



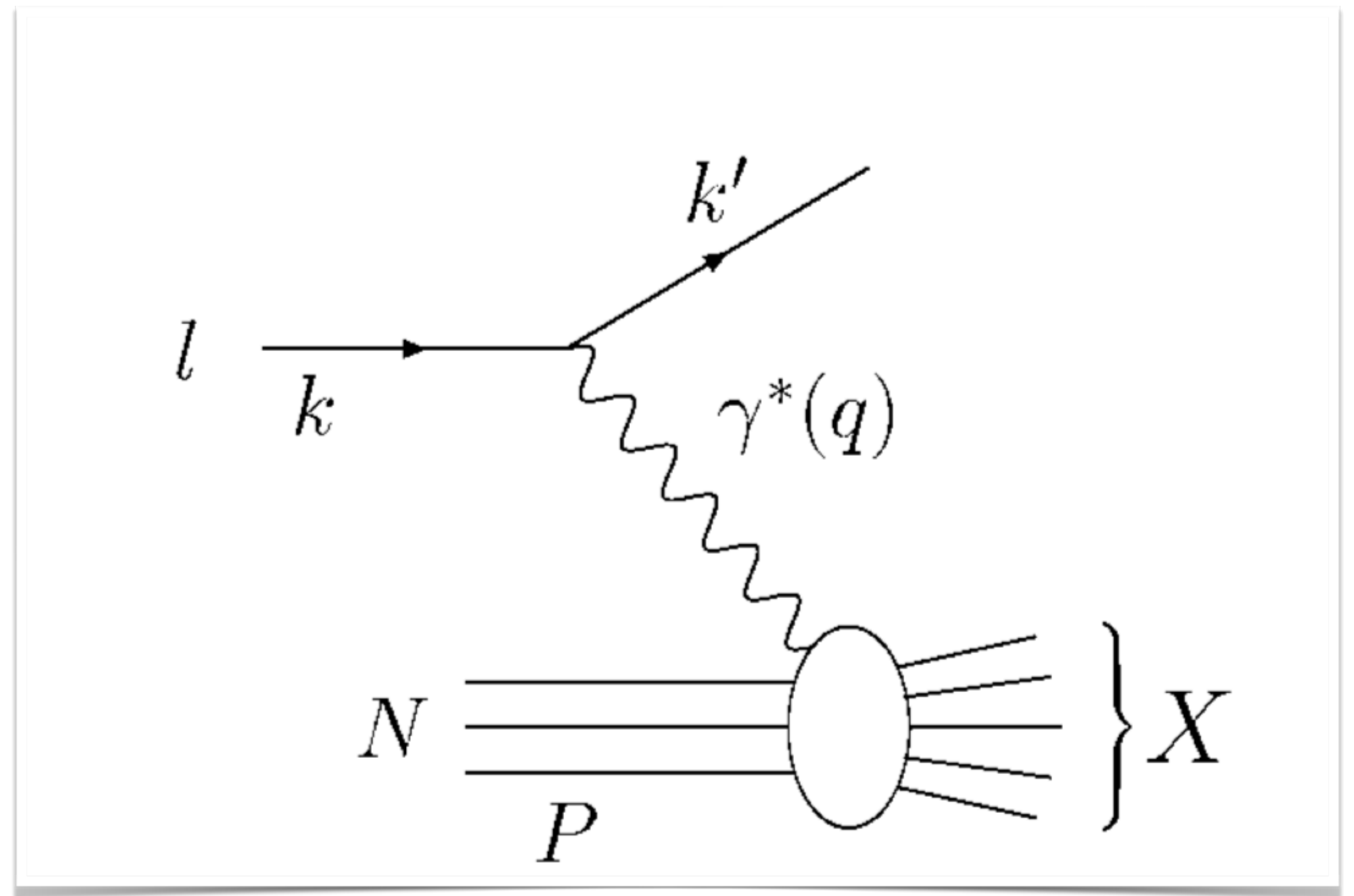
Miniworkshop difrakce a ultraperiferálních srážek
2-3 May, 2018
Děčín, Česká republika

DIS at HERA

J. G. Contreras
Czech Technical University

May 2, 2018, Děčín

The process we are interested in

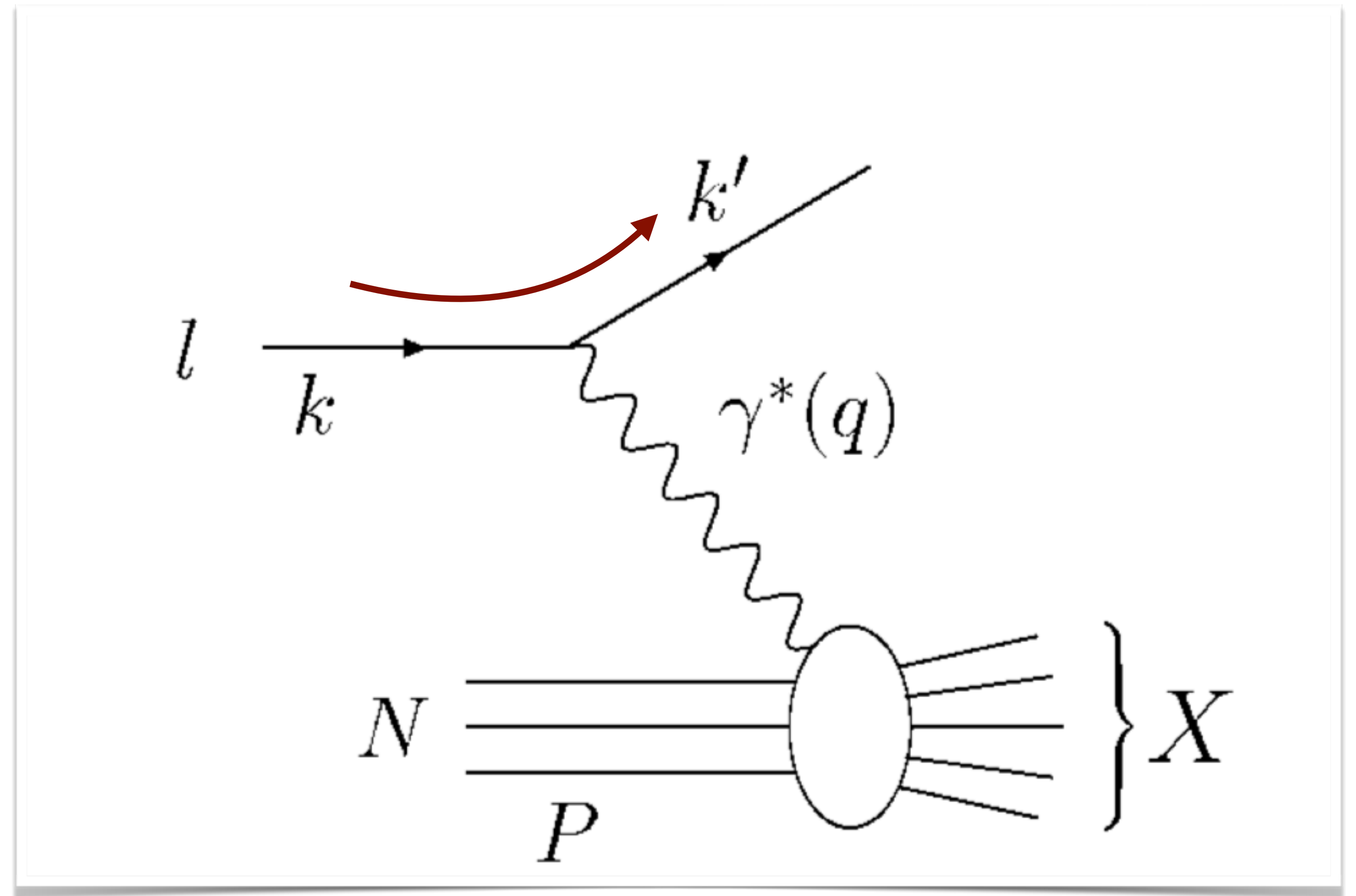


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The process can be factorised in three parts:

