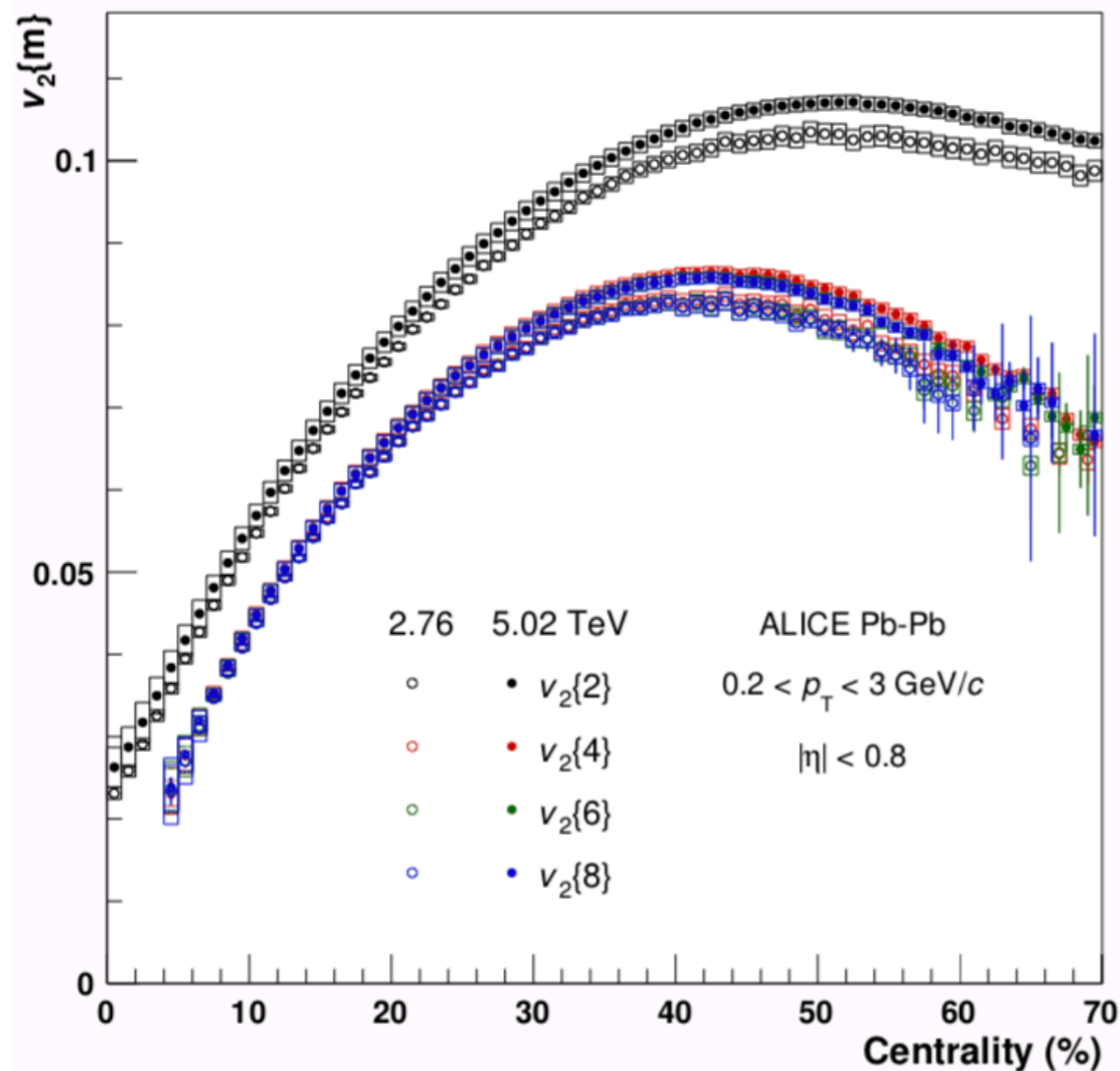
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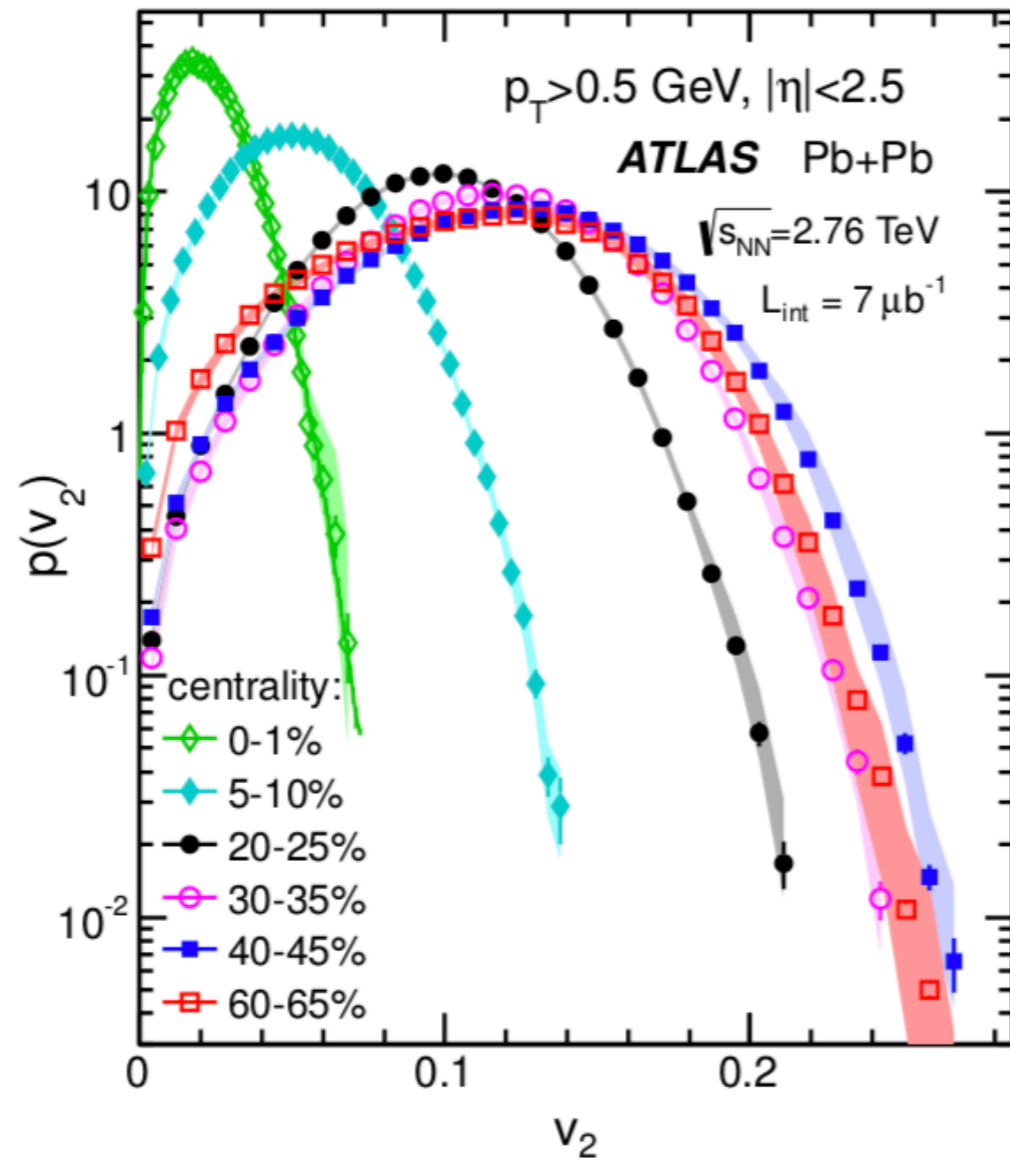
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ATLAS, JHEP11 (2013) 183



