

# Phase stability of actinide carbides

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# Introduction

## What do we do?

- prospective nuclear fuels for IV. generation nuclear reactors
- calculating materials properties using quantum mechanical calculations
  - experimental research too expensive

## What are we interested in?

- 5f-electrons behavior
  - not localized but itinerant, especially at high temperatures
  - possible study of other 5f compounds
- nuclear fuels
  - heat capacity, thermal conductivity

# Goals

## Motivation

- there was only one study<sup>1</sup> that calculated energy – volume curves and elastic constants of  $\text{U}_2\text{C}_3$
- No  $\text{Th}_2\text{C}_3$  in phase diagram of thorium carbides
  - Krupka<sup>2</sup> managed to synthesize  $\text{Th}_2\text{C}_3$  only under high pressure

## Questions

- What is the magnetic order of our compounds?
- What is the effect of spin-orbital coupling?
- What is the electronic structure of the phases?
- Is  $\text{Th}_2\text{C}_3$  stable at ambient pressure?
- What is the best way to model properties of selected structures?

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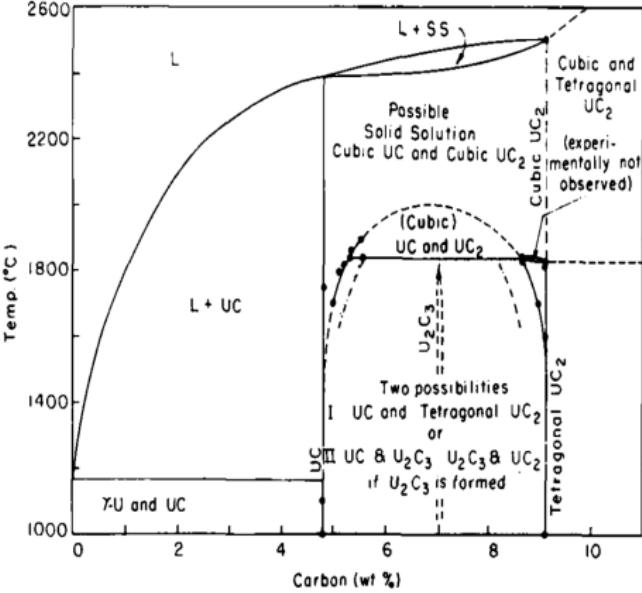
<sup>1</sup>H. Shi et al., J. Nucl. Mater., 396, 218-222 (2010).

<sup>2</sup>M. C. Krupka, J. Less-Common Metals 20, 135-140 (1970).

# Uranium Sesquicarbide

## Available experimental data

- Cubic, space group 220 (I-43d),  $\text{Pu}_2\text{C}_3$  type<sup>1</sup>
- Lattice parameter<sup>1,2</sup>, density<sup>3,4</sup>, C – C bond length<sup>5,6</sup>
- Thermal conductivity<sup>4</sup> for  $T = 1000 - 2200 \text{ K}$
- Thermal expansion<sup>7,8</sup> for  $T = 1300 - 2000 \text{ K}$
- Thermodynamic properties (e. g. heat capacity<sup>8,9</sup> for  $0 - 330 \text{ K}$ )



<sup>1</sup>W. B. Wilson, J. Am. Ceram. Soc., 43, 77-81 (1960).

<sup>2</sup>J. F. A. Hennecke and C. J. Toussaint, J. Appl. Crystallogr. 2, 301 (1969).

<sup>3</sup>M. W. Mallett et al., J. Electrochem. Soc. 98, 12 1961., <sup>4</sup>R. De Coninck et al., J. Nucl. Mater., 46, 213-216 (1973).

<sup>5</sup>A. E. Austin, Acta Cryst., 12, 159-161 (1959)., <sup>6</sup>H. Shi et al., J. Nucl. Mater., 396, 218-222 (2010).

<sup>7</sup>R. De Coninck et al., J. Nucl. Mater., 46, 213-216 (1973)., <sup>8</sup>R. J. L. Andon et al., Trans. Faraday Soc., 60, 1030-1037 (1964).

