

David Horák

FJFI ČVUT v Praze



# Symmetric cumulants as a probe of the proton substructure

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## Symmetric cumulants as a probe of the proton substructure at LHC energies

Javier L. Albacete,<sup>1,\*</sup> Hannah Petersen,<sup>2,3,4,†</sup> and Alba Soto-Ontoso<sup>1,2,‡</sup>

<sup>1</sup>CAFPE and Departamento de Física Teórica y del Cosmos,  
Universidad de Granada, E-18071 Campus de Fuentenueva, Granada, Spain.

<sup>2</sup>Frankfurt Institute for Advanced Studies, Ruth-Moufang-Strasse 1, 60438 Frankfurt am Main, Germany.

<sup>3</sup>Institute for Theoretical Physics, Goethe University, Max-von-Laue-Strasse 1, 60438 Frankfurt am Main, Germany.

<sup>4</sup>GSI Helmholtzzentrum für Schwerionenforschung, Planckstr. 1, 64291 Darmstadt, Germany.

We present a systematic study of the normalized symmetric cumulants,  $NSC(n,m)$ , at the eccentricity level in proton-proton interactions at  $\sqrt{s} = 13$  TeV within a wounded hot spot approach. We focus our attention on the influence of spatial correlations between the proton constituents, in our case gluonic hot spots, on this observable. We notice that the presence of short-range repulsive correlations between the hot spots systematically decreases the values of  $NSC(2,3)$  and  $NSC(2,4)$  in mid-to ultra-central collisions while increases them in peripheral interactions. In the case of  $NSC(2,3)$  we find that, as suggested by data, an anti-correlation of  $\varepsilon_2$  and  $\varepsilon_3$  in ultra-central collisions, i.e.  $NSC(2,3) < 0$ , is possible within the correlated scenario while it never occurs without correlations when the number of gluonic hot spots is set to three. We attribute this fact to the decisive role of correlations on enlarging the probability of interaction topologies that reduce the value of  $NSC(2,3)$  and, eventually, make it negative. Further, we explore the dependence of our conclusions on the number of hot spots, the values of the hot spot radius and the repulsive core distance. Our results add evidence to the idea that considering spatial correlations between the subnucleonic degrees of freedom of the proton may have a strong impact on the initial state properties of proton-proton interactions [1].

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be positive. However, it turns out to be negative for very high multiplicities,  $N_{\text{trk}}^{\text{offline}} > 60$  in both p+Pb and Pb+Pb and  $N_{\text{trk}}^{\text{offline}} \sim 100$  in p+p. Moreover, NSC(2,3) in

tematic uncertainties make it compatible with zero. Relating the negative sign of NSC(2,3) at very high multiplicities with the initial geometry of the proton is the main goal of this work.

the color fields in the heavy nuclear target [21, 22]. Up to today we are unaware of any theoretical prediction for the values of SC(n,m) in p+p interactions at LHC energies, although results for RHIC energies were presented

tween different flow harmonics  $v_n$  i.e. the symmetric cumulants defined as [2, 3]

$$\text{SC}(n, m) = \langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle \quad (1)$$

or in their normalized version

$$\text{NSC}(n, m) = \frac{\langle v_n^2 v_m^2 \rangle - \langle v_n^2 \rangle \langle v_m^2 \rangle}{\langle v_n^2 \rangle \langle v_m^2 \rangle} \quad (2)$$

parameter for the collision, we sample the transverse positions of the three hot spots in each proton  $\{\vec{s}_i\}$  according to the distribution

$$D(\vec{s}_1, \vec{s}_2, \vec{s}_3) = C \prod_{i=1}^3 e^{-s_i^2/R^2} \delta^{(2)}(\vec{s}_1 + \vec{s}_2 + \vec{s}_3) \times \prod_{\substack{i < j \\ i,j=1}}^3 \left(1 - e^{-\mu|\vec{s}_i - \vec{s}_j|^2/R^2}\right). \quad (3)$$

model. The third term of Eq. 3 allows us to go beyond these approaches by implementing short range repulsive correlations among all pairs of hot spots that effec-

jectile, the next step in the Monte Carlo simulation is to decide which of them have been wounded [40, 41] i.e.