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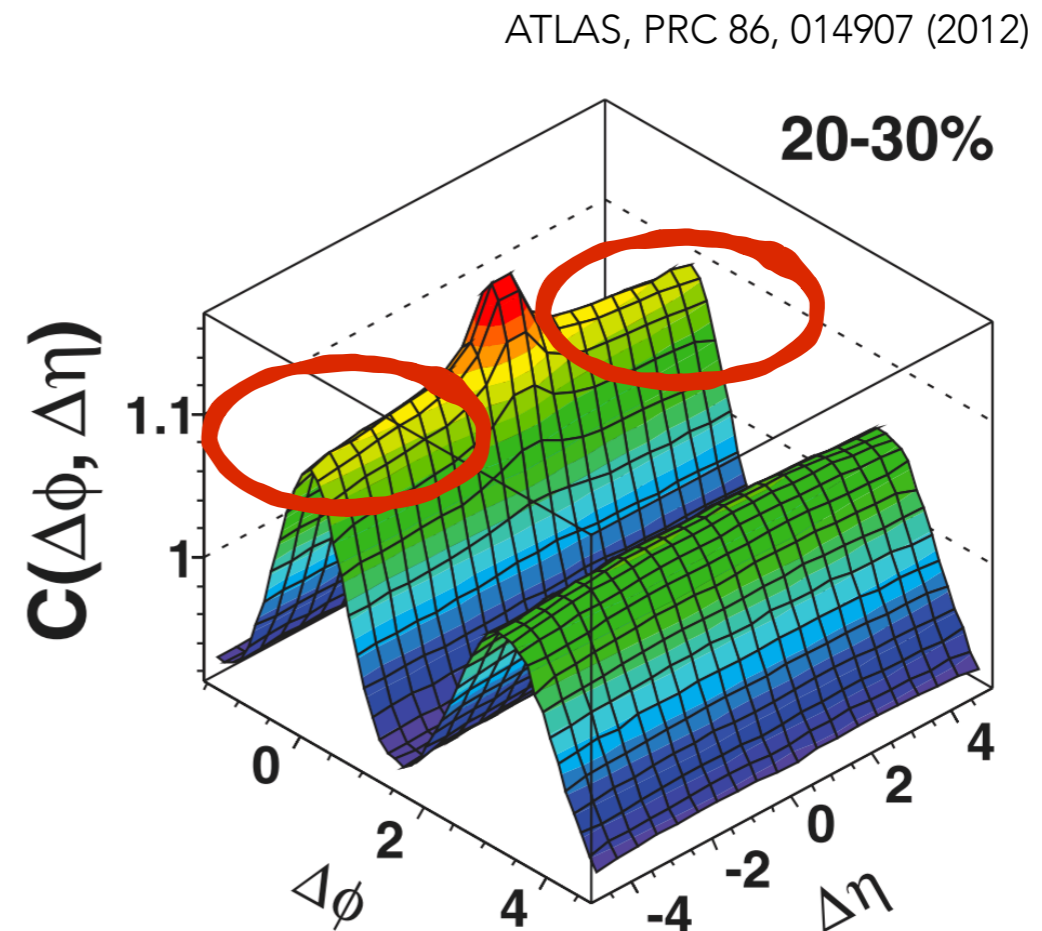
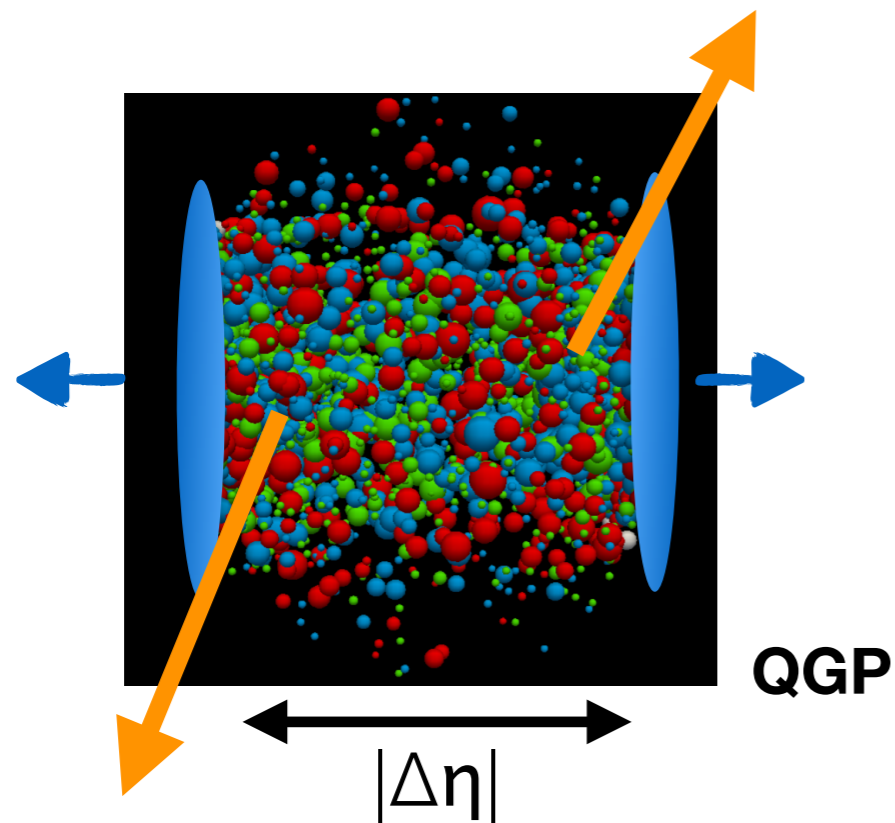
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“DEFINITION” OF COLLECTIVITY

- Based on a collective system (heavy-ion collisions) we define:
- **Collectivity** = long-range multi-particle correlations

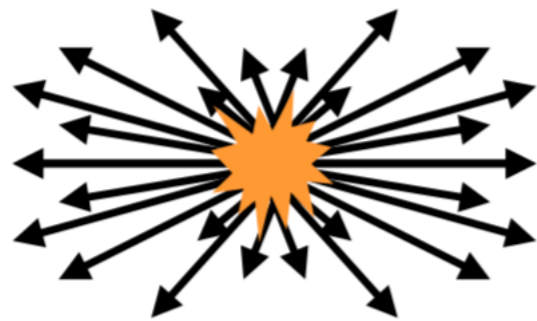
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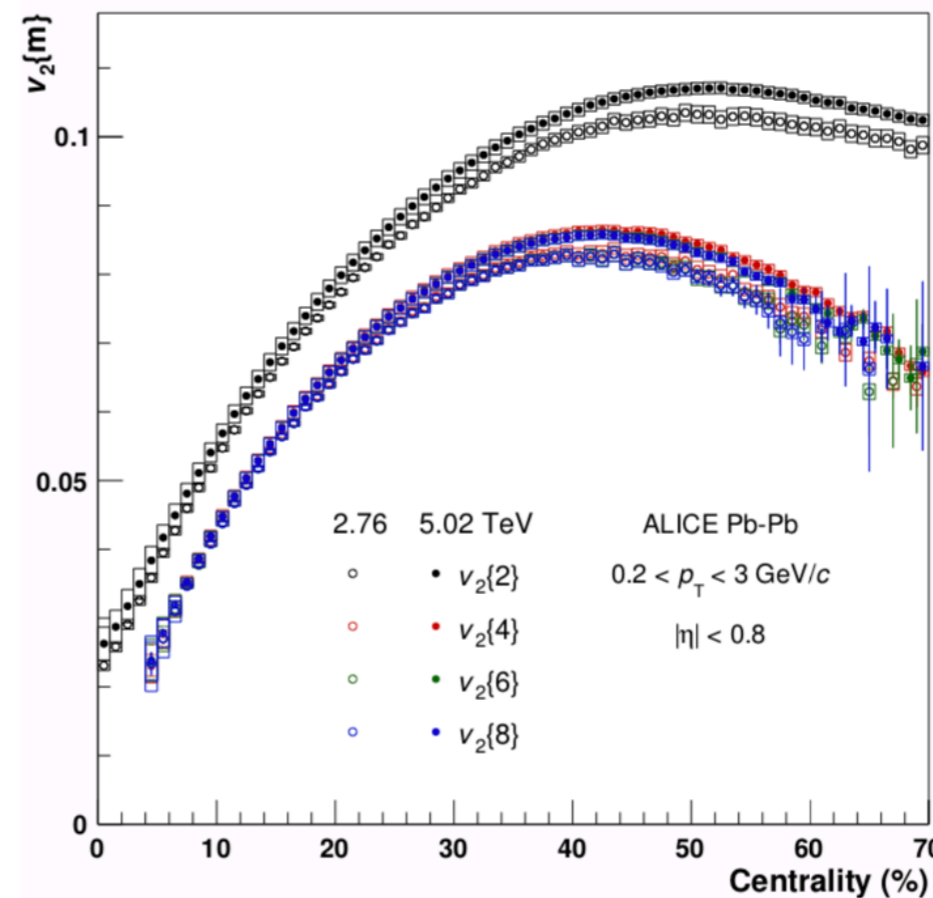
"DEFINITION" OF COLLECTIVITY

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All particles originate from a common source