<sup>9</sup>J. M. Leitnaker and T. G. Godfrey, J. Nucl. Mater., 21, 175-189 (1967).

# Methodology

- Born-Oppenheimer approximation
  - calculations include only electrons, not atomic cores
- we calculate electron density<sup>1</sup>, not electron wavefunctions
- SCF - Self-Consistent Field
  - iterative method

## Density Functional Theory (DFT)

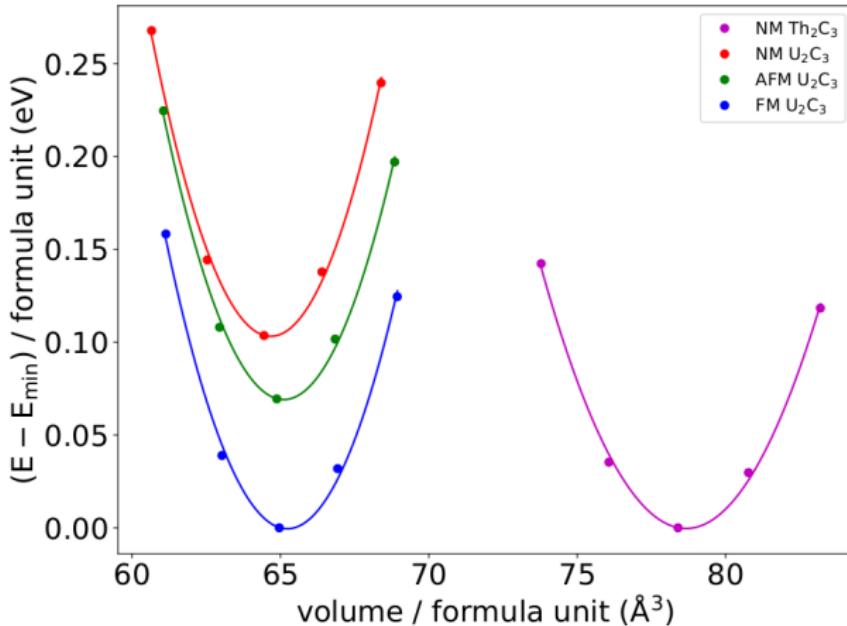
- potential of all particles can be rewritten as electron density<sup>1</sup>
- Kohn-Sham orbitals<sup>2</sup> - orbitals close to real ones
  - one electron in the field of other electrons
  - variation principle - there is only one density that corresponds to global energy minimum

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<sup>1</sup>Hohenberg, P. and Kohn, W., Phys. Rev. B, 136, B864-& (1964).

<sup>2</sup>Kohn, W. and Sham, LJ, Phys. Rev., 140, 1133-& (1965).

# Results - Ground-State Properties



• NM  $\text{Th}_2\text{C}_3$   
• NM  $\text{U}_2\text{C}_3$   
• AFM  $\text{U}_2\text{C}_3$   
• FM  $\text{U}_2\text{C}_3$

$\text{U}_2\text{C}_3$	$a[\text{\AA}]$
our work	8.1061
exp. <sup>1</sup>	8.0870
exp. <sup>2</sup>	8.0899
theory <sup>3</sup>	8.0970

$\text{Th}_2\text{C}_3$	$a[\text{\AA}]$
our work	8.5599
exp. <sup>4</sup>	8.5555

<sup>1</sup>W. B. Wilson, J. Am. Ceram. Soc., 43, 77-81 (1960).

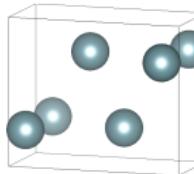
<sup>2</sup>J. F. A. Hennecke and C. J. Toussaint, J. Appl. Crystallogr. 2, 301 (1969).

<sup>3</sup>H. Shi et al., J. Nucl. Mater., 396, 218-222 (2010).

<sup>4</sup>M. C. Krupka, J. Less-Common Metals 20, 135-140 (1970).