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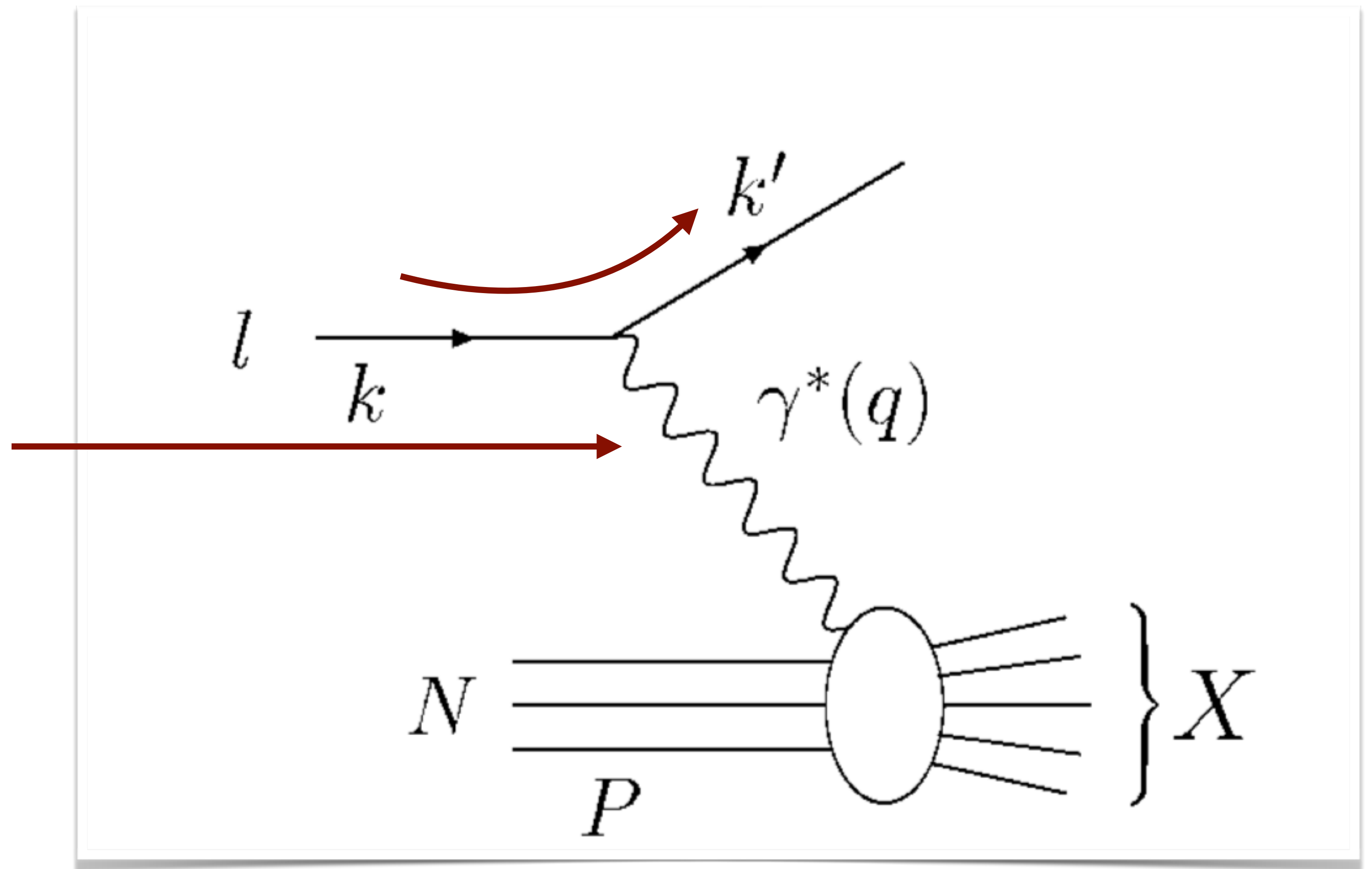
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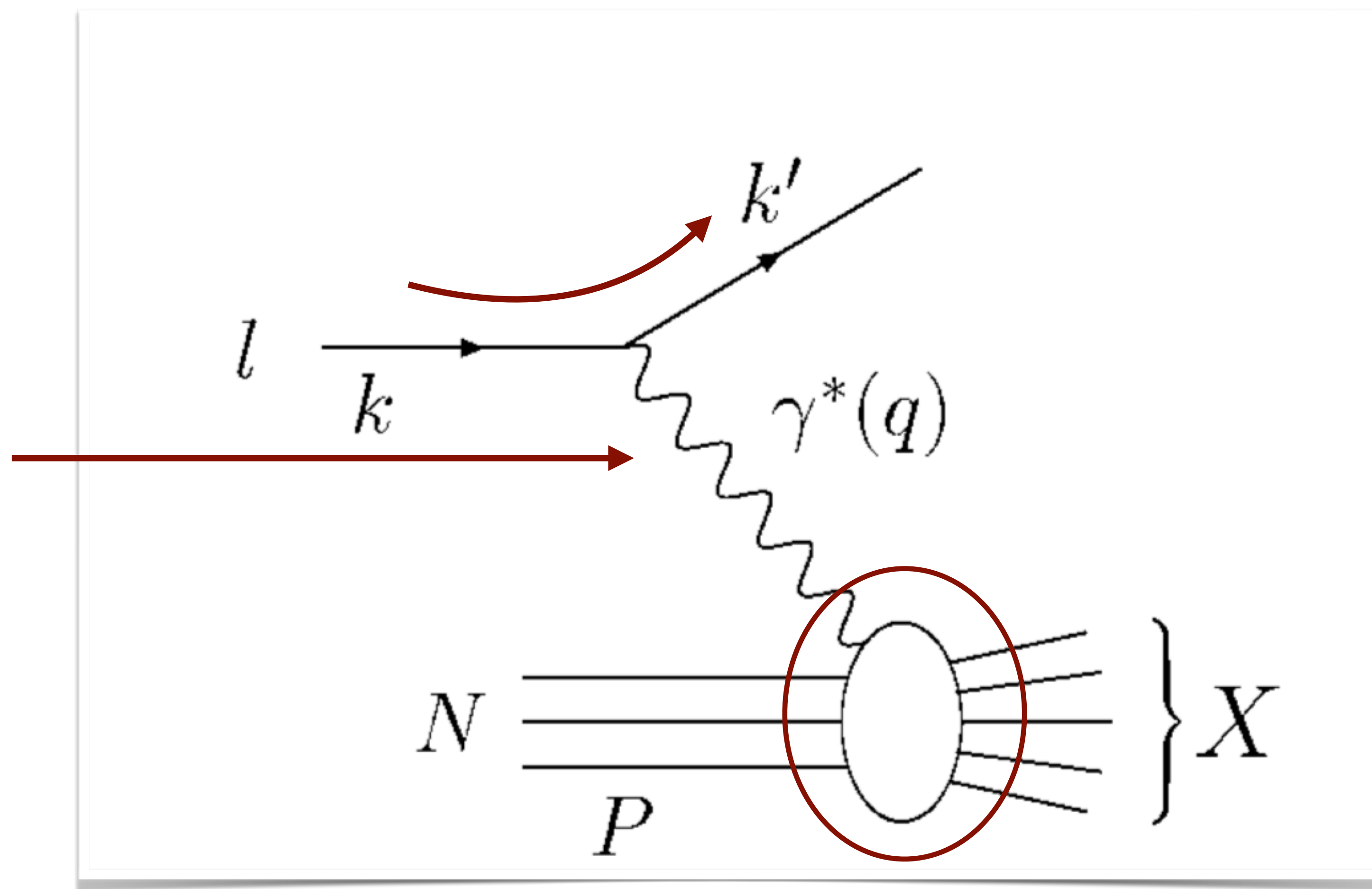
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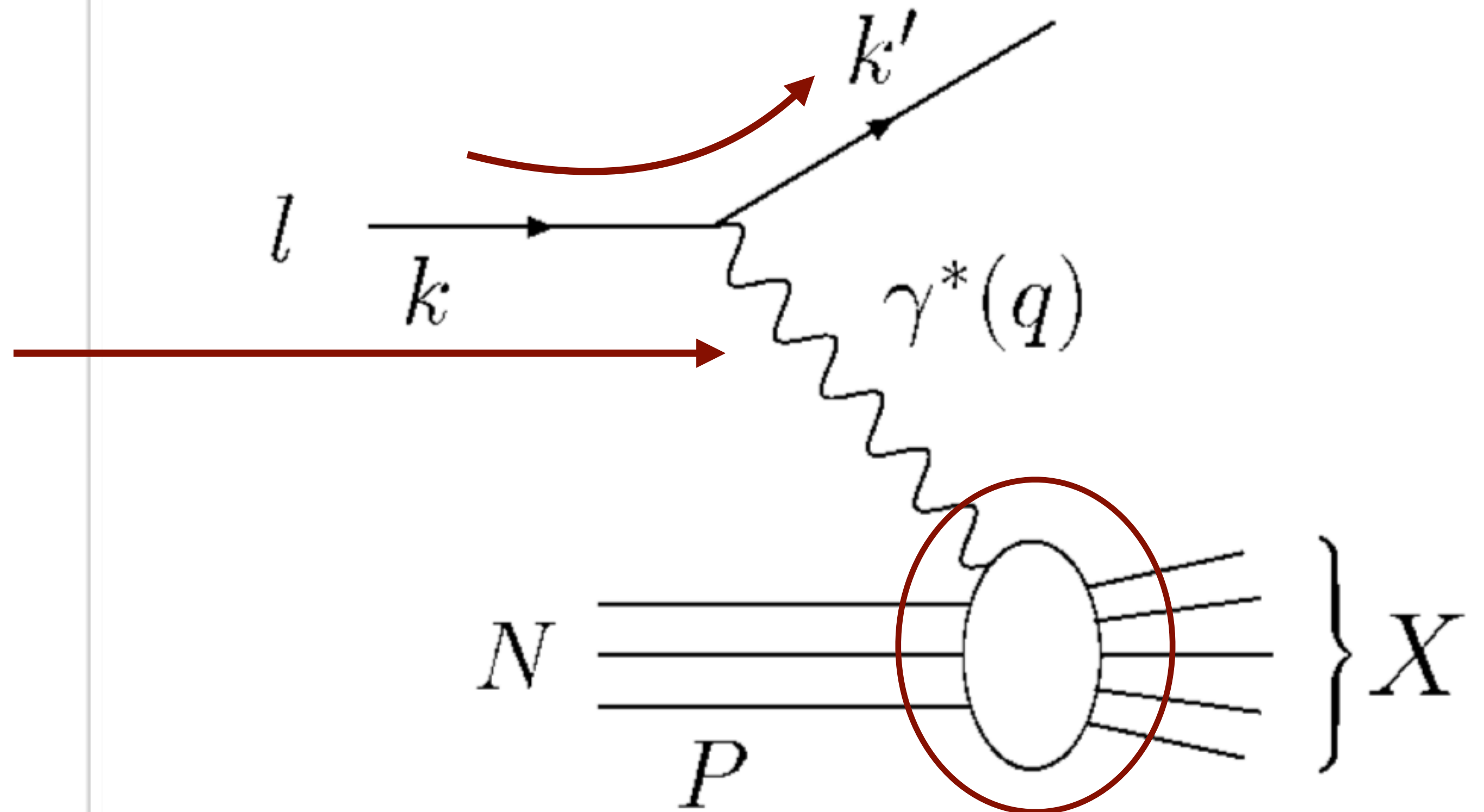