ALICE, JHEP07 (2018) 103

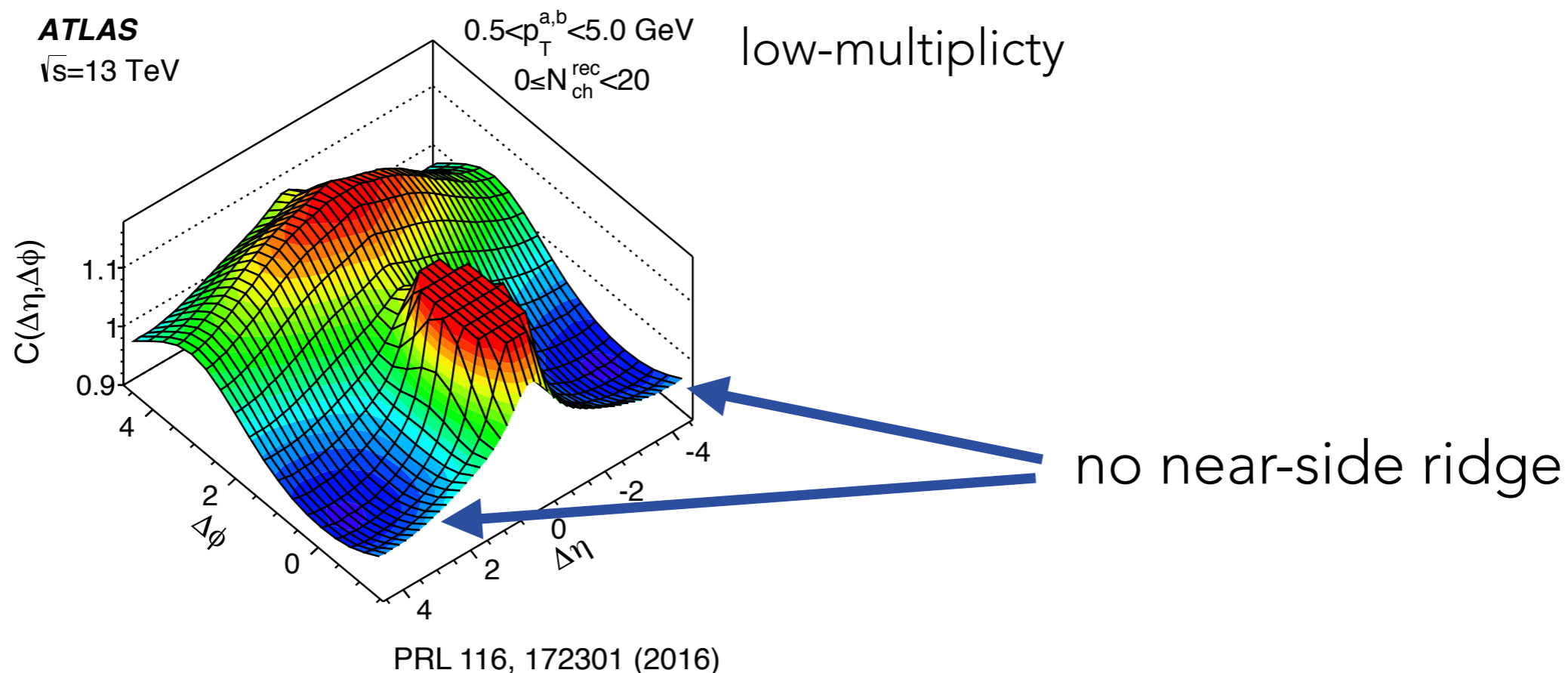


"correct"
sign
of
cumulants

$$v_n\{4\} \approx v_n\{6\} \approx v_n\{8\}$$

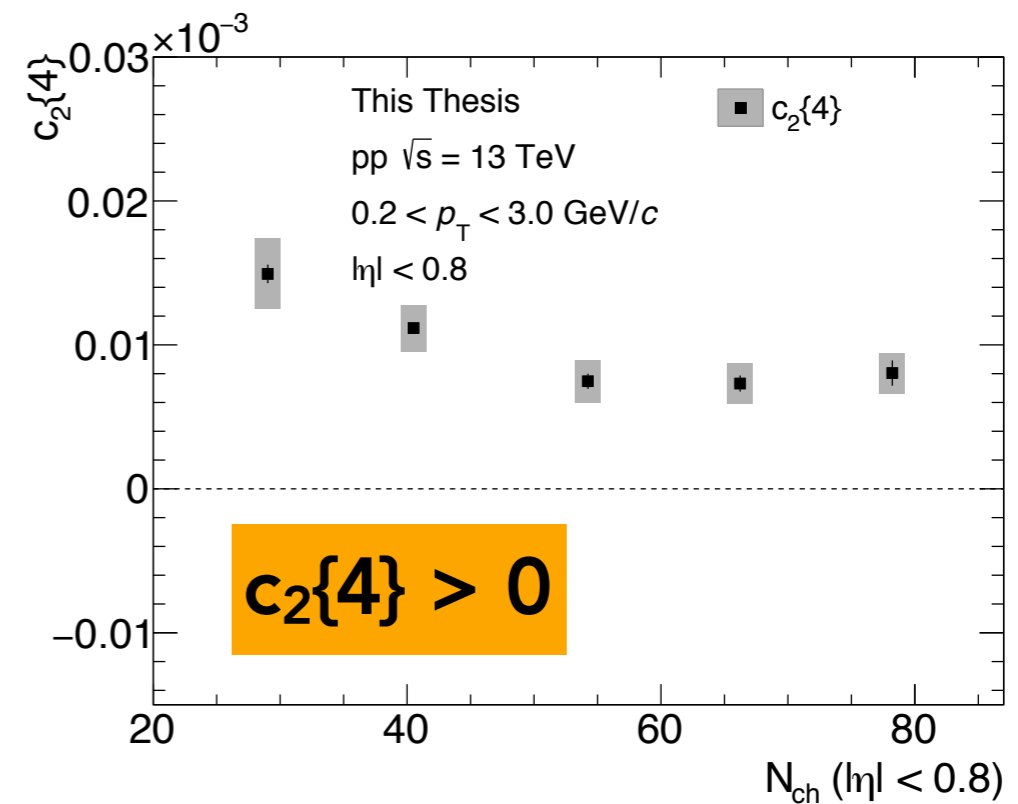
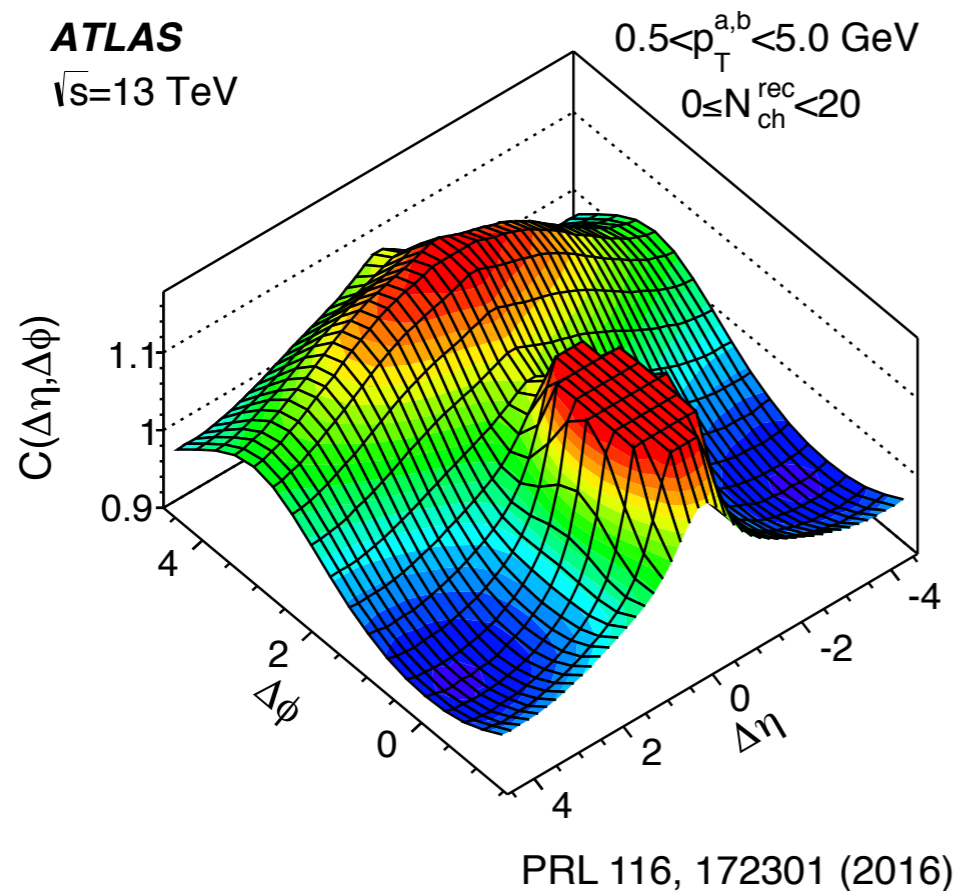
SMALL COLLISION SYSTEMS

- Original understanding:
 - No QGP is formed in small systems
 - pp collisions: reference for measurements from HI collisions
 - p-Pb collisions: Cold Nuclear Matter effects



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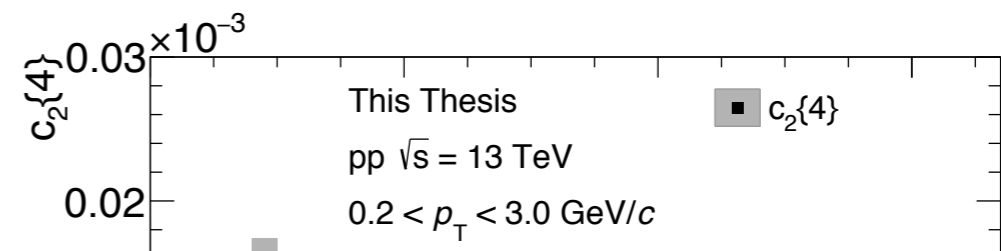


SMALL COLLISION SYSTEMS

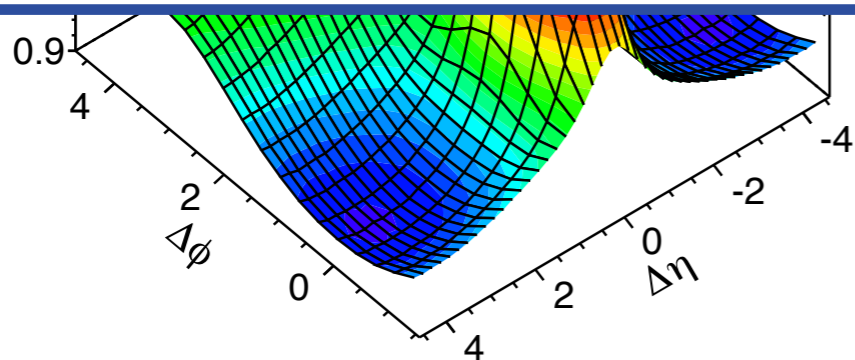
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ATLAS
 $\sqrt{s}=13$ TeV