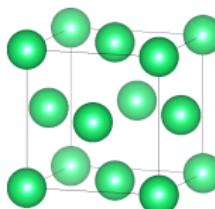
# Results - Enthalpy of Formation

	$\frac{\Delta H_f}{\text{formula unit}} [\text{eV}]$
NM $\text{U}_2\text{C}_3$	-1.037
AFM $\text{U}_2\text{C}_3$	-1.060
FM $\text{U}_2\text{C}_3$	-1.127
FM+SOI+U $\text{U}_2\text{C}_3$	-1.428
NM $\text{Th}_2\text{C}_3$	-1.706

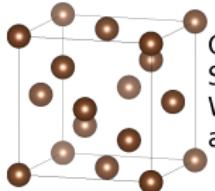


Uranium - Orthorhombic  
Space group: 63 (Cmcm)  
Wyck.: 4c exp<sup>1</sup>:  
 $a = 2.8087 \text{ \AA}$   $a = 2.854 \text{ \AA}$   
 $b = 5.8379 \text{ \AA}$   $b = 5.870 \text{ \AA}$   
 $c = 4.9160 \text{ \AA}$   $c = 4.955 \text{ \AA}$

$$\Delta H_f = E_{\text{Ac}_2\text{C}_3} - (2 E_{\text{Ac}} + 3 E_{\text{C}})$$



Thorium - Cubic (fcc)  
Space group: 225 (Fm-3m)  
Wyck.: 4a exp<sup>2</sup>:  
 $a = 5.0408 \text{ \AA}$   $a = 5.180 \text{ \AA}$



Carbon - Cubic (diamond)  
Space group: 227 (Fd-3m)  
Wyck.: 8a exp<sup>3</sup>:  
 $a = 3.5716 \text{ \AA}$   $a = 3.5597 \text{ \AA}$

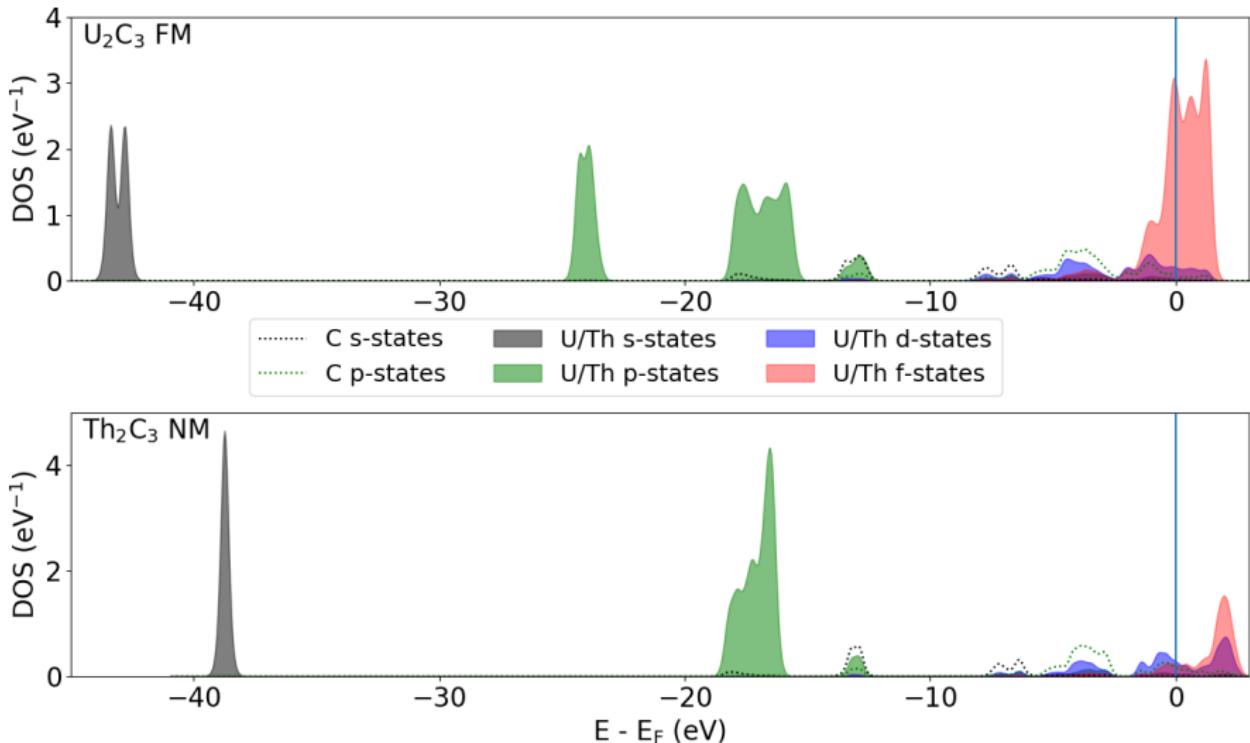
- Both  $\text{U}_2\text{C}_3$  and  $\text{Th}_2\text{C}_3$  are stable at 0 K and ambient pressure
- $\text{U}_2\text{C}_3$  is ferromagnetic while magnetism plays no role in  $\text{Th}_2\text{C}_3$ 's enthalpy of formation