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$$\frac{d^2\sigma}{dx dy} \propto \mathcal{L}_{\mu\nu}(k, q, s) \mathcal{W}^{\mu\nu}(P, q, S),$$

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 & + \frac{P^\mu P^\nu}{Pq} F_2(x, Q^2) - i\varepsilon^{\mu\nu\rho\sigma} \frac{q_\rho P_\sigma}{2Pq} F_3(x, Q^2) + i\varepsilon^{\mu\nu\rho\sigma} q_\rho \left[\frac{S_\sigma}{Pq} g_1(x, Q^2) \right. \\
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Parity violating terms: F_3 , g_3 , g_4 and g_5 . Exchange of a weak vector boson!

The measurements

HERA was operated in two phases: HERA I, from 1992 to 2000, and HERA II, from 2002 to 2007. From 1994 onwards, and for all data used here, HERA operated with an electron beam energy of $E_e \simeq 27.5 \text{ GeV}$. For most of HERA I and II, the proton beam energy was $E_p = 920 \text{ GeV}$, resulting in the highest centre-of-mass energy of $\sqrt{s} \simeq 320 \text{ GeV}$.

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Interpretation in Quark-Parton Model

QCD enters here, but without gluons

$$\begin{aligned}(F_2, F_2^{\gamma Z}, F_2^Z) &\approx [(e_u^2, 2e_u v_u, v_u^2 + a_u^2)(xU + x\bar{U}) \\ &\quad + (e_d^2, 2e_d v_d, v_d^2 + a_d^2)(xD + x\bar{D})], \\ (xF_3^{\gamma Z}, xF_3^Z) &\approx 2[(e_u a_u, v_u a_u)(xU - x\bar{U}) \\ &\quad + (e_d a_d, v_d a_d)(xD - x\bar{D})],\end{aligned}$$

$$\begin{aligned}xU &= xu + xc, & x\bar{U} &= x\bar{u} + x\bar{c}, \\ xD &= xd + xs, & x\bar{D} &= x\bar{d} + x\bar{s},\end{aligned}$$

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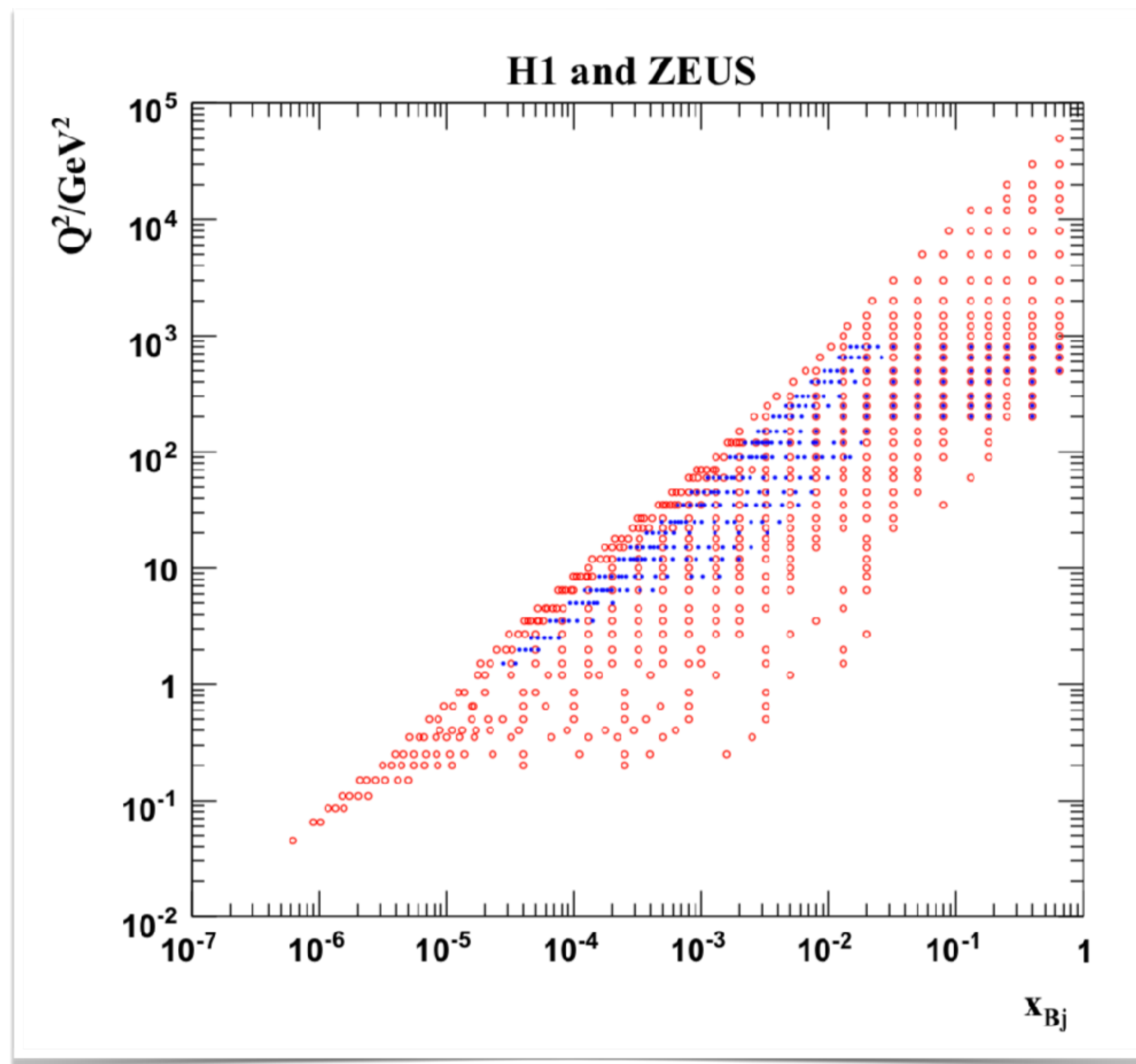
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$$\begin{aligned}W_2^+ &\approx x\bar{U} + xD, & xW_3^+ &\approx xD - x\bar{U}, \\ W_2^- &\approx xU + x\bar{D}, & xW_3^- &\approx xU - x\bar{D}.\end{aligned}$$