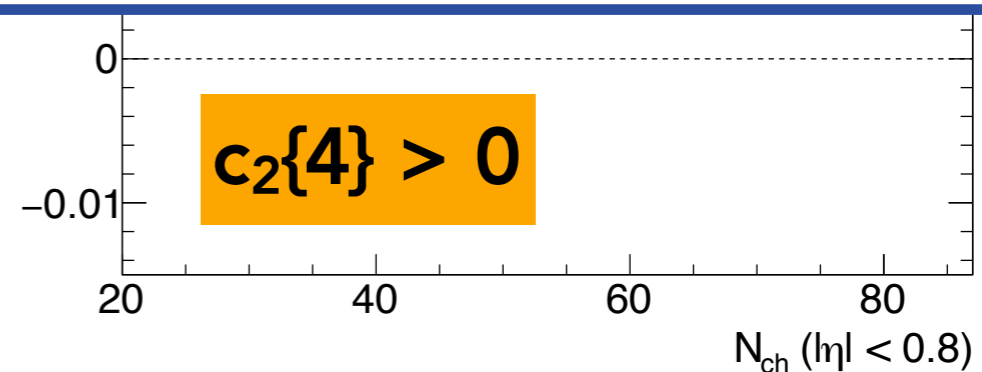
$0.5 < p_T^{a,b} < 5.0$ GeV
 $0 \leq N_{ch}^{rec} < 20$



correlations NOT long-range, NOR multi-particle



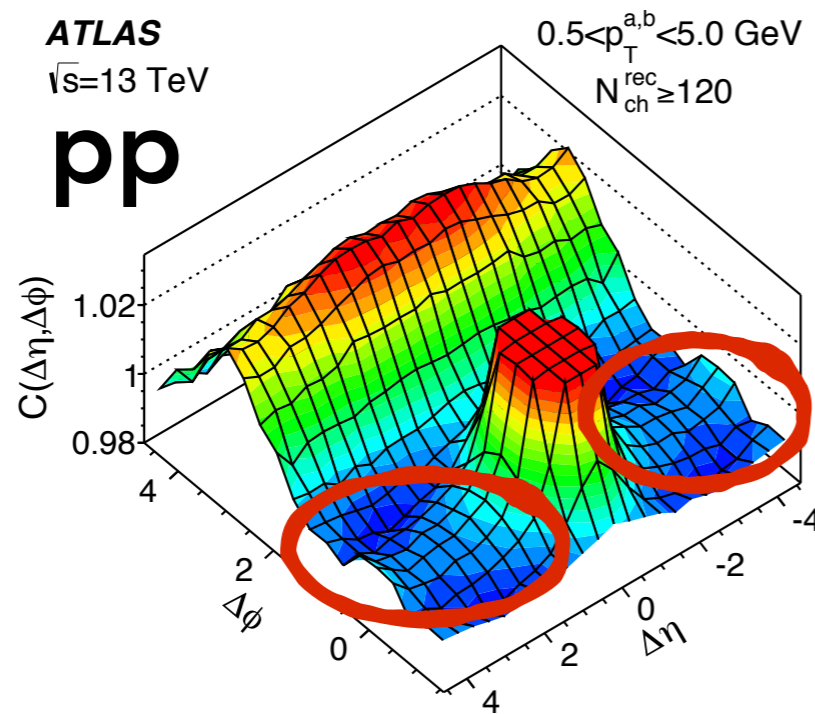
PRL 116, 172301 (2016)



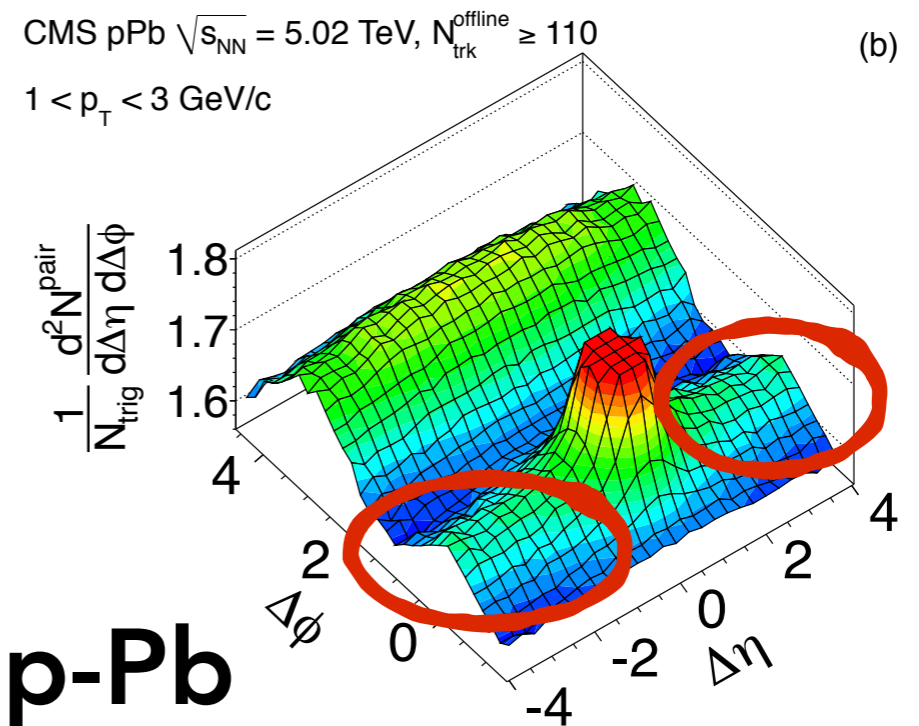
SMALL COLLISION SYSTEMS

- **Surprise:**
 - near-side ridge is observed at high-multiplicity pp and p-Pb collisions

high-multiplicity collisions



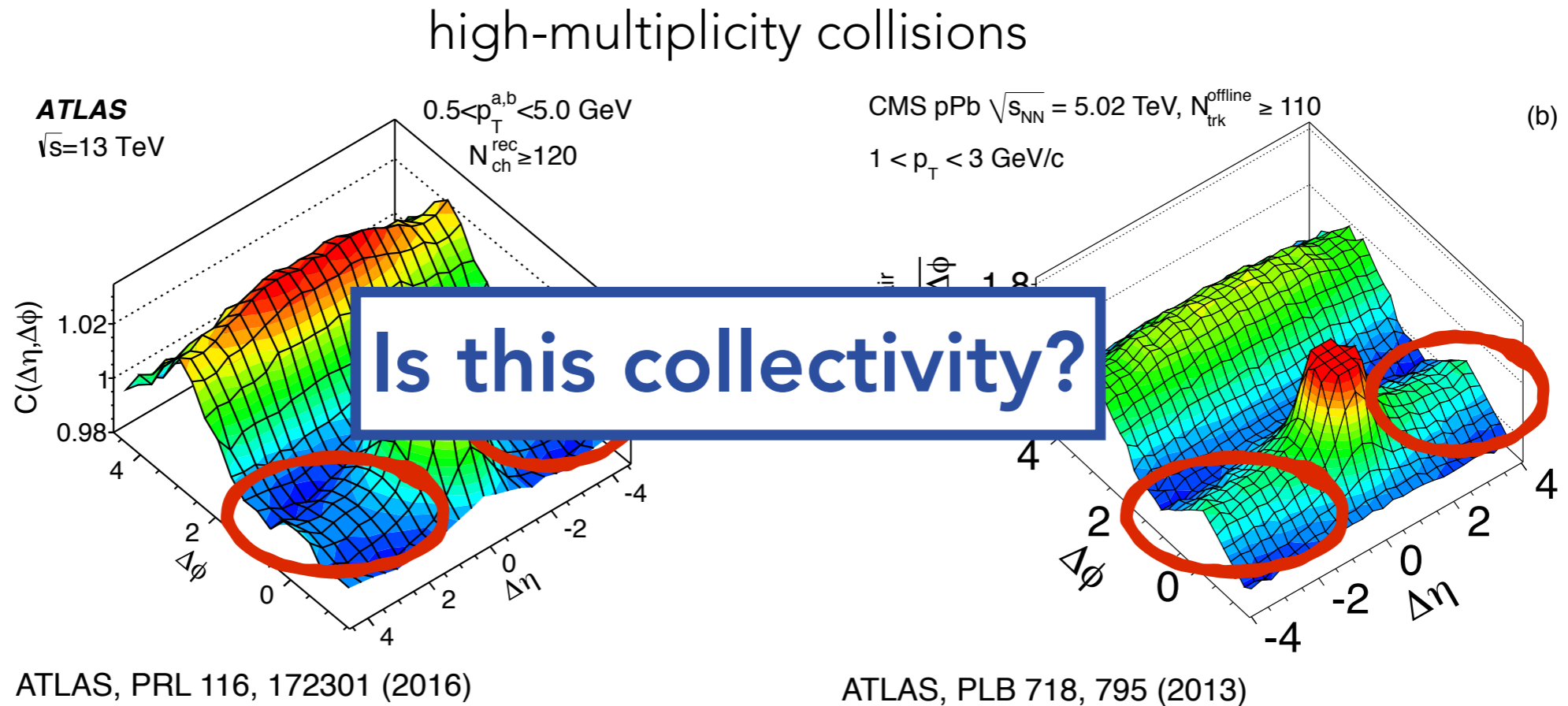
ATLAS, PRL 116, 172301 (2016)



ATLAS, PLB 718, 795 (2013)