the hot spot-hot spot scattering amplitude  $\rho_{hs}$ . Thus, in each event, the maximum number of wounded hot spots  $N_w$  and collisions  $N_{coll}$  is 6 and 9 respectively. In

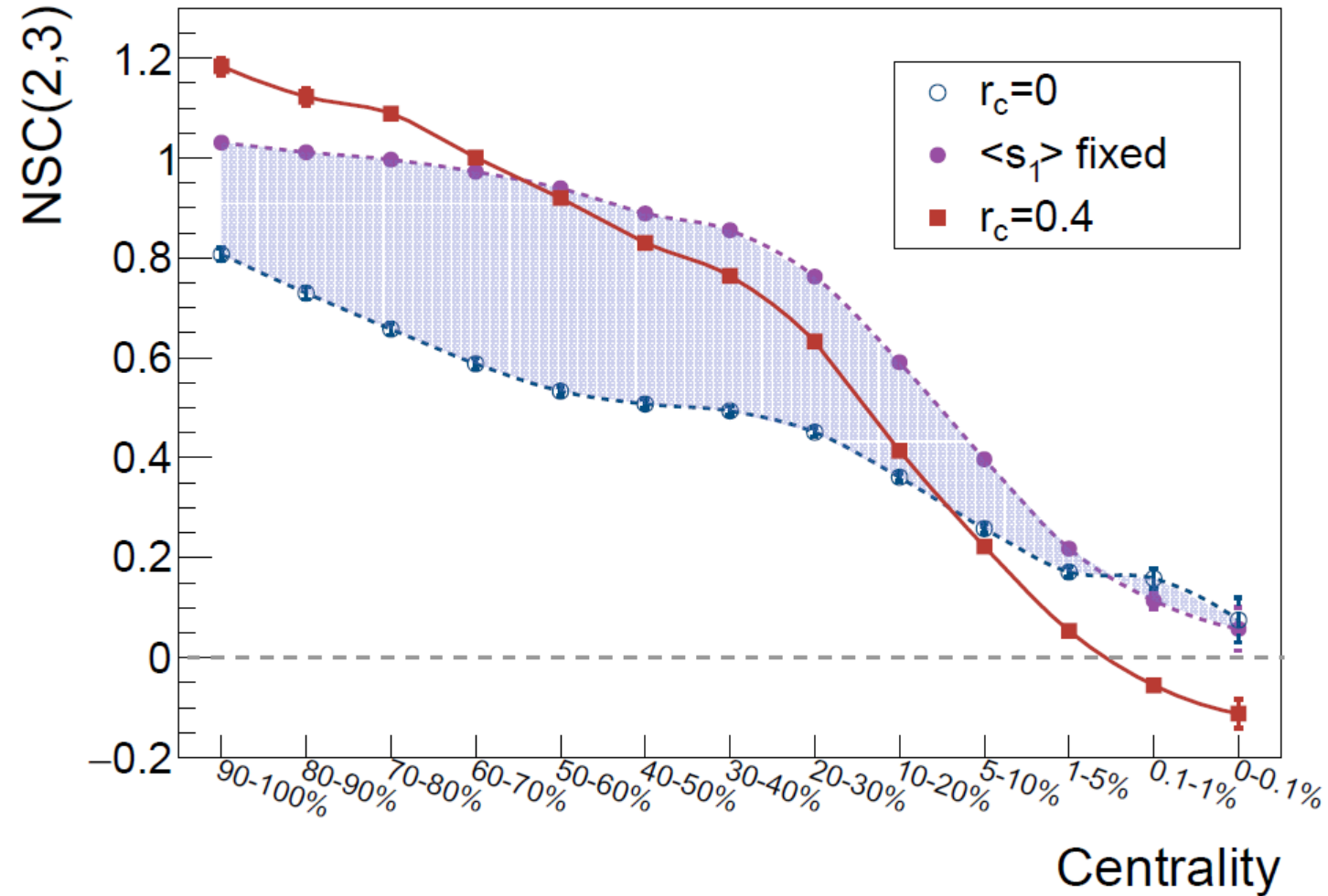
calculation to other regions of the parameter space. The three correlation scenarios under consideration in this work are the following: first,  $r_c = 0.4$  refers to the correlated scenario with  $\{R_{hs}, R, \rho_{hs}\}$  constrained to reproduce the extrapolated values of the total cross section and the ratio of real and imaginary parts of the scattering amplitude [42]. In the second case we impose the latter constraints to  $\{R_{hs}, R, \rho_{hs}\}$  after setting  $r_c = 0$ . However, in order to do a more realistic comparison between