$$xu_v = xU - x\bar{U}, \quad xd_v = xD - x\bar{D}.$$

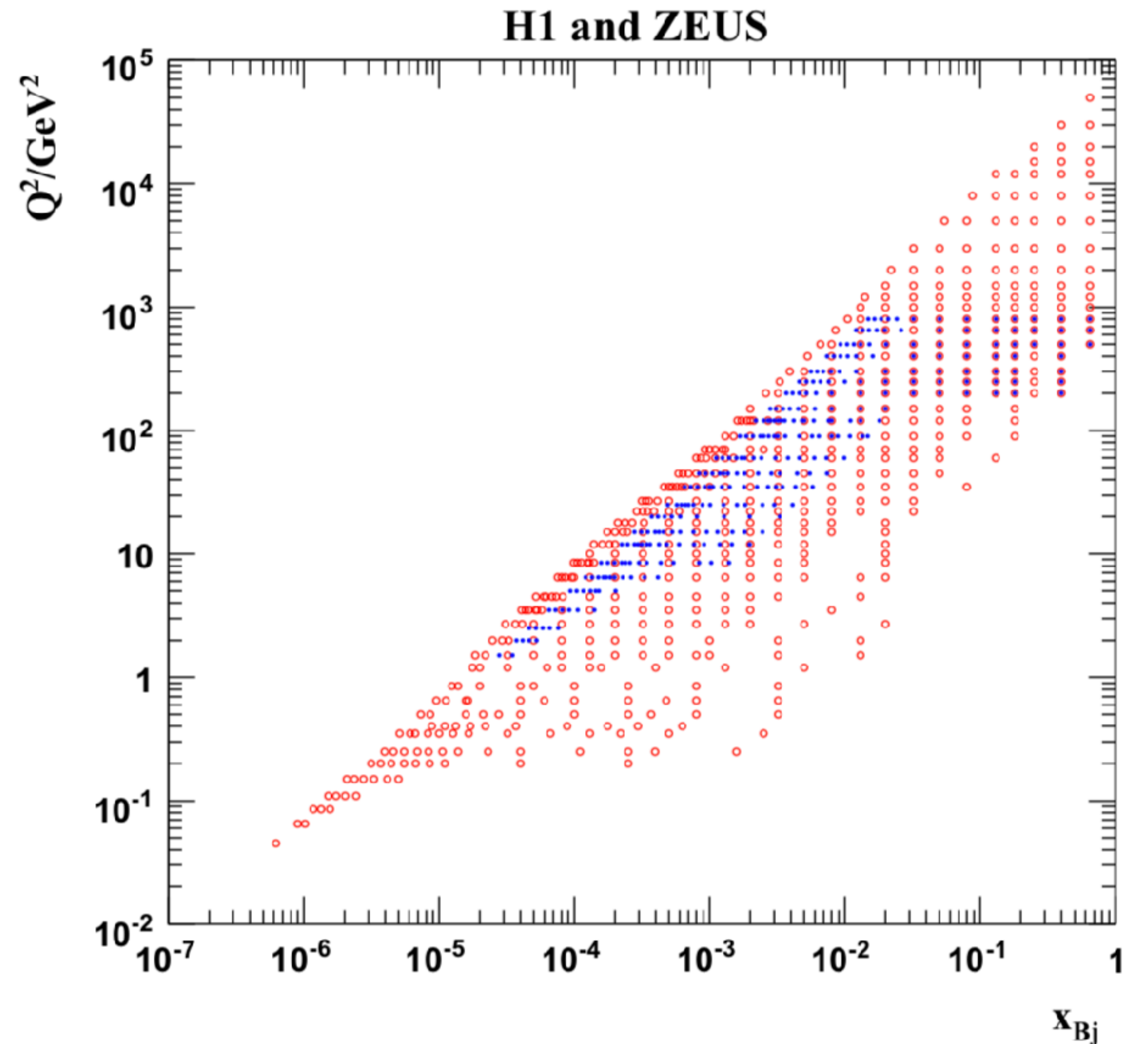
$$\begin{aligned}\sigma_{r,\text{CC}}^+ &\approx (x\bar{U} + (1-y)^2 xD), \\ \sigma_{r,\text{CC}}^- &\approx (xU + (1-y)^2 x\bar{D}).\end{aligned}$$