SMALL COLLISION SYSTEMS

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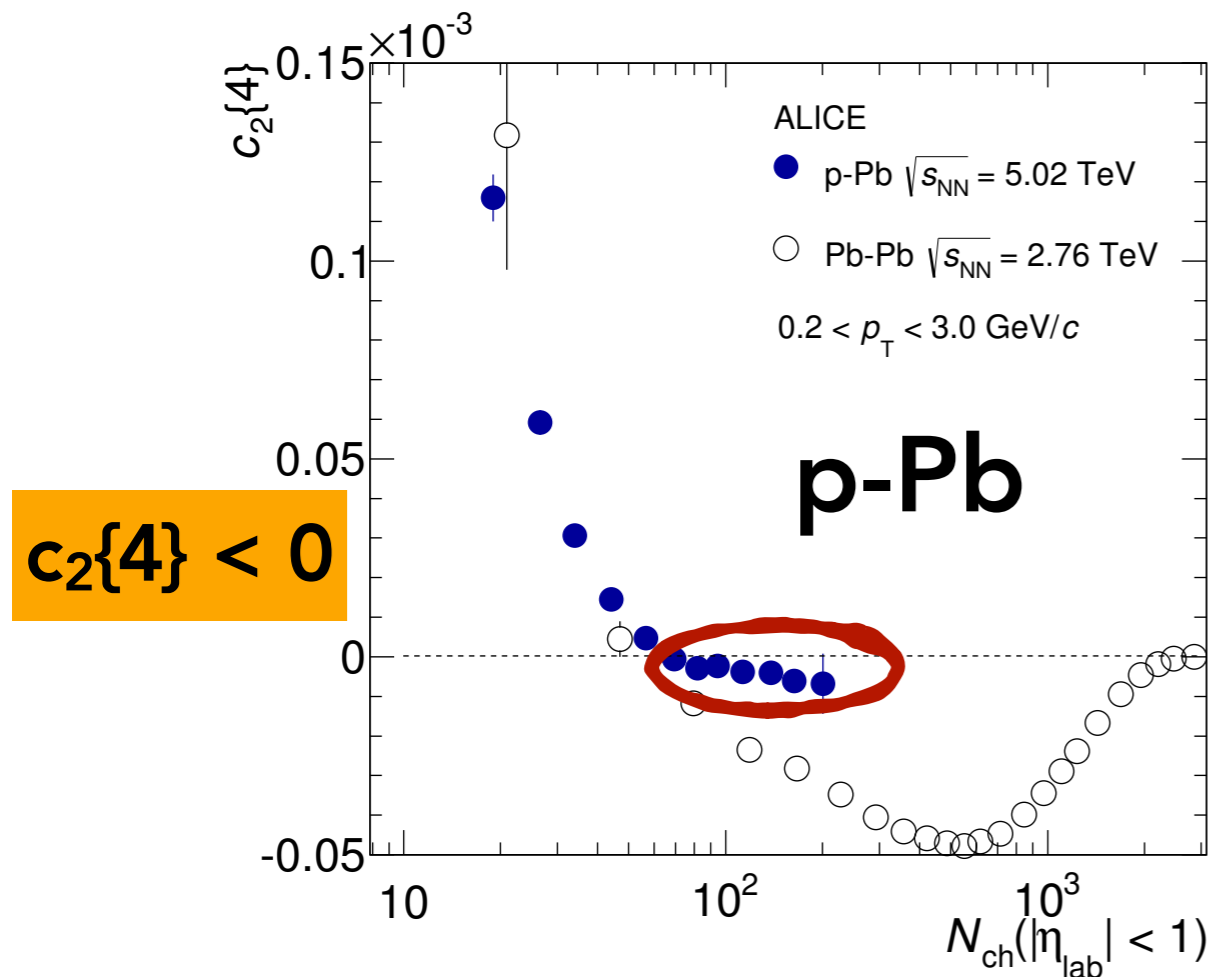


4-PARTICLE CUMULANT

- REMINDER: **Collectivity** = long-range multi-particle correlations
- What about multi-particle cumulants ($m > 2$) ?

4-PARTICLE CUMULANT

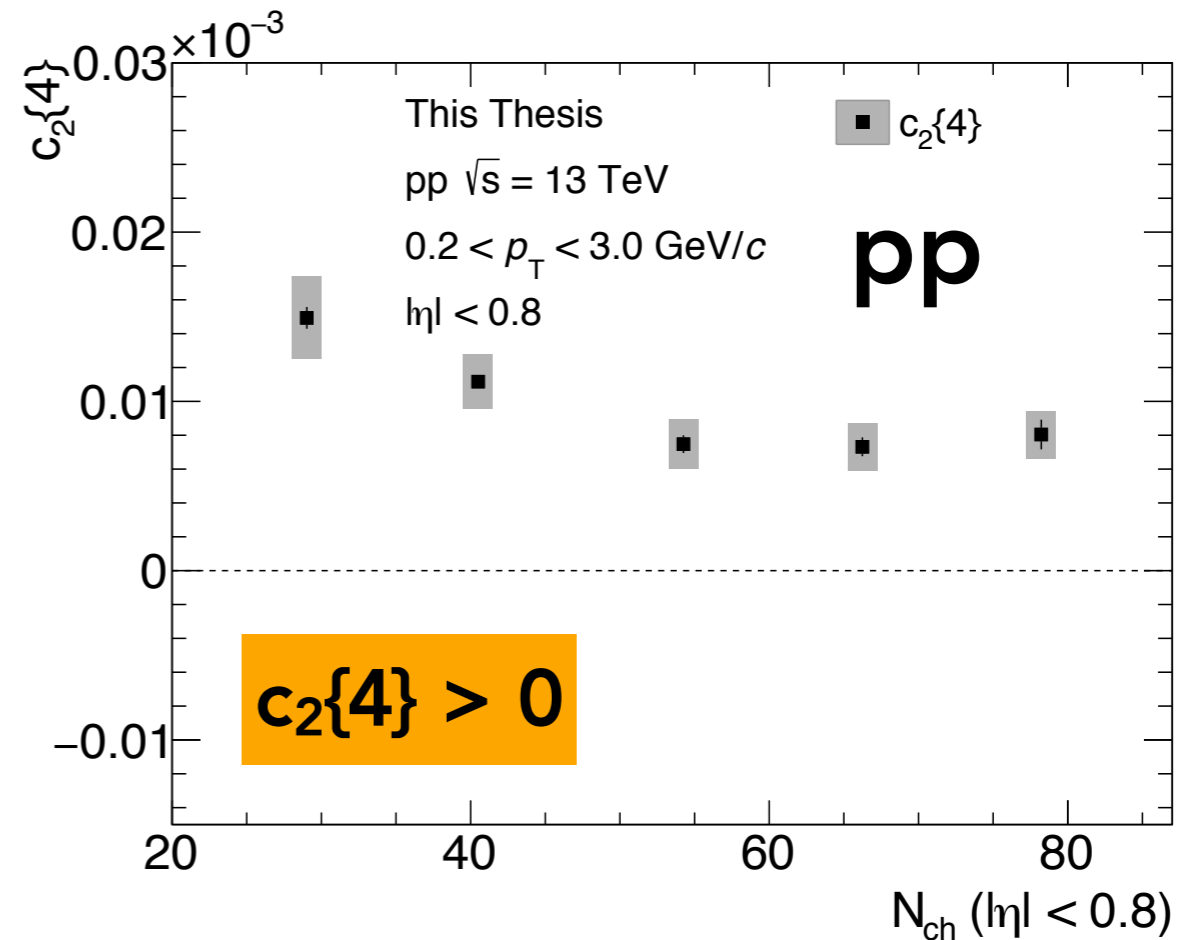
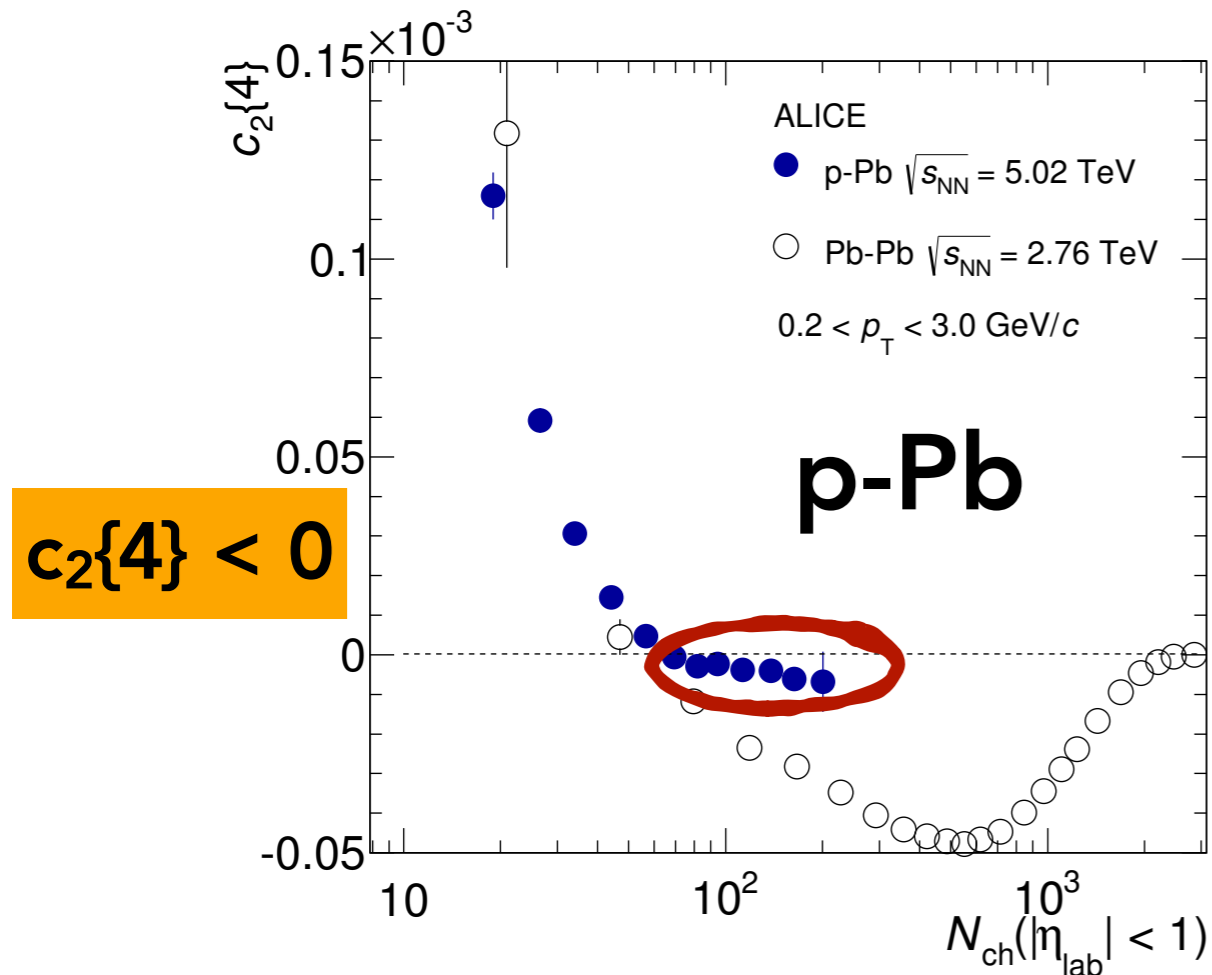
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- Hint of collectivity in p-Pb collisions