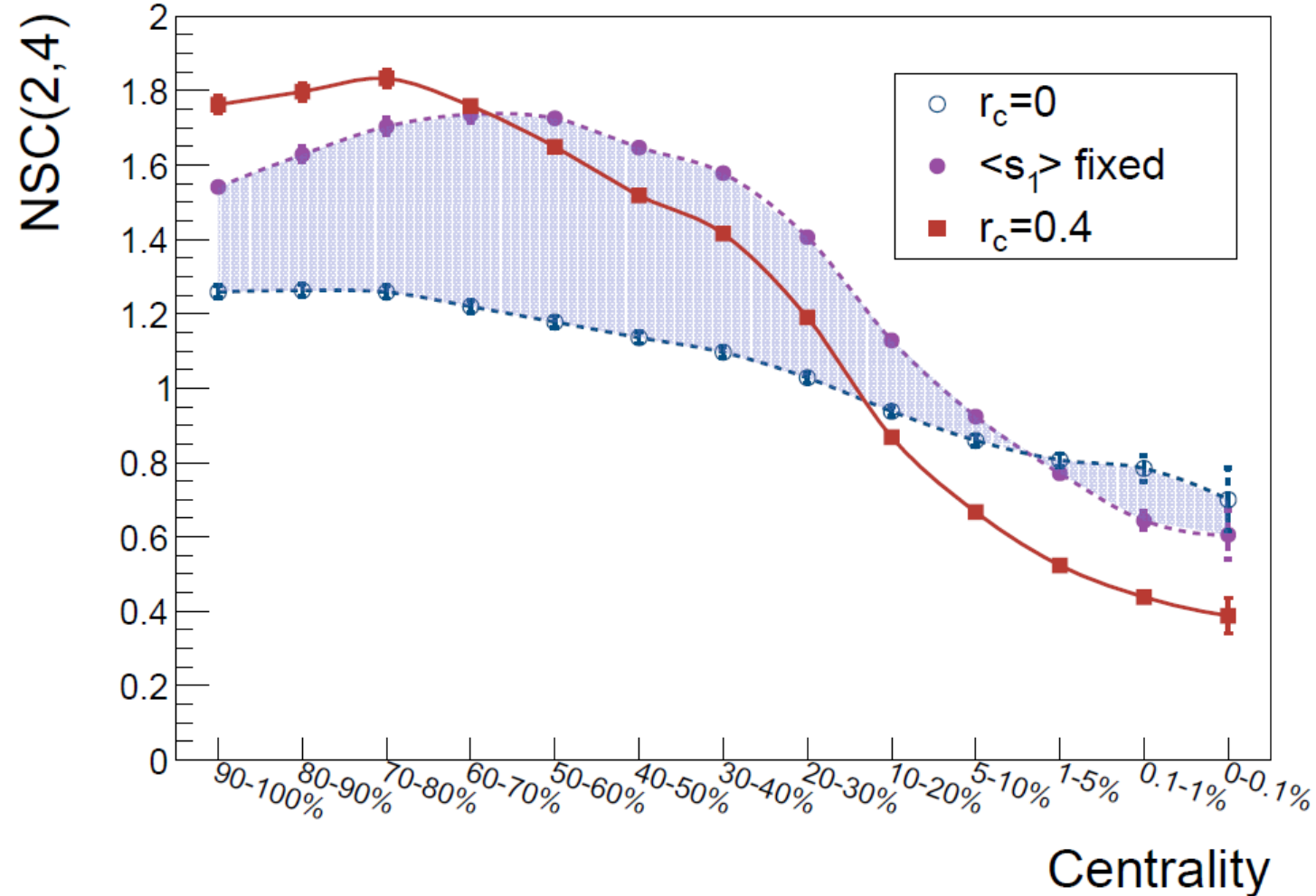
ence of repulsive correlations. The case labeled as " $\langle s_1 \rangle$  fixed" constitutes an attempt to perform this task by fixing the r.m.s of the spatial probability distribution given by Eq. 3 to be the same as in the  $r_c = 0.4$  scenario. In the following plots the uncorrelated results will be exhibited as a band bounded by the  $r_c = 0$  and  $\langle s_1 \rangle$  fixed cases to display the different possibilities considered.