<sup>1</sup>I. Grenthe et al., *The Chemistry of the Actinide and Transactinide Elements* (Springer, Dordrecht, 2008).

<sup>2</sup>Premo Chiotti, J. Electrochem. Soc. 110, 567-570 (1954).

<sup>3</sup>M. E. Straumanis and E. Z. Aka, J. Am. Chem. Soc. 73, 5643-5646 (1951).

# Results - Density of States



# Mechanical Properties

- for a cubic system, there are three independent elastic constants<sup>1</sup>

$$C_{cubic} = \begin{vmatrix} c_{11} & c_{12} & c_{12} & 0 & 0 & 0 \\ & c_{11} & c_{12} & 0 & 0 & 0 \\ & & c_{11} & 0 & 0 & 0 \\ & & & c_{44} & 0 & 0 \\ & & & & c_{44} & 0 \\ & & & & & c_{44} \end{vmatrix}$$

- Young's modulus<sup>1</sup> - materials resistance to uniaxial deformation
  - $E = \frac{(c_{11}-c_{12})(c_{11}+2c_{12})}{c_{11}+c_{12}}$
- Shear modulus<sup>1</sup> - materials resistance to shear stress
  - $G = c_{44}$
- Bulk modulus<sup>1</sup> - materials resistance to compression
  - $B = \frac{c_{11}+2c_{12}}{3}$

<sup>1</sup> G. Grimvall, *Thermophysical Properties of Materials* (Elsevier, North-Holland, Amsterdam, 1999).

# Results - Mechanical Properties

- Born's elastic stability conditions<sup>1</sup> for cubic system
  - $(c_{11} > |c_{12}|) \wedge (c_{44} > 0)$
- Pugh ratio<sup>2</sup>  $\frac{G}{B}$  - brittle to ductile border at 0.57
- Zener anisotropy<sup>1</sup>  $A_Z$  - if equal to 1, the material is isotropic
  - $A_Z = \frac{c_{44}}{C'} = \frac{2c_{44}}{c_{11}-c_{12}}$
- Poisson's ratio<sup>1</sup> - brittle to ductile border at 0.26
  - $\nu = \frac{3B-2G}{2(3B+G)}$

GPa	$c_{11}$	$c_{12}$	$c_{44}$	$B$	$E$	$G$	$\frac{G}{B}$	$A_Z$	$\nu$
Th <sub>2</sub> C <sub>3</sub>	310	96	84	167	234	92	0.55	0.79	0.27
U <sub>2</sub> C <sub>3</sub>	311	129	101	189	249	97	0.51	1.11	0.28
Shi et al. <sup>3</sup>	383	121	91	208	238 <sup>4</sup>	91 <sup>4</sup>	0.44 <sup>4</sup>	0.69 <sup>4</sup>	0.31 <sup>4</sup>