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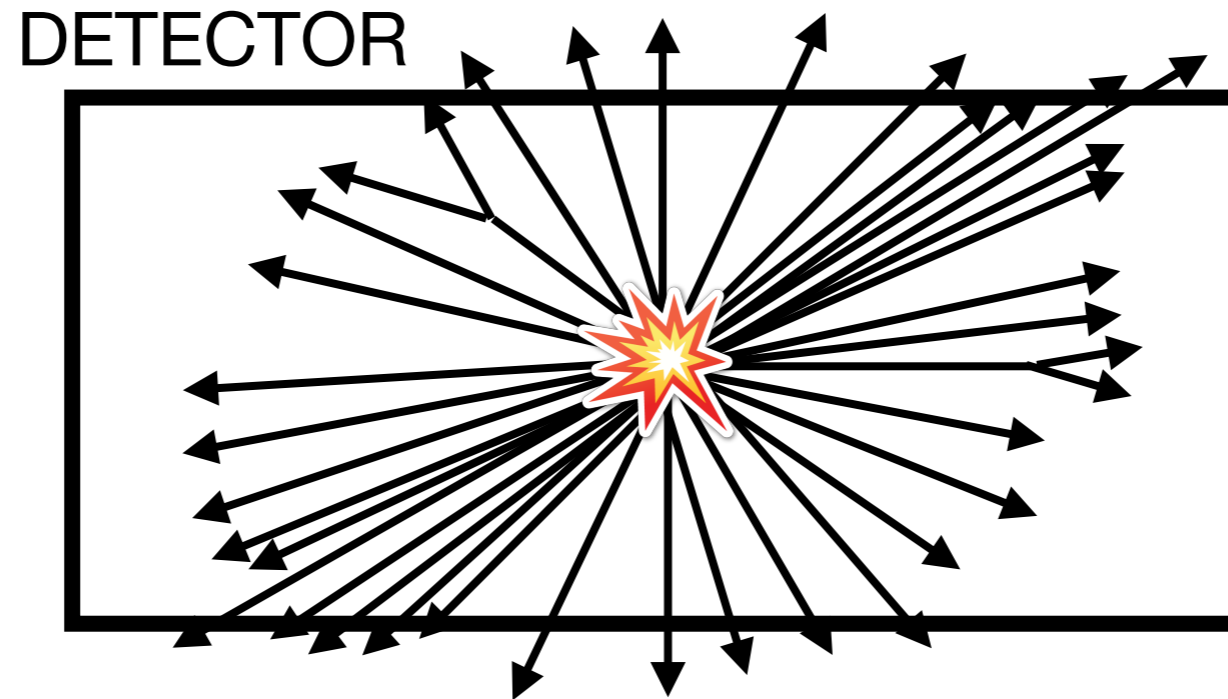


- Hint of collectivity in p-Pb collisions

$c_2\{4\} < 0 \Rightarrow$ collectivity

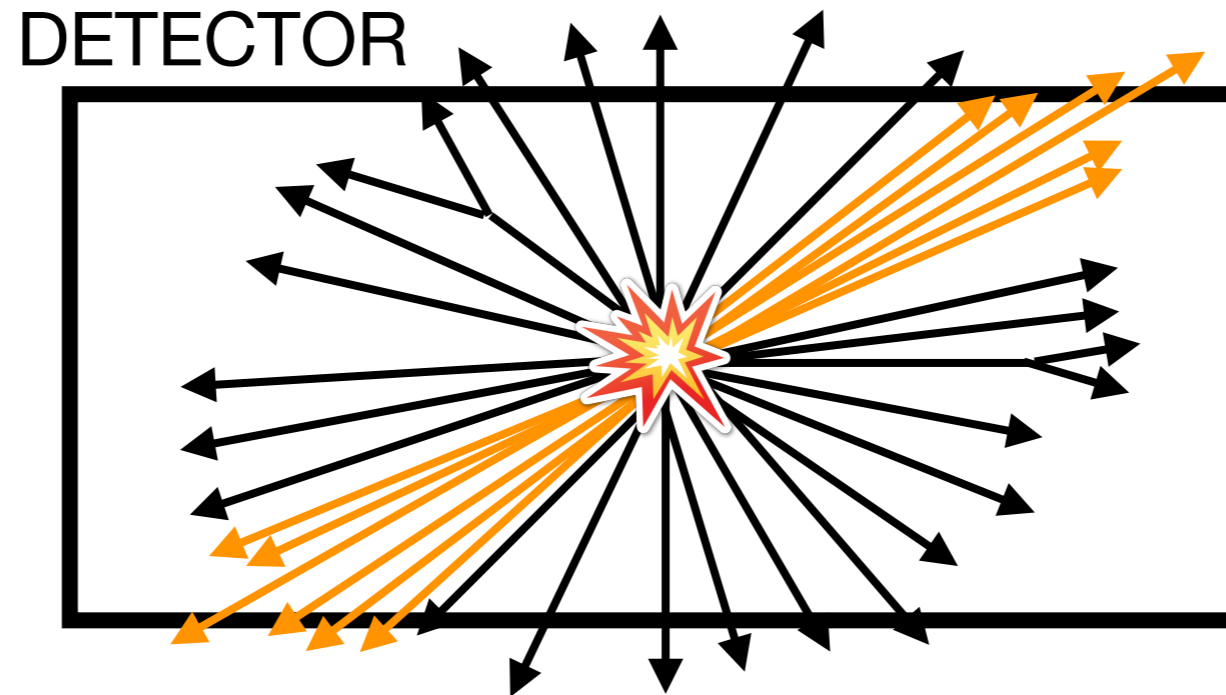
$c_2\{4\} > 0 \not\Rightarrow$ collectivity

NON-FLOW EFFECTS



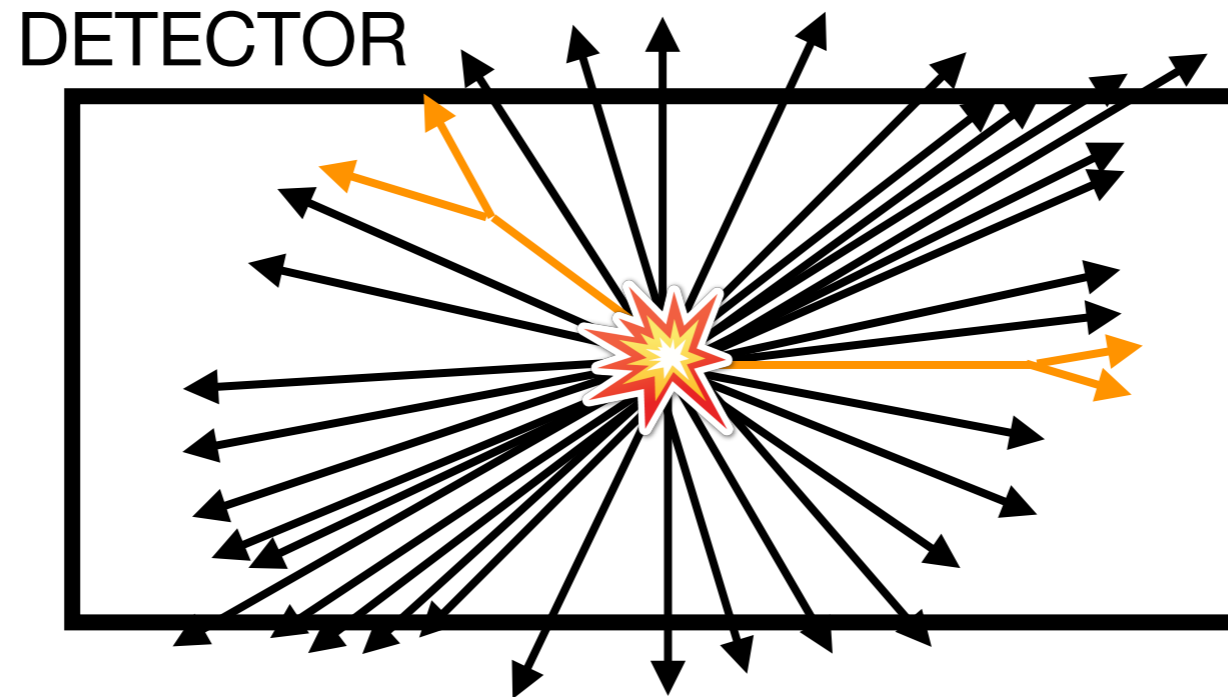
- Correlations not associated with the global symmetry plane Ψ_n