served in the ultra-central bins [0-0.1%] and [0.1-1%]: only in the  $r_c = 0.4$  case there exists an anti-correlation of  $\varepsilon_2$  and  $\varepsilon_3$  as data dictates. Then, we conclude that the experimental evidence of  $\text{NSC}(2,3) < 0$  may back up the necessity to consider correlated proton constituents.

ticular mechanism i.e. the presence of spatial correlations inside the proton that builds up a negative value of  $\text{NSC}(2,3)$  in the highest centrality bin at the geometric level.



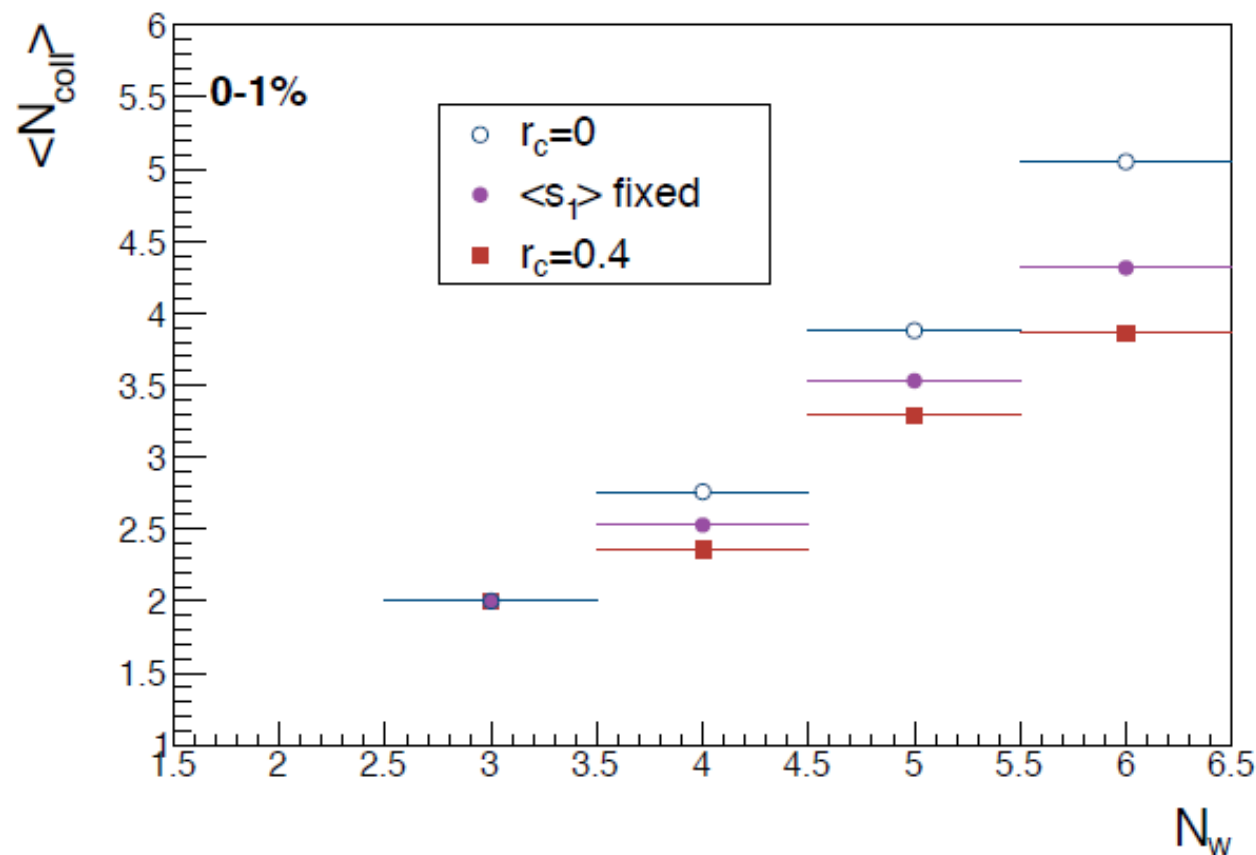


In the case of NSC(2,4), the role of the repulsive correlations is qualitatively the same as in the NSC(2,3) cal-



In order to capture the effect of the spatial correlations we characterize each proton-proton interaction by its number of wounded hot spots and the number of collisions ( $N_w, N_{\text{coll}}$ ), the two basic quantities of any Monte-Carlo Glauber calculation. We dub each ( $N_w, N_{\text{coll}}$ )-

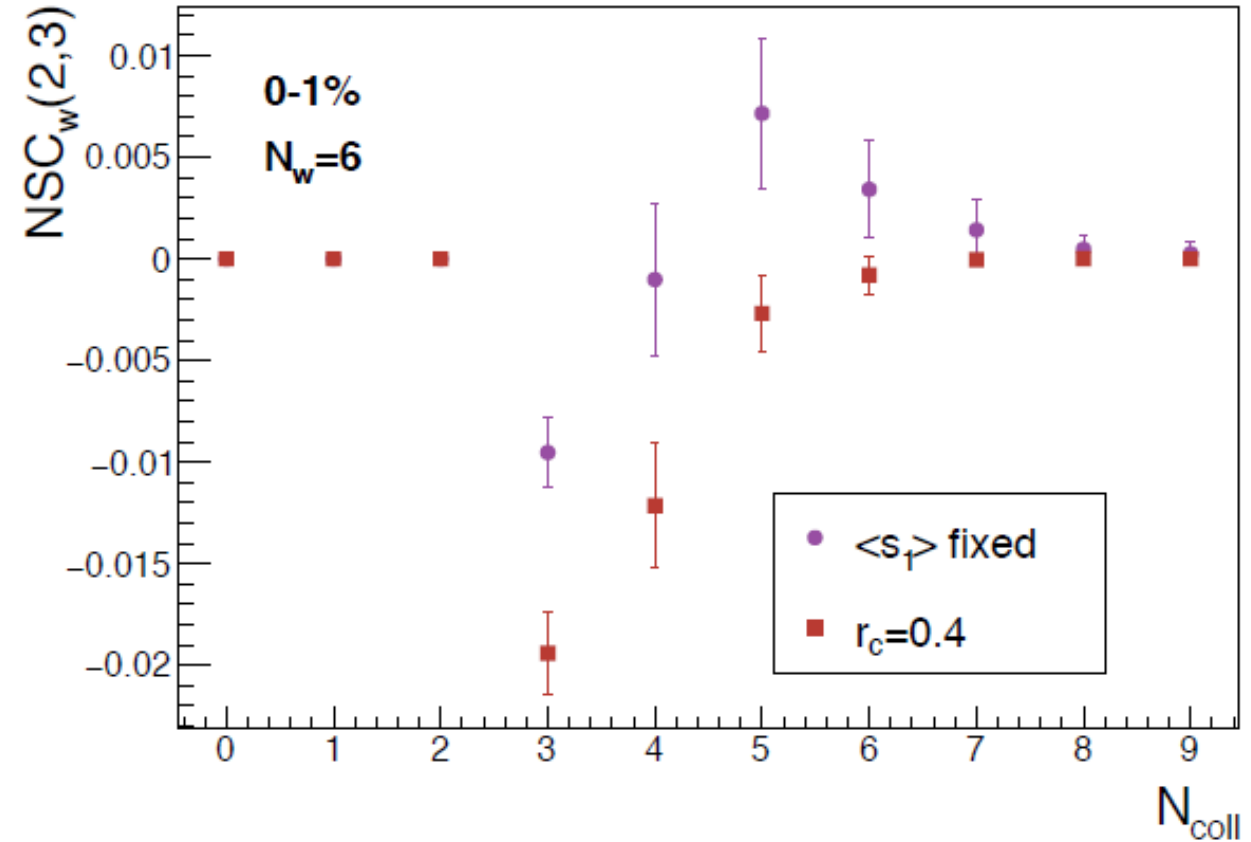
the only existing configuration. However, for  $N_w > 3$  the average number of collisions starts to differ between the three different cases. We observe that  $\langle N_{\text{coll}} \rangle$  is systematically reduced when including repulsive correlations with respect to the uncorrelated cases. This effect has a very straightforward interpretation: enlarging the mean transverse distance between the hot spots reduces the probability of having interaction topologies with a high number of collisions. In other words, the repulsive