Phase space covered



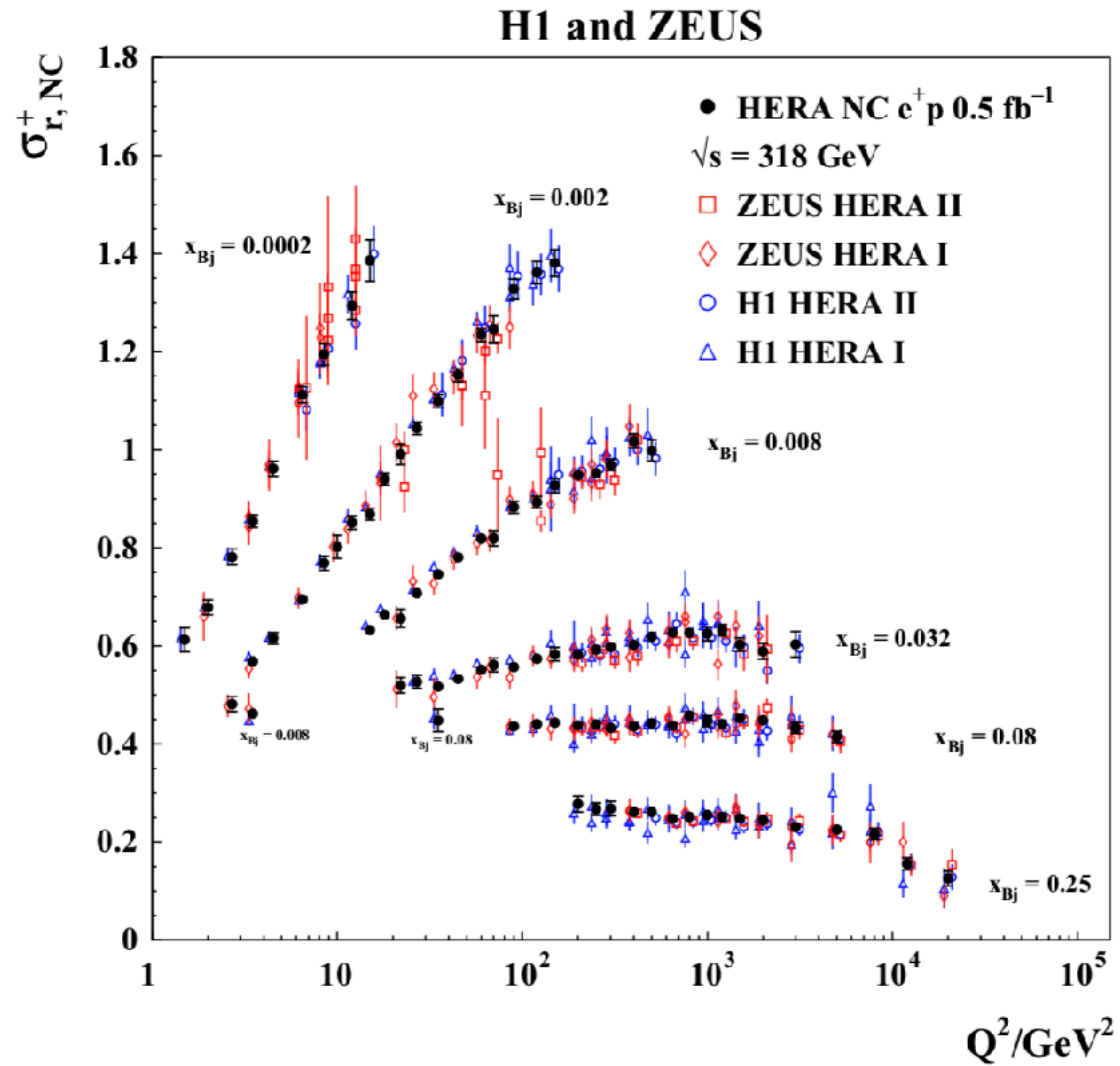
Phase space covered

- Data covers **six orders of magnitude** in x and **six order of magnitude** in Q^2 !
- There is a correlation between them due to finite centre-of-mass energy.
- Data from 1994 to 2007 and from two different collaborations!



Neutral current results

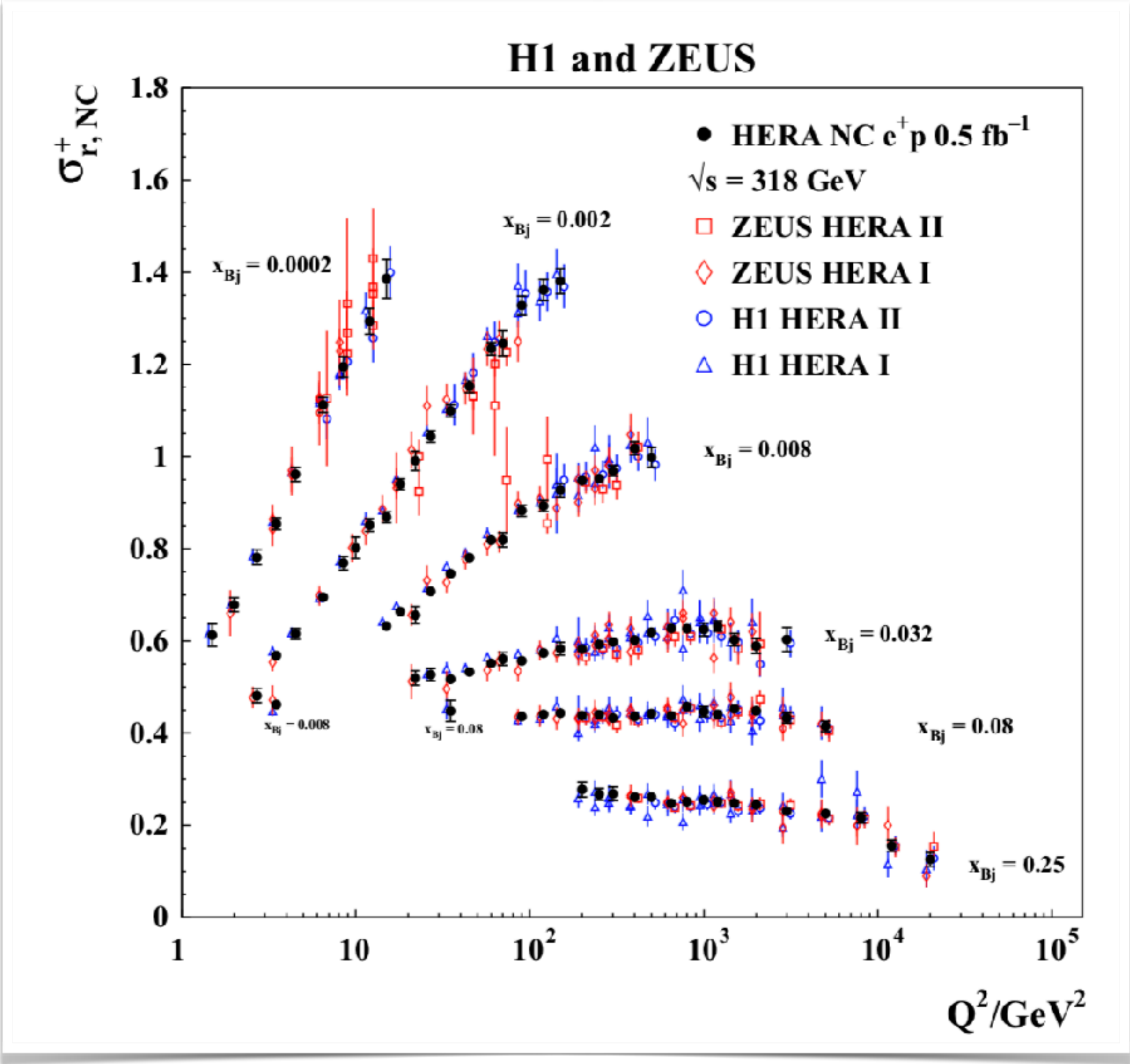
H1 and Zeus, Eur.Phys.J. C75 (2015) no.12, 580