NON-FLOW EFFECTS



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- **Jets**: correlations between particles within a jet cone
correlations between particles from opposite cones

NON-FLOW EFFECTS

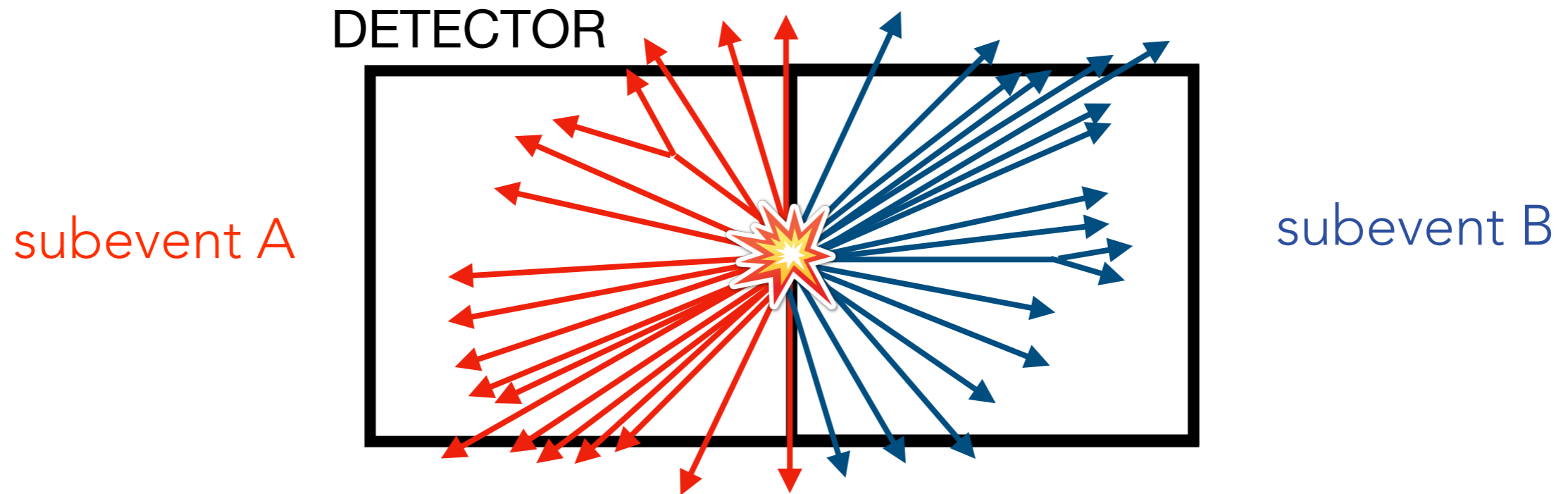


- Correlations not associated with the global symmetry plane Ψ_n
- **Jets**: correlations between particles within a jet cone
correlations between particles from opposite cones
- **Resonance decays**: correlations between the decay products

NON-FLOW EFFECTS

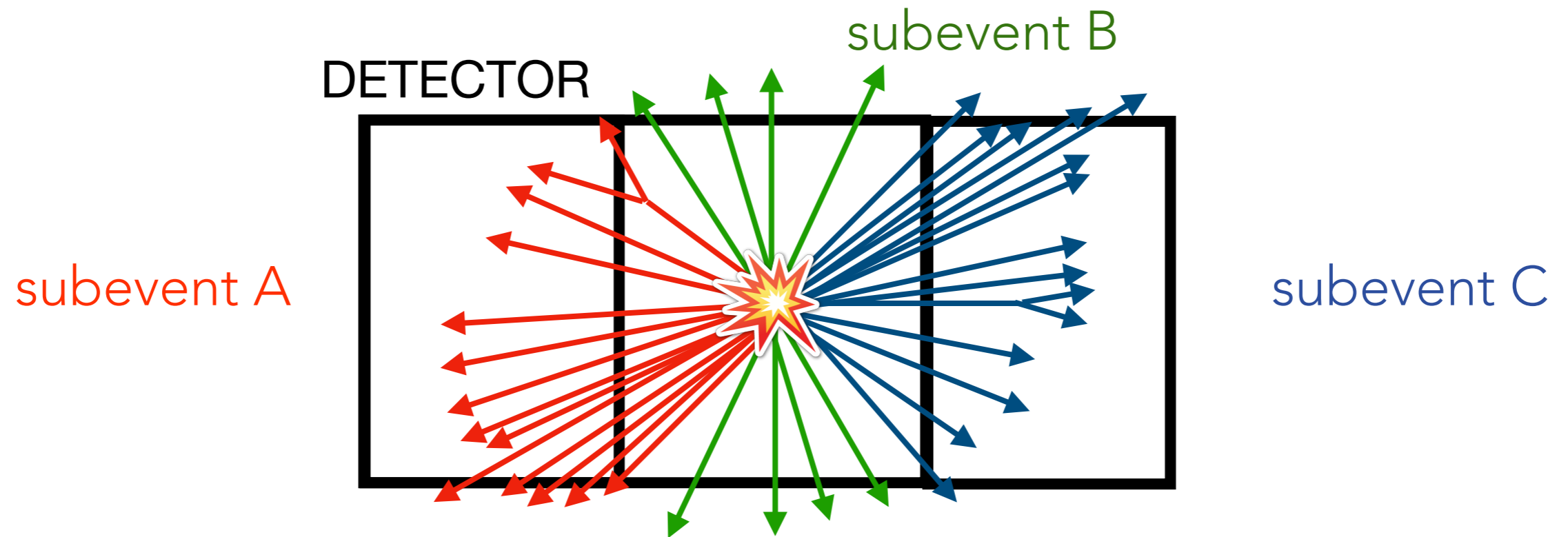
- **Subevent method**: suppresses such non-flow effects
 - Spatial separation between particles that are being correlated

NON-FLOW EFFECTS



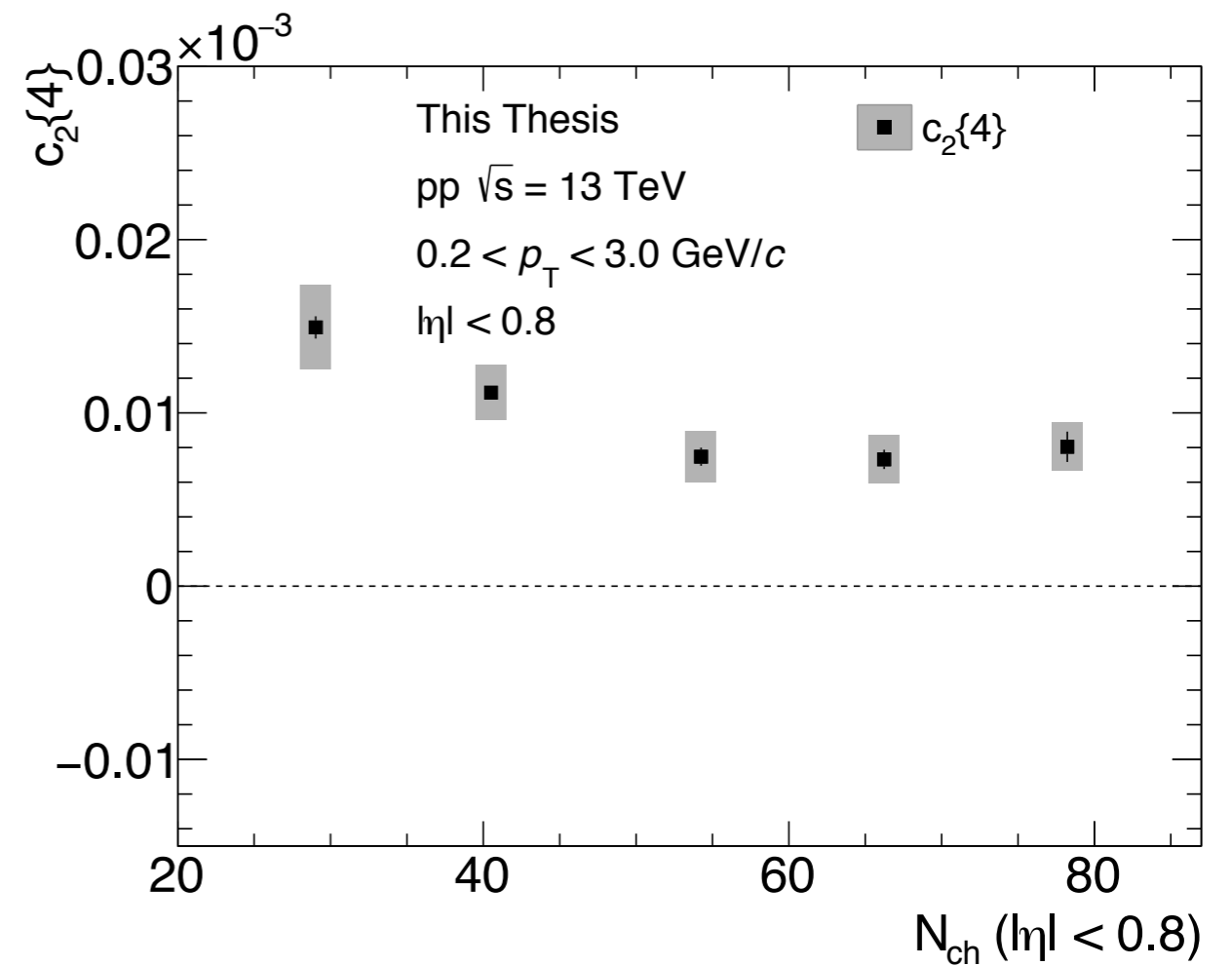
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NON-FLOW EFFECTS