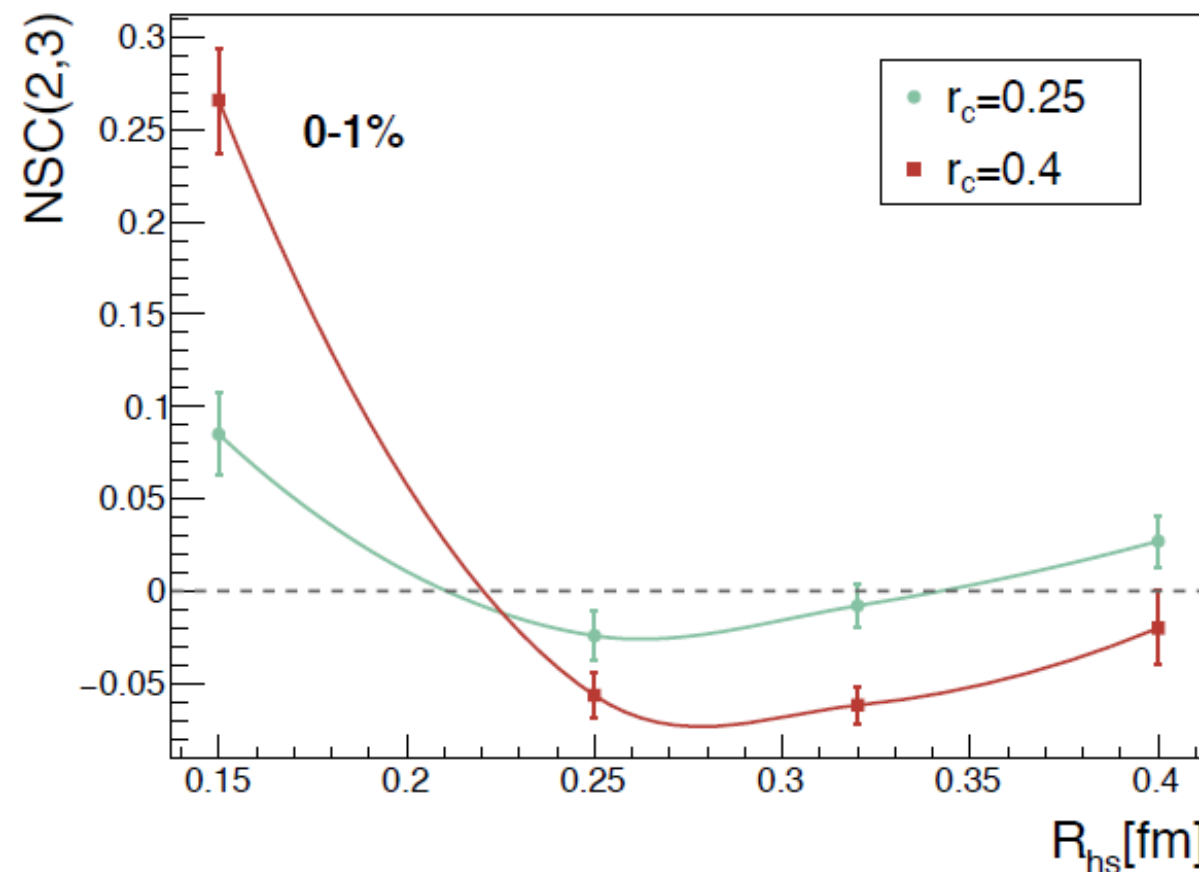
$$N_W = 6$$

configurations with a large number of collisions, e.g.  $N_{\text{coll}} > 6$ , only occur in the uncorrelated case where the three hot spots are closer to each other or, equiva-

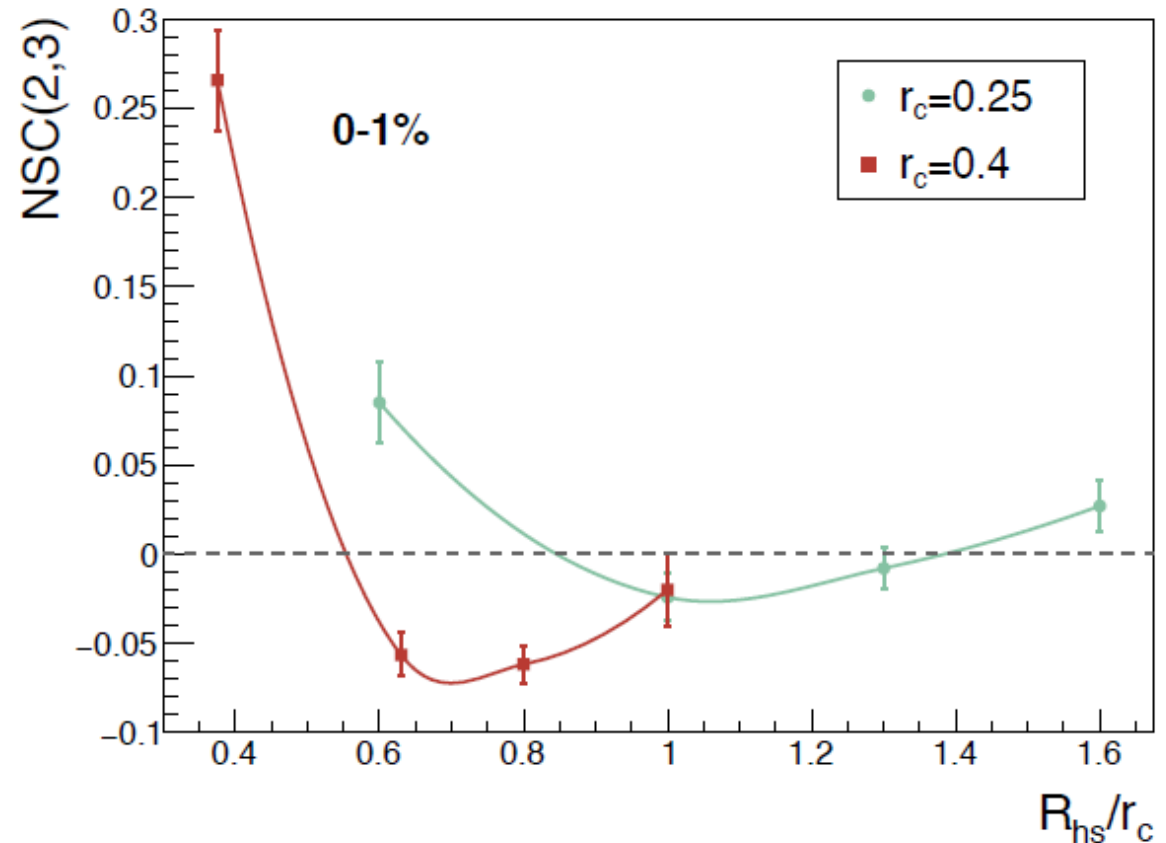
lently, clustered. Second, and more important, the value of  $\text{NSC}_w(2,3)$  shows a clear dependence on  $N_{\text{coll}}$ : configurations with a smaller number of collisions reduce the value of  $\text{NSC}(2,3)$  and, eventually, contribute negatively.



universal as it breaks down when  $R_{hs} \lesssim 0.22$  fm. In this scenario of very small values of the radius of the hot spot, i.e.  $R_{hs} \lesssim 0.22$  fm,  $\varepsilon_2$  and  $\varepsilon_3$  are positively correlated for both values of the repulsive core distance and the value of NSC(2,3) is larger in the  $r_c = 0.4$  case. This result indicates that NSC(2,3) is not sensitive to  $R_{hs}$  and  $r_c$  independently but to the interplay of both scales. In other words, NSC(2,3) depends on a generic function of the radius of the hot spot and the repulsive core distance  $f(R_{hs}, r_c)$ .