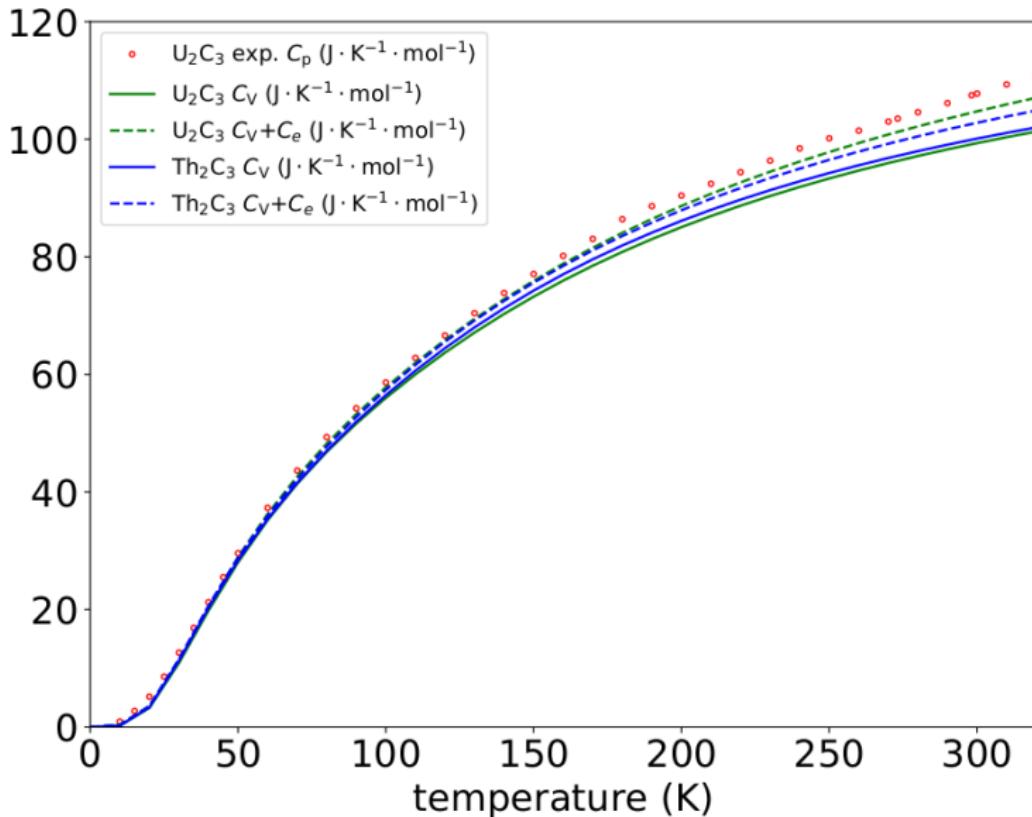
<sup>1</sup>G. Grimvall, *Thermophysical Properties of Materials* (Elsevier, North-Holland, Amsterdam, 1999).

<sup>2</sup>S. F. Pugh, Philos. Mag., 45, 823-843 , (1954).

<sup>3</sup>H. Shi et al., J. Nucl. Mater., 396, 218-222 (2010).

<sup>4</sup>For a cubic system,  $G \approx c_{44}$ ; we calculated marked values using this fact

# Results - Thermodynamic Properties



# Discussion

## Conclusion

- $\text{U}_2\text{C}_3$  is FM with about 0.07 eV/f.u. lower than AFM ordering
- $\text{Th}_2\text{C}_3$  is non-magnetic and stable at 0 K and ambient pressure
- magnetism in  $\text{U}_2\text{C}_3$  originates from the  $\approx 7\times$  more 5f electrons than in  $\text{Th}_2\text{C}_3$
- the chemical bonding in  $\text{U}_2\text{C}_3$  and  $\text{Th}_2\text{C}_3$  is caused by 5f and 6d electrons, respectively
- both phases are anisotropic and lie on the verge of brittle-to-ductile behavior, with  $\text{U}_2\text{C}_3$  being slightly more ductile
  - $\text{U}_2\text{C}_3$ :  $\frac{G}{B} = 0.51$
  - $\text{Th}_2\text{C}_3$ :  $\frac{G}{B} = 0.55$
- calculated temperature dependence of heat capacity with its electronic contribution is in a good agreement with experimental values

<sup>1</sup>H. Shi et al., J. Nucl. Mater., 396, 218-222 (2010).