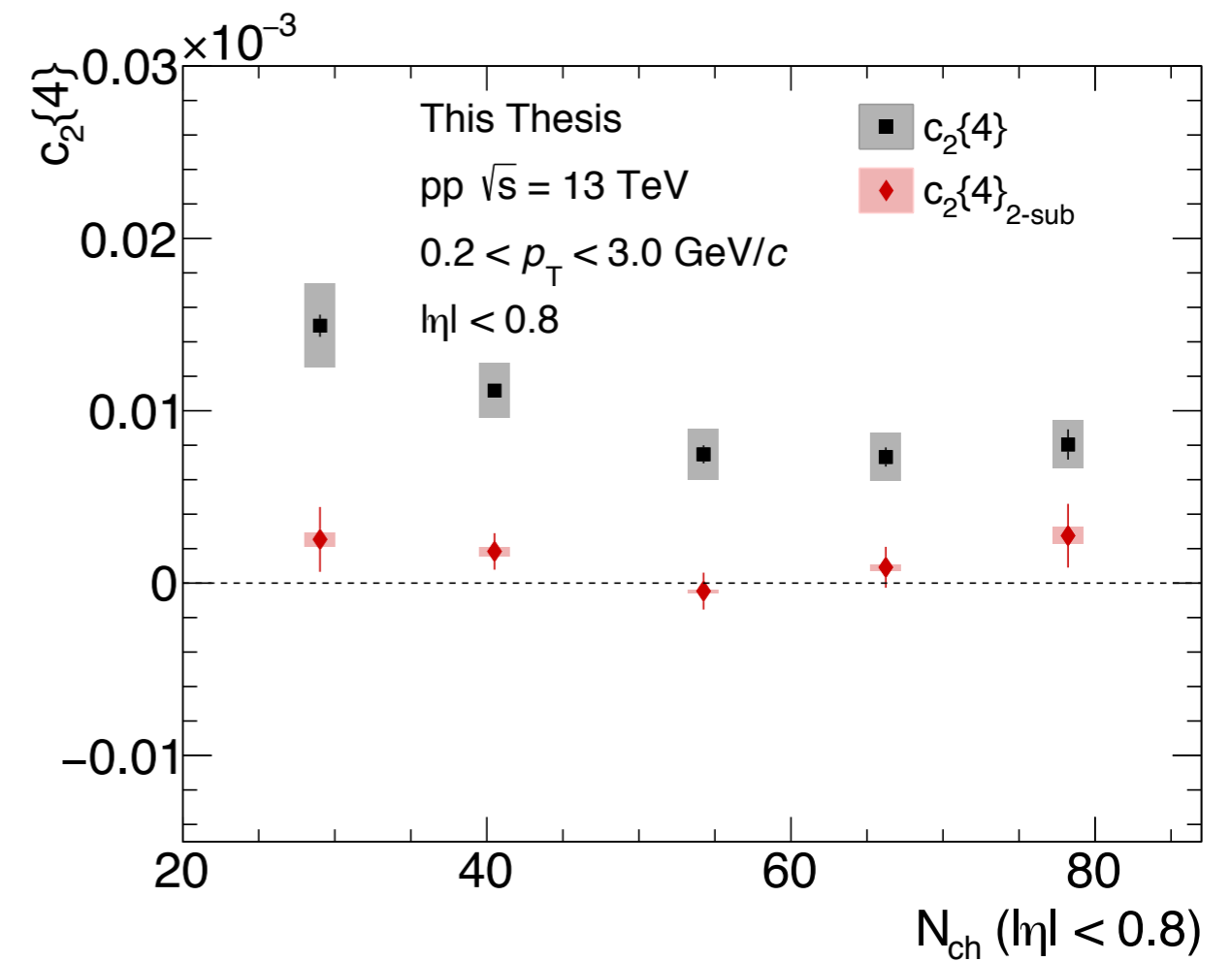


- **Subevent method:** suppresses such non-flow effects
 - Spatial separation between particles that are being correlated
- **2-subevent method:**
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- **3-subevent method:**
 - In addition suppresses correlations between jet cones

4-PARTICLE CUMULANT IN PP COLLISIONS

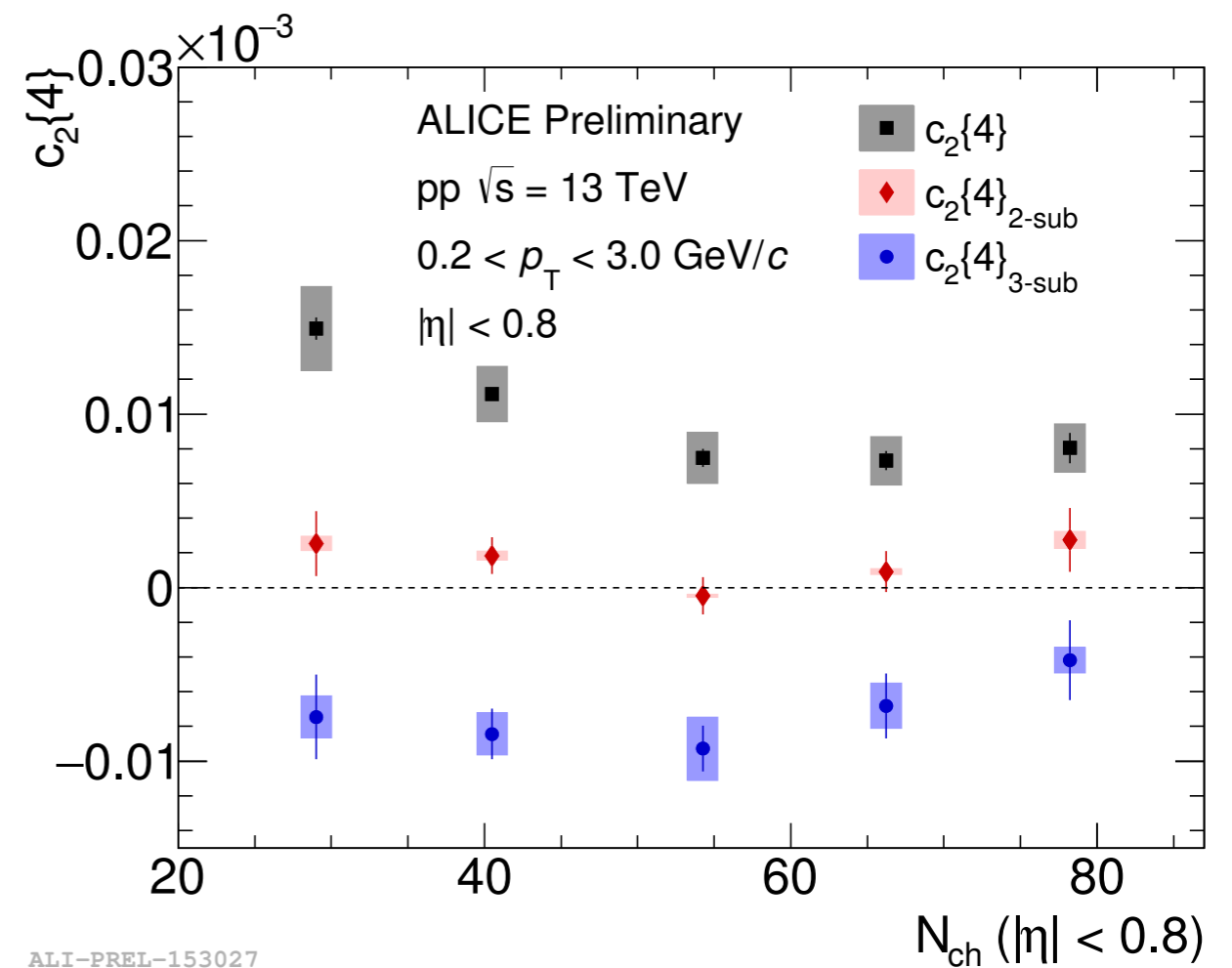


4-PARTICLE CUMULANT IN PP COLLISIONS



4-PARTICLE CUMULANT IN PP COLLISIONS

- Negative $c_2\{4\}$!
- Indication of collectivity also in pp collisions



WHAT NOW?

- The presence of collectivity doesn't necessarily mean presence of the QGP
- Next step: Investigation of the origin of collectivity in small systems by comparison to models