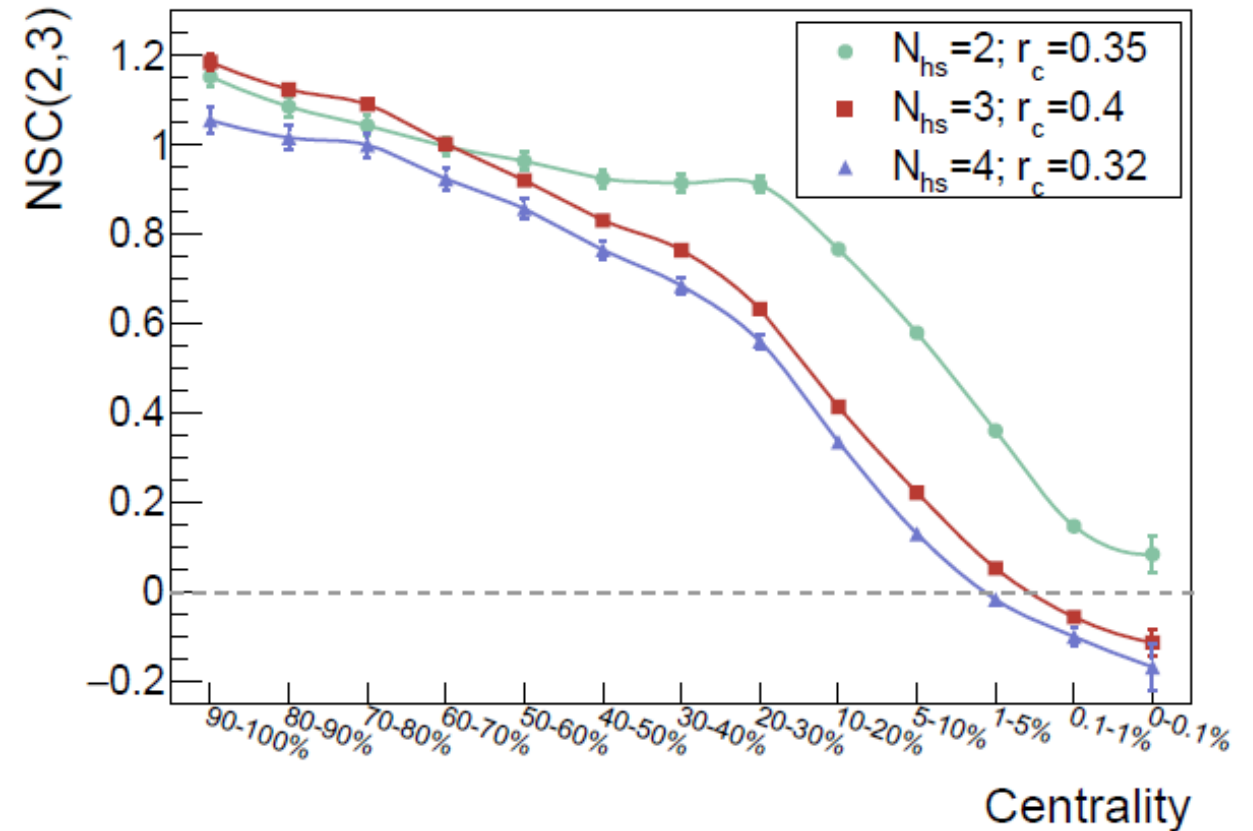


sult into a positive correlation between  $\varepsilon_2$  and  $\varepsilon_3$ . Then, our study favors values of  $0.6 \lesssim R_{hs}/r_c \lesssim 1.3$  in order to be compatible with the experimental observation of  $NSC(2,3) < 0$  in the highest centrality bin. Unfortunately, this interval is large enough to be compatible with a picture of the proton in which the hot spots transverse separation is larger than in the uncorrelated case but still they can overlap ( $R_{hs}/r_c \sim 1.3$ ) and with a much more dilute description in which the probability of two hot spots to overlap is highly suppressed ( $R_{hs}/r_c \sim 0.6$ ).



ering the two more straight-forward extensions of our model:  $N_{hs} = 2$  and  $N_{hs} = 4$ . In order to make a

ered. Specifically, the negative sign of  $NSC(2,3)$  in the high centrality bins is not achieved when  $N_{hs} = 2$  even with correlations. Thus, we conclude that with the selected parameters the minimum number of hot spots to describe the onset of the anti-correlation between  $\varepsilon_2$  and  $\varepsilon_3$  is  $N_{hs} = 3$ . It should also be noted that the inclusion of an additional hot spot i.e.  $N_{hs} = 4$  helps to make  $NSC(2,3)$  even more negative in the highest centrality bins although the effect is small when compared to the drastic impact of changing from  $N_{hs} = 2$  to  $N_{hs} = 3$ .



tropy deposition as a proxy of particle production. We find that the inclusion of short-range repulsive correlations has a critical impact on the sign of  $NSC(2,3)$  in ultra central collisions. The net effect of the presence of corre-