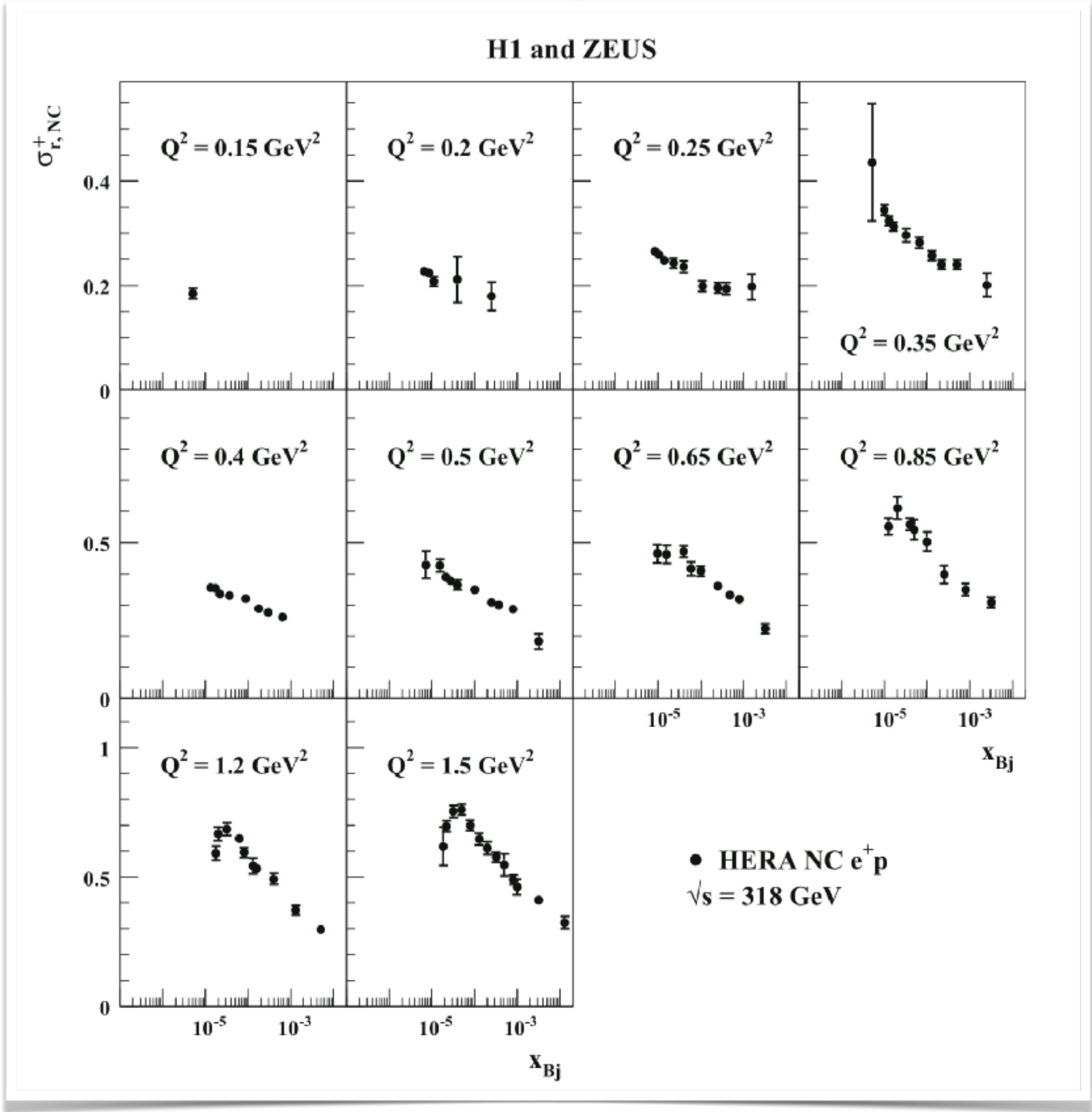
Scaling violations are clearly observed

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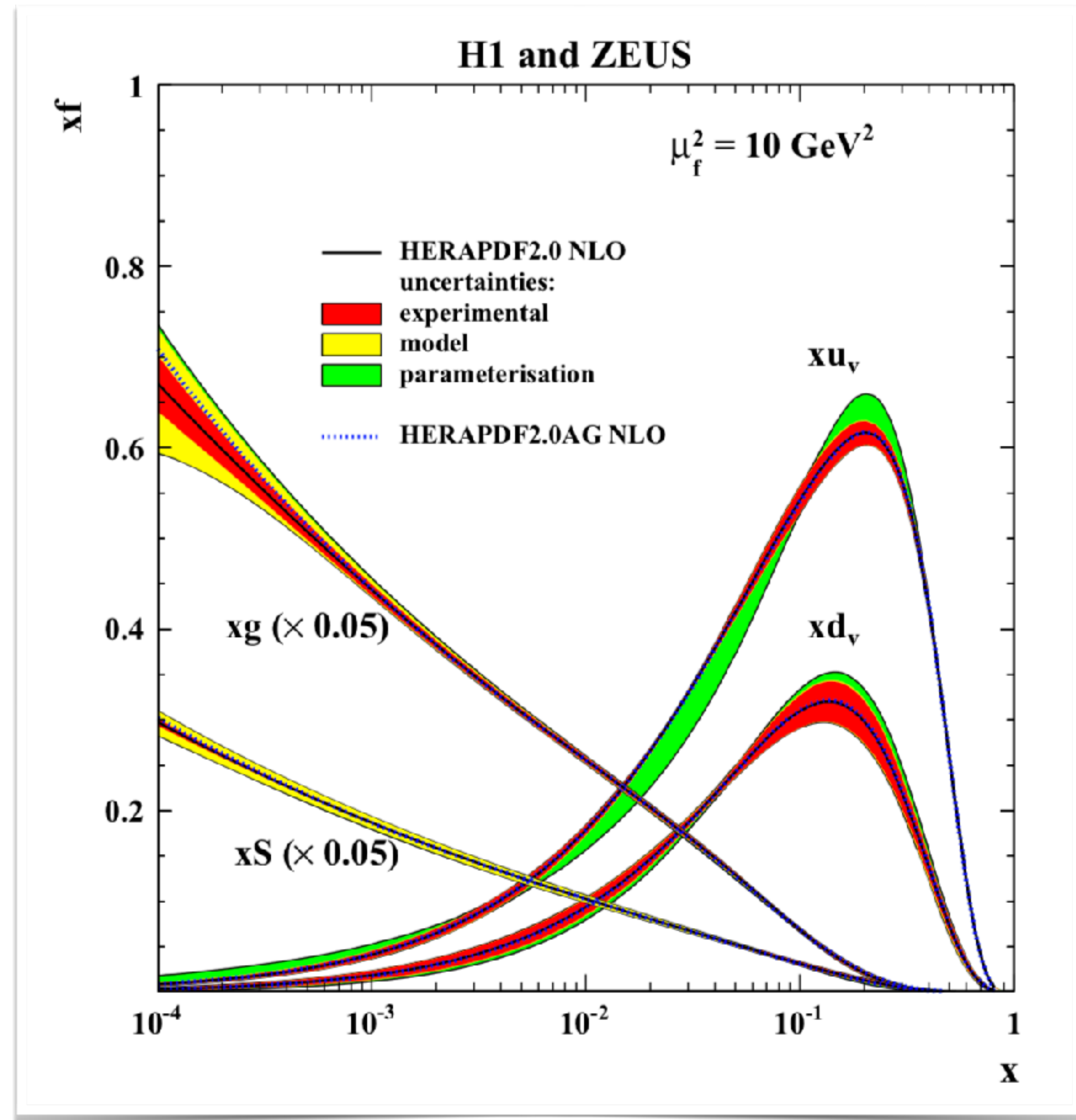
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Power law and effect of F_L clearly seen

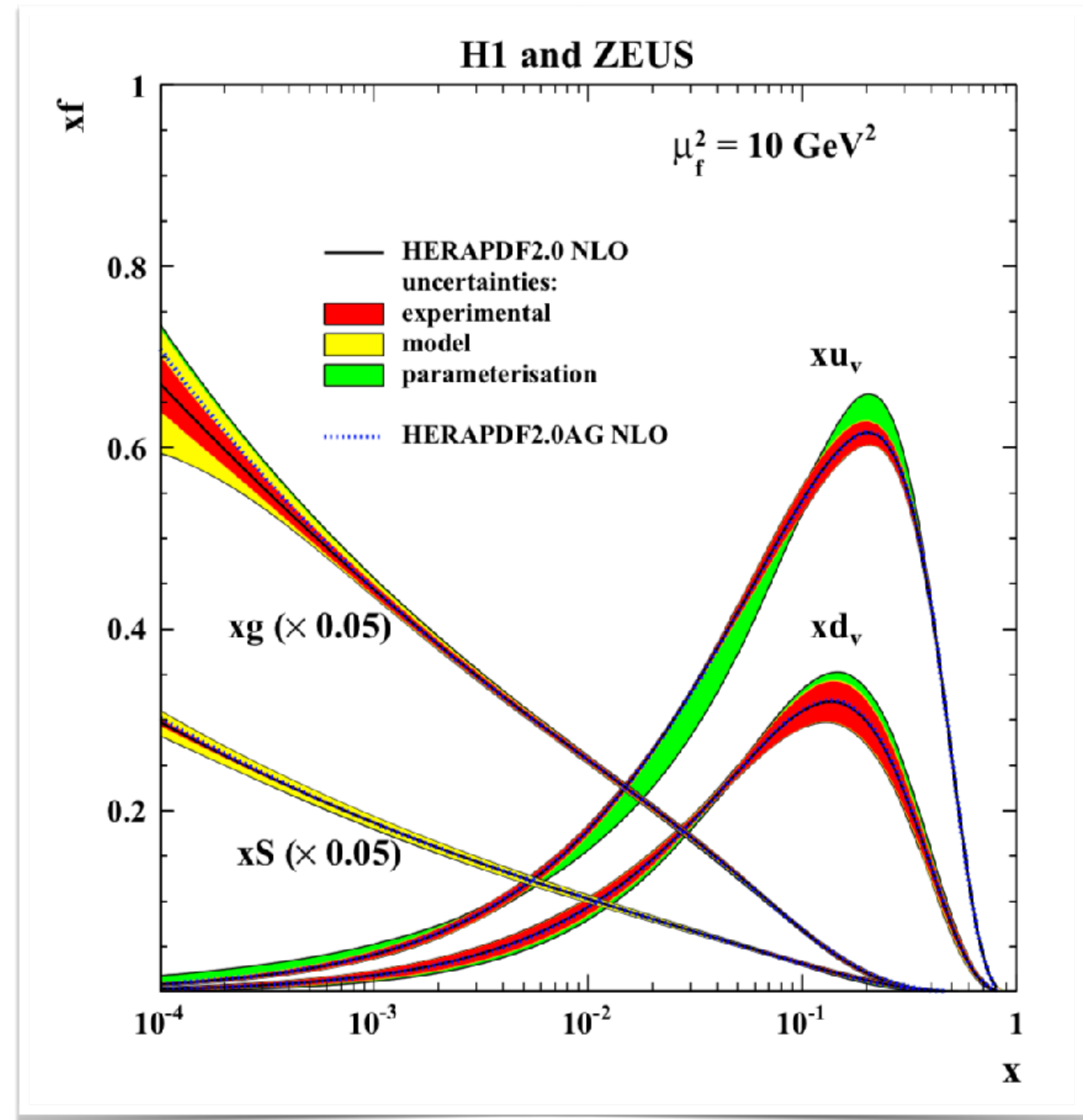
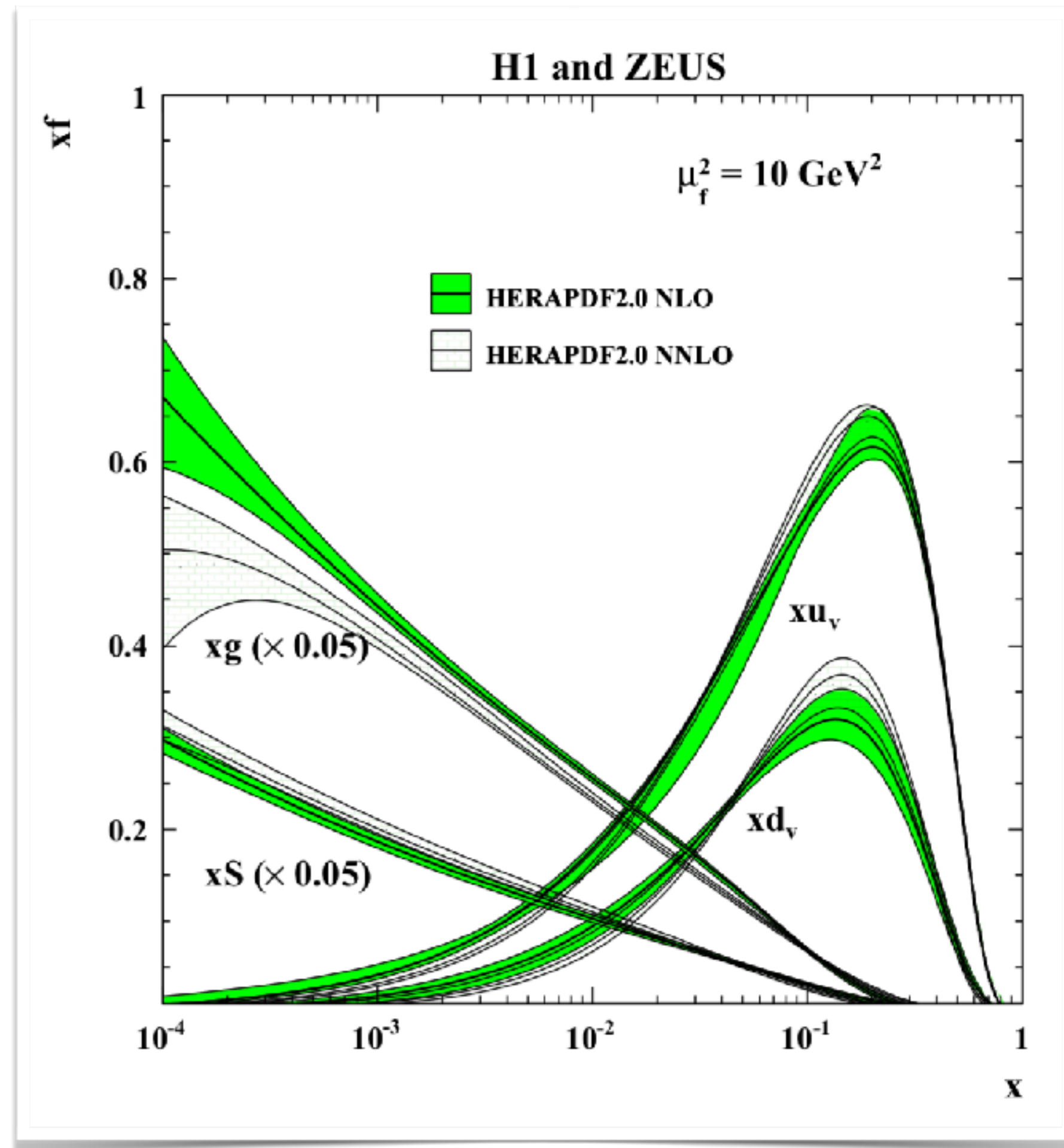
PDF extraction

Use a parameterisation of partons at a given scale and use DGLAP equations to evolve them.



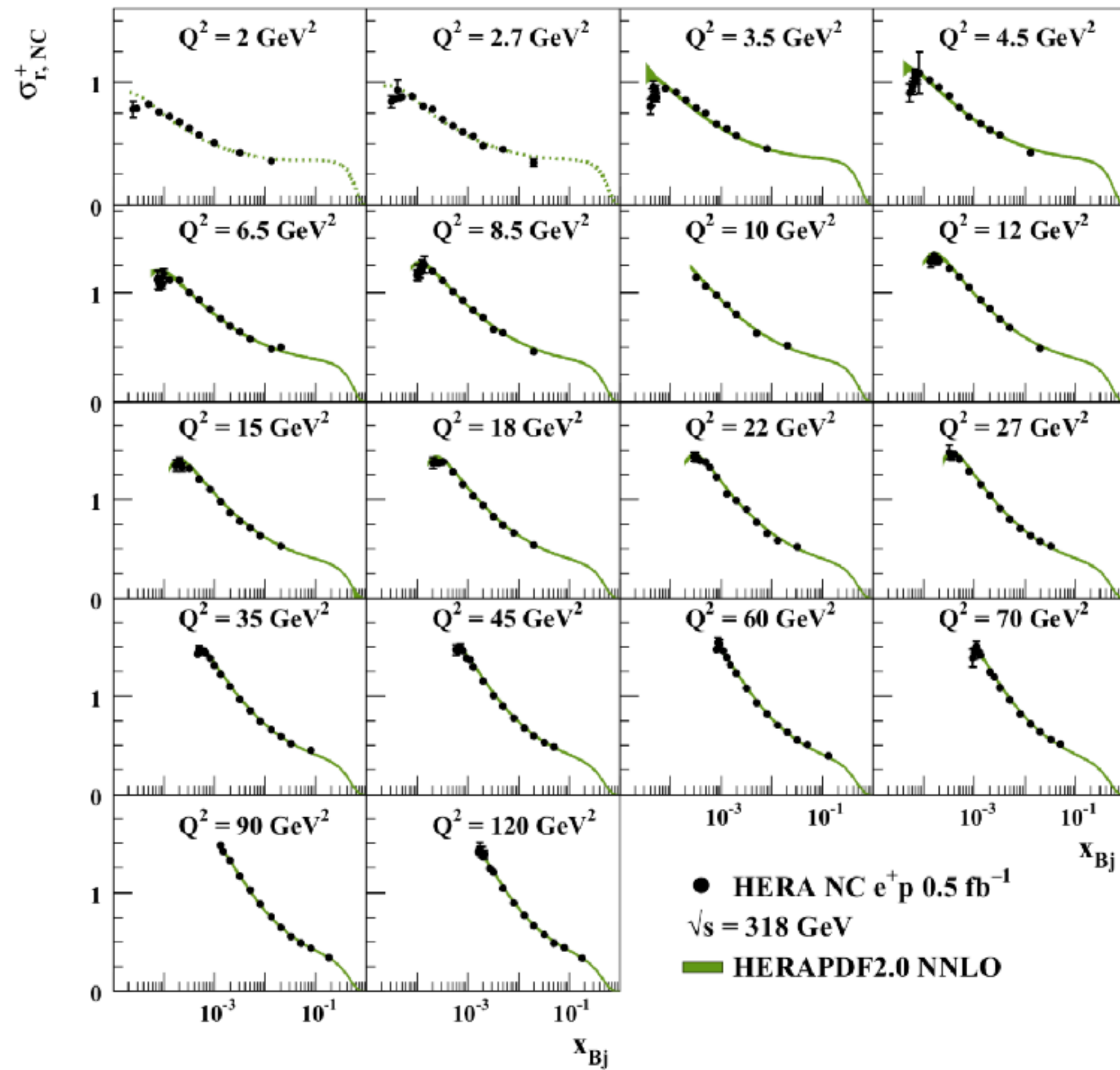
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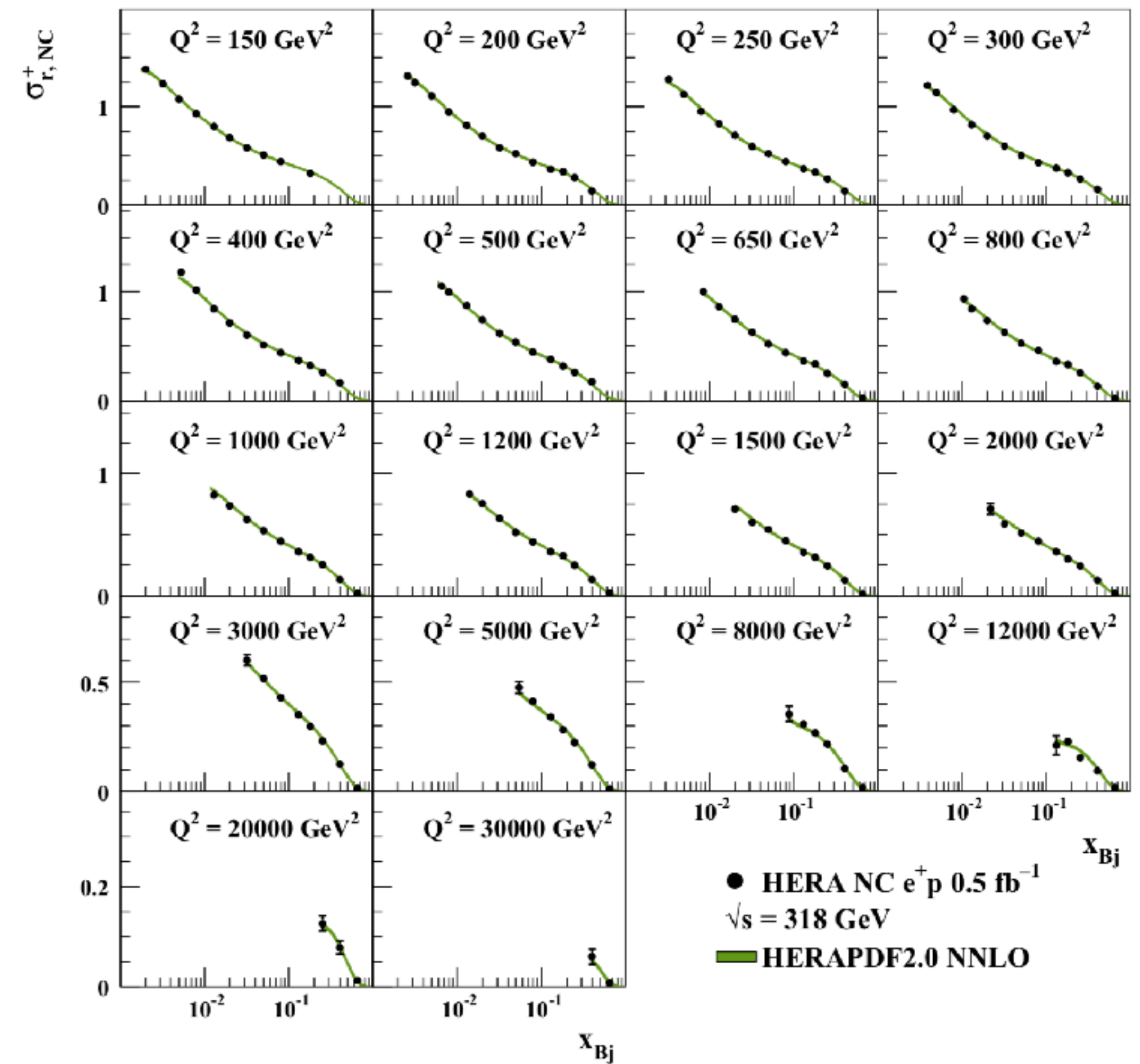


Data DGLAP comparison

H1 and ZEUS



H1 and ZEUS



A text book plot!

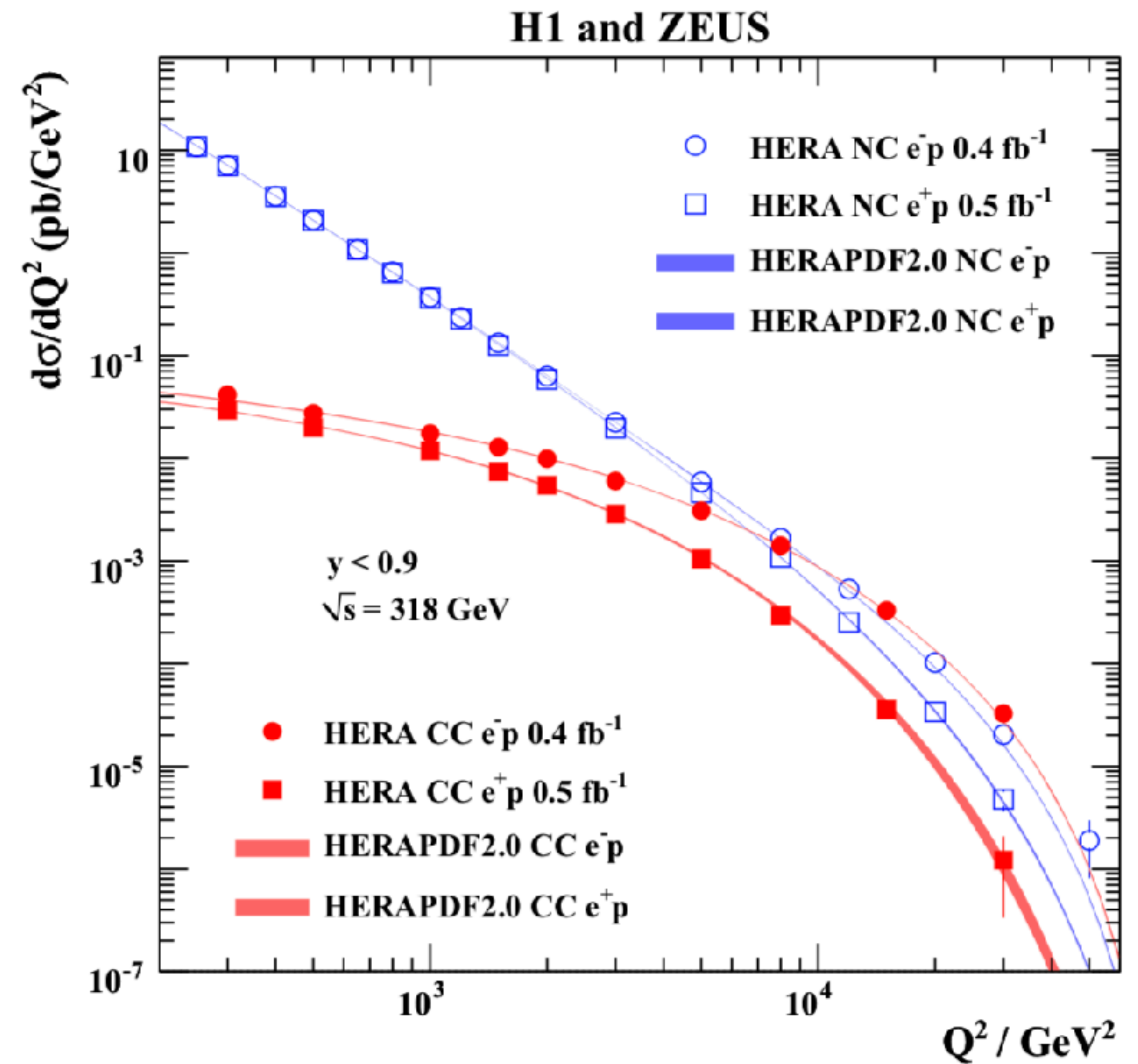


Fig. 74 The combined HERA NC and CC e^-p and e^+p cross sections, $d\sigma/dQ^2$, together with predictions from HERAPDF2.0 NLO. The *bands* represent the total uncertainty on the predictions

An another two